

Partial Safety Analysis for a Reduced Uranium Enrichment Core for the High Flux Isotope Reactor

April 2009

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Research Reactors Division

PARTIAL SAFETY ANALYSIS FOR A REDUCED URANIUM ENRICHMENT CORE FOR THE HIGH FLUX ISOTOPE REACTOR

C. Galvez Velit R. T. Primm, III J. C. Gehin

April 2009

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CONTENTS

LIST	OF TA	BLES	iv
LIST	OF FIG	URES	v
ACK	NOWL	EDGEMENTS	vi
1.0	INTE	RODUCTION	1
2.0	VER	IFICATION AND VALIDATION STUDIES	3
2.0	2.1	International Atomic Energy Agency (IAEA) 10 Megawatt Benchmark	
	2.2	The Massachusetts Institute of Technology — II Reactor	
	2.3	Conclusion from Verification Studies	
	2.4	Validation Studies with Earlier Versions of PARET	
	2.5	Operational Data from HFIR	
3.0	HFIR	MODEL CONSTRUCTION	Q
5.0	3.1	Reactor Geometry and Neutronics Input	
	3.2	Core Materials Description	
	3.3	Neutronic Parameters.	
	3.4	Operating Parameters	
	3.5	Control Systems	
	3.6	Thermal Hydraulic Parameters	
	3.7	Channel Dependent Flow Rates	
4.0	RESU	ULTS OF CALCULATIONS	31
5.0	CON	CLUSION	20
J.U	CON	CLUSION	39
6.0	REFI	ERENCES	41
APPE	ENDIX A	Α	45

LIST OF TABLES

2.1	Representative validation studies for PARET with other reactors	7
3.1	Relative pwoer distribution for the inner fuel element, HEU, beginning-of-cycle	12
3.2	Relative power distribution for the inner fuel element, HEU, end-of-cycle	13
3.3	Relative power distribution for the outer fuel element, HEU, beginning-of-cycle	14
3.4	Relative power distribution for the outer fuel elelment, HEU, end-of-cycle	15
3.5	Equivalent diameter for each core region in PARET HEU model	16
3.6	Relative power distribution for the inner fuel element, LEU, beginning-of-cycle	17
3.7	Relative power distribution for the outer fuel element, LEU, beginning-of-cycle	18
3.8	Relative power distribution for the inner fuel element, LEU, end-of-cycle	19
3.9	Relative power distribution for the otuer fuel element, LEU, end-of-cycle	20
3.10	Nested tube model dimensions	23
3.11	Core and fuel plate geometric data	24
3.12	Fuel and clad material thermal property coefficients	
3.13	Reactor kinetics parameters for HEU fuel	
3.14	Reactor kinetics parameters for LEU fuel	27
3.15	Typical operational parameters	28
3.16	Control systems data for HEU model	29
3.17	Control systems reactivity work for HEU fuel	29
3.18	Thermal hydraulic dta and correlations used	30
4.1	Primary coolant pump seizure initial and boundary conditions	31
A.1	Prompt neutron lifetime and effective delayed neutron fractions for the HFIR HEU cor-	e
	(critical conditions throughout the cycle)	51
A.2	Prompt neutron lifetime and effective delayed neutron fractions for the HFIR LEU	
	(monolithic U-10Mo) core (critical conditions throughout the cycle)	51
A.3	Contributions to effective delayed neutron fraction by nuclide for the HEU and LEU co	ores
	computed with ENDF/B-VII.0 data	51

LIST OF FIGURES

1.1	Block diagram of PARET program	2
2.1	IAEA (right) horizontal core cross section	3
2.2	Transient response of benchmark core to reactivity insertion of \$0.50/0.5 s with an	
	overpower scram trip at 12 MW and a 25 ms delay from Ref. 4.	4
2.3	Transient response of benchmark core to reactivity insertion of \$1.50/0.5 s with an	
	over-power scram trip at 12 MW and a 25 ms delay (this work)	5
2.4	Comparion of LEU fuel temperature during a reactivity transient as reported by	
	Newton using an old version of PARET (top) and the version 7.2 of PARET (bottom, this work)	6
	(bottom, this work)	0
3.1	HFIR core configuration	9
3.2	HFIR involute fuel plates showing variable fuel "meat" thickness within the fuel plate	10
3.3	HFIR simplified core discretization scheme	
3.4	Radial mesh spacing; inner fuel element	11
3.5	Radial mesh spacing for outer fuel element	12
3.6	PARET model spatial discretization	15
3.7	Plate radial subsectioning used in thermal hydraulic calculation in PARET	
	(same plate in each radial emenent in reactor model)	21
3.8	Conversion of "nested tube" model	21
3.9	Fuel thickness inside plates for inner elements	22
3.10	Fuel thickness inside plates for outer fuel elements	22
3.11	Fuel plate discretization	23
3.12	Thermal conductivity variation as a function of temperature for typical U-A1 fuel	
	For varioius enrichments	25
4.1	Mass flux functions for transient in discussion. Note negative values of mass flux	
	As they indicte the downward direction of flow that exists in the HFIR core	33
4.2	Volumetric flow rate for this transient as found in the most recent version of the	
	USAR of the HFIR. Both initial and final values of he flow are equivalent to the	
	ones shown in the graph, only expressed in different parameters	33
4.3	Power profile for primary pump seizure at beginning-of-life	
4.4	Power profile for HEU transientasf ound in the USAR	
4.5	Reactivity profile of the reduction in primary flow transient as calculated with PARET	
4.6	Fuel temperature profile for several core regions for HEU for pump seizure transient	36
4.7	Fuel temperature for transient as reproduced by the USAR	36
4.8	Fuel temperature profile for several core regions for LEU for transient	
A.1	Selected data from ENDF/B-VI.8 library	47
A.2	Selected data from ENDF/B-VII.0 library	
A.3	Comparison of the number of delayed neutrons from ²³⁵ U fission from ENDF/B-VI.8 and	
	ENDF/B-VII.0 (ENDF/B-VI.8 is identical to ENDF/B-V data)	50

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ABSTRACT

A computational model of the reactor core of the High Flux Isotope Rector (HFIR) was developed in order to analyze non-destructive accidents caused by transients during reactor operation. The reactor model was built for the latest version of the nuclear analysis software package called Program for the Analysis of Reactor Transients (PARET). Analyses performed with the model constructed were compared with previous data obtained with other tools in order to benchmark the code. Finally, the model was used to analyze the behavior of the reactor under a transient using a different nuclear fuel with lower enrichment of uranium (LEU) than the fuel currently used, which has a high enrichment of uranium (HEU). The study shows that the presence of fertile isotopes in LEU fuel, which increases the neutron resonance absorption, reduces the impact of transients on the fuel and enhances the negative reactivity feedback, thus, within the limitations of this study, making LEU fuel appear to be a safe alternative fuel for the reactor core.

1.0 INTRODUCTION

An initiative to investigate the feasibility of low-enriched uranium fuel as a potential alternative fuel for the High Flux Isotope Reactor (HFIR) originated from the Reduced Enrichment for Research and Test Reactors (RERTR). The proof of principle of this project was performed by R T. Primm [1] in a study based on only minor changes to the current fuel design, namely, the thickness of the fuel within the fuel plate.

After this preliminary study was performed, the next logical step was to analyze the safety of this potential fuel for the HFIR. The desired safety analysis would provide information on the behavior of this new fuel design under anticipated transients. At the same time, it was brought to the attention of the author the existence of a nuclear safety computer code called PARET which had not been employed before in this reactor design, and appeared to be an appropriate choice as the main research tool.

There are many potential accident scenarios to be studied, and they are explained in detail on the HFIR Updated Safety Analysis Report [2]. Given that this study is the initial safety analysis being performed, and given the time constrains of the project, the present study was limited to one class of transients. The chosen transient was the primary coolant pump seizure.

PARET [8] is a computer code which iteratively solves for the neutronic-hydrodynamic-heat transfer aspect of the reactor under steady state and transient behavior. This code uses the point reactor kinetics relations for the neutronic aspect of the analysis; furthermore there are multiple laminar and turbulent correlations for the hydrodynamic part and finally an array of heat transfer correlations as well. The user has the capability to select the appropriate correlation based on the operational parameters and the range of data available for the analysis. A simplified diagram showing the functionality of the PARET code is provided in Fig. 1.1, a slightly updated version from that in Ref. 8.

The goals of this study are to:

- 1. obtain an initial assessment of the safety of the new fuel design, and
- 2. access PARET as a safety analysis tool for the reactor core in question.

Initially, PARET will be used to benchmark against previously published problems by other researchers that used similar tools in other reactor designs and other transients. After this is accomplished, PARET will be used to re-analyze previously documented transients of the current fuel design, namely highly enriched uranium fuel, and this will allow an initial assessment of the applicability of PARET on the safety analysis of the low enriched uranium fuel. The results of this study will be used as a starting point for a complete safety analysis for the new fuel design.

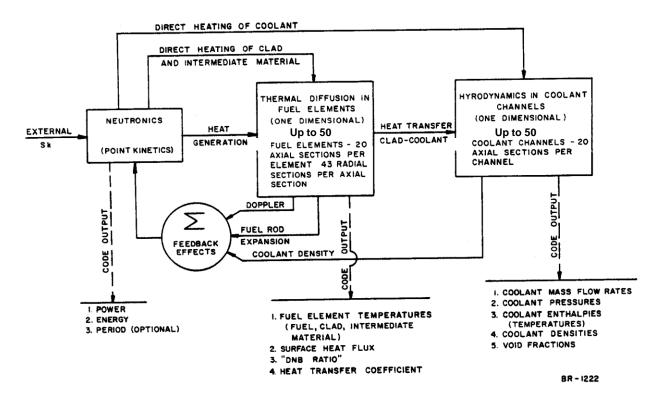


Fig. 1.1. Block diagram of PARET program.

2.0 VERIFICATION AND VALIDATION STUDIES

The version of PARET used in this study is 7.2 and was obtained from A. P. Olson of Argonne National Laboratory [9]. Both WINDOWS and LINUX versions of the code were supplied and both were tested in this project. All calculations reported here were performed with the LINUX version.* Before the code can be used to represent the HFIR reactor core, it is necessary to benchmark it against results published by other researchers obtained with previous versions of the PARET code.

2.1 International Atomic Energy Agency (IAEA) 10 Megawatt Benchmark

A 10-MW research reactor core is defined in Ref. 3 in sufficient detail to serve as a benchmark for the PARET code. The IAEA reactor core is shown in Fig. 2.1 and contains four different regions. Three of the core regions are made up of fuel assemblies that are physically similar to each other, but have different fuel enrichments. These three regions are shown shaded in Fig. 2.1. The fourth core region is the fuel-control assembly and there are four of these fuel assemblies in this core. The control elements are the eight white vertical rectangles in Fig. 2.1.

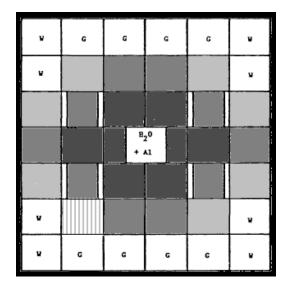


Fig. 2.1. IAEA (right) horizontal core cross section.

The benchmark problem consists of a fast reactivity insertion as described by Woodruff [4]. An input file for the problem was distributed with the PARET code and was used as a didactic tool as well as a base for building the dataset for HFIR. Published results from [4] obtained by using an older version of PARET and also using the RELAP code [5] are shown in Fig. 2.2. Corresponding graphs produced from the output of the current version of PARET are shown in Fig. 2.3. The power profile, peak clad temperature, and peak coolant temperature from the current work all match well to published results in Ref. 4. Peak fuel temperature from the current calculation is slightly lower than that reported in Ref. 4. A change in the materials properties library might be an explanation for the difference.

^{*} ORNL Software Registry System ID is 1424.

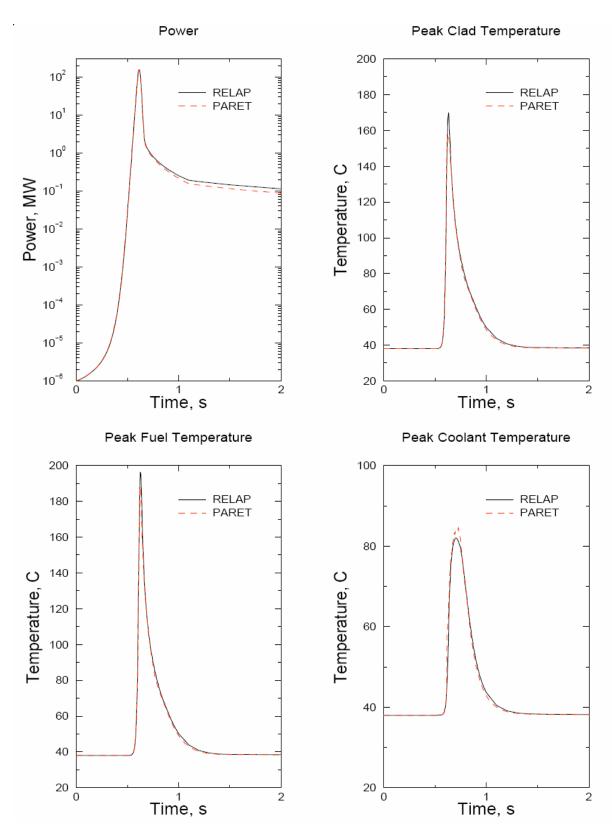
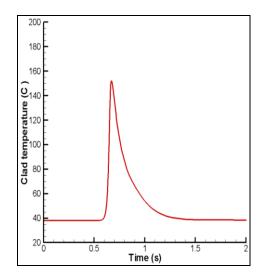


Fig. 2.2. Transient response of benchmark core to reactivity insertion of \$1.50/0.5 s with an overpower scram trip at 12 MW and a 25 ms delay from [4].

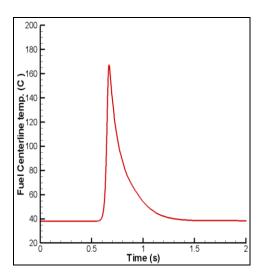
Power

10² 10¹ 10² 10³ 10³ 10⁴ 10⁵ 10⁵ 10⁵ 1.5 2

Peak Clad Temperature



Peak Fuel Temperature



Peak Coolant Temperature

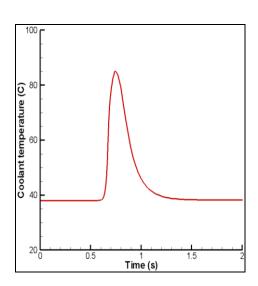
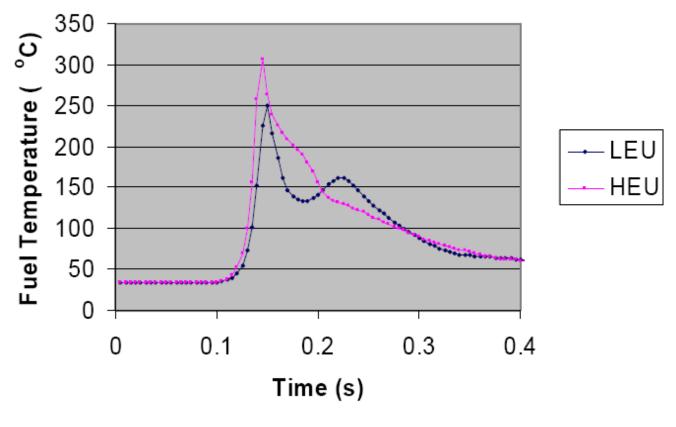


Fig. 2.3. Transient response of benchmark core to reactivity insertion of \$1.50/0.5 s with an over-power scram trip at 12 MW and a 25 ms delay (this work).

2.2 The Massachusetts Institute of Technology – II Reactor

The next problem used to benchmark PARET is a reactivity insertion transient at the MIT research reactor (see [6] for reactor description and description of transient). The input file used is provided by Newton [6], who performed a similar study on the mentioned research reactor. As the previous benchmark problem, Newton utilized the older version of PARET. Figure 2.4 shows the level of agreement between the current work and that reported in Ref. 6.



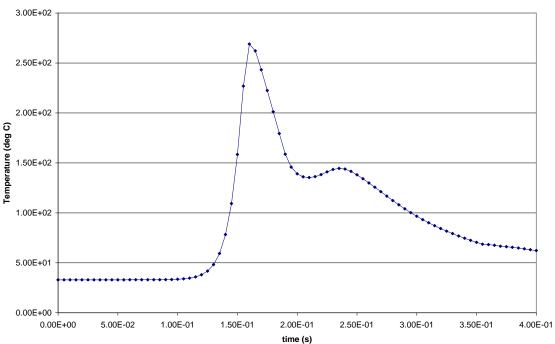


Fig. 2.4. Comparison of LEU fuel temperature during a reactivity transient as reported by Newton using an old version of PARET (top) and the version 7.2 of PARET (bottom, this work).

2.3 Conclusion from Verification Studies

The only input datasets available to the authors were the two discussed in previous sections. It can be inferred from the IAEA and MIT studies that the new version of PARET (7.2) was successfully installed at ORNL and this new version produces results that are consistent with prior versions of PARET. Thus, it is reasonable to apply this code to the HFIR reactor core as it appears capable to handle transients of interest.

2.4 Validation Studies with Earlier Versions of PARET

A search of the web-based, Reduced Enrichment for Research and Test Reactors publication database (www.rertr.anl.gov) revealed that calculation-to-experiment comparisons had been made with versions of PARET for three research reactors [11-13]. Table 2.1 provides a brief summary of the levels of agreement between calculations and experiments that are reported in these references. In no case was the result of the PARET calculation non-conservative, i.e. less than measurement.

Table 2.1. Representative validation studies for PARET with other reactors

	•	Calculation-to-experiment ratio						
Ref. number	Reactor	Peak clad	Peak power	Core outlet coolant temperature	Margin to incipient boiling			
11a	SPERT-IV	Always >1.0, max of 1.73 for \$1.8 transient	1.0-1.1	-	-			
12a	MNSR	-	-	~1.0	Agrees with prediction from correlation derived from expts for 3.77 mk transient			
13a	ORR	-	1-2.75	-	-			

Computer programs can be validated by comparison to other, similar computer programs for which the level of accuracy is known over a specified area of applicability (see Fig. 2.2). Several computational comparisons among PARET and other codes have been documented [14 - 17] but are not reviewed here.

2.5 Operational Data from HFIR

Records in the operators' log books for the HFIR exist that can be used to validate the PARET program and associated materials property library. These include:

- 1) shutdown from full power coolant outlet temperature as a function of time,
- 2) as rods are pulled at startup and power increases at some rate, outlet coolant temperature as a function of time, and
- 3) power change as a function of time due to reactivity insertion caused by "rabbits" (capsules) inserted in the hydraulic tube located in the central target region of HFIR [18].

The object of the studies documented in this report was to create the PARET models for HEU-fuelled and LEU-fuelled HFIR cores. A follow-on study could use the models to conduct validation studies with these HFIR operational data.

3.0 HFIR MODEL CONSTRUCTION

It is necessary to define the following terms as they will be used throughout this document. For any type of reactor – power or research or other - the reactor core is a three dimensional body that typically can be represented in terms of two dimensional core regions perpendicular to the unidirectional flow of coolant (i.e., axial slices through the three dimensional body). Each "slice" or core region is frequently composed of multiple fuel assemblies and each fuel assembly consists of multiple fuel plates and coolant channels.

3.1 Reactor Geometry and Neutronics Input

The core design of the HFIR is shown in Fig. 3.1 and differs from the typical plate-fueled reactor core. As it can be observed, the HFIR reactor core is made up of two regions, the inner and outer annulus which contains the curved fuel plates. These two regions are different since the fuel plates that make up each region contain different uranium loadings and differing curvatures. The control elements are the two sparsely shaded outer annuli in the HFIR core.

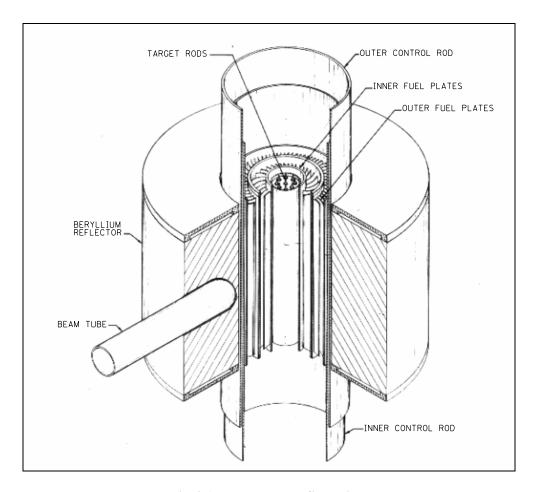


Fig. 3.1. HFIR core configuration.

The HFIR fuel plates are curved, with an involute shape, whereas the fuel plates of the IAEA core (Fig. 2.1) are flat plates. There are 23 fuel plates per fuel assembly and 17 fuel plates per fuel-control assembly in the IAEA core. In the HFIR core there are 171 fuel plates in the inner fuel region and 369 fuel plates in the outer fuel region (refer to Fig. 3.1). In addition to this difference, the layer of fuel in the HFIR does not have constant thickness along the width of the fuel plate, however the standard fuel plate, such as that of the IAEA core has a constant fuel layer thickness along the width of the fuel plate [7]. Fuel plates for the inner fuel element have a different arc of curvature from those of the outer fuel element (see Fig. 3.2).

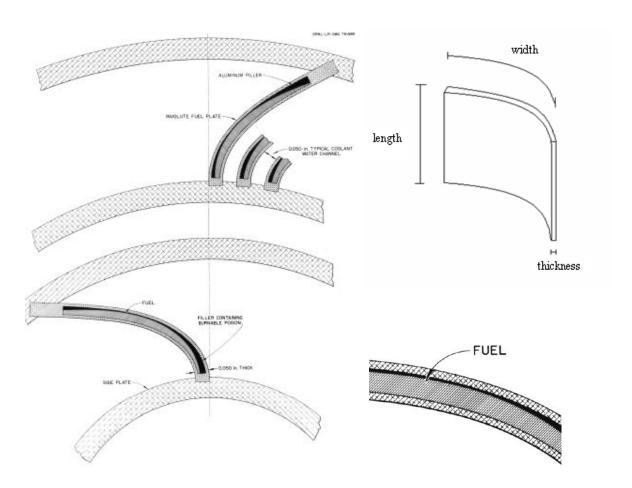


Fig. 3.2. HFIR involute fuel plates showing variable fuel 'meat' thickness within the fuel plate.

In order to model the HFIR core in PARET, is necessary to decide the number of core regions that are to be modeled. Given that the power distribution in not uniform across both fuel elements of the reactor, it is necessary to spatially discretize the reactor core so as to model these non-uniformities. The discretization must be such that there are enough nodes as to accurately describe the power distribution, yet should not be so large as to lead to long computational time due to an unnecessary large number of mesh points. Thus, a discretization must be done to the inner and outer fuel elements and along the height of the core such that the ratio of the local power to the average power can be represented in both directions, radial and axial.

Based on the a recent static reactor physics study by Primm [10], the power distribution of each of the two fuel elements of the core can be accurately represented by eight radial regions in the inner fuel and nine radial regions in the outer fuel. Nineteen axial zones were present in the neutronics model – one less than the maximum allowed in PARET. Fig. 3.3 shows this relation for the HEU fuel. Figs. 3.4 and 3.5 show the radial discretization schemes for the inner and outer elements. Axial mesh intervals had a uniform thickness of 3 cm except for the top and bottom interval which were each 0.4 cm and the interval containing the axial midplane which was 2 cm. The power distribution for beginning-of-life in the inner element is presented in Table 3.1

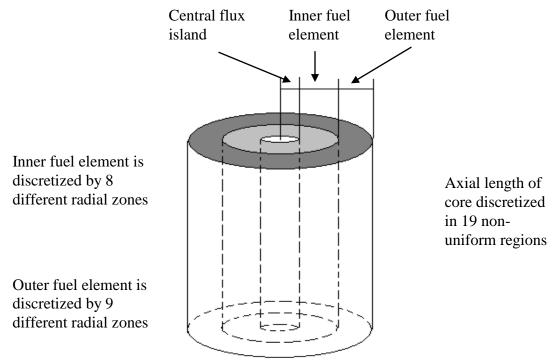
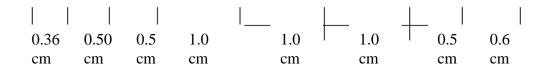


Fig. 3.3. HFIR simplified core discretization scheme.



7.141 cm
Inner radius

12.598 cm
Outer radius

Fig. 3.4. Radial mesh spacing; inner fuel element.

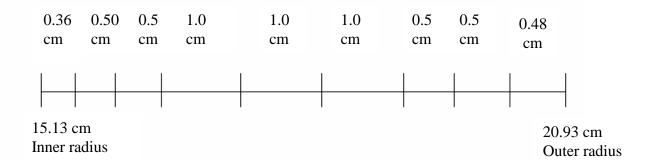


Fig. 3.5. Radial mesh spacing for outer fuel element.

Table 3.1. Relative power distribution for the inner fuel element, HEU, beginning-of-cycle

Power Level Distribution Inner Fuel Element: HEU Fuel

Power Level Distribution Inner Fuel Element: HEU Fuel											
				Rad	ial Mesh						
	No.	1	2	3	4	5	6	7	8		
	19	1.049	1.093	1.145	1.210	1.269	1.231	1.146	1.109		
	18	0.881	0.836	0.811	0.803	0.809	0.807	0.819	0.873		
	17	0.922	0.871	0.833	0.810	0.807	0.817	0.838	0.901		
	16	1.065	1.005	0.960	0.937	0.942	0.956	0.979	1.047		
	15	1.205	1.140	1.093	1.070	1.077	1.093	1.120	1.195		
	14	1.336	1.263	1.205	1.181	1.188	1.213	1.250	1.328		
	13	1.423	1.351	1.298	1.274	1.288	1.312	1.347	1.432		
	12	1.479	1.405	1.351	1.334	1.355	1.384	1.423	1.515		
Axial	11	1.512	1.440	1.391	1.369	1.390	1.420	1.462	1.556		
Mesh	10	1.518	1.445	1.388	1.375	1.392	1.428	1.465	1.563		
	9	1.512	1.437	1.381	1.359	1.382	1.408	1.448	1.544		
	8	1.470	1.397	1.343	1.317	1.337	1.360	1.396	1.485		
	7	1.400	1.328	1.272	1.250	1.259	1.282	1.312	1.397		
	6	1.283	1.217	1.169	1.148	1.155	1.172	1.201	1.279		
	5	1.158	1.097	1.054	1.029	1.038	1.047	1.073	1.145		
	4	1.012	0.961	0.917	0.893	0.897	0.906	0.930	0.990		
	3	0.886	0.831	0.787	0.762	0.762	0.768	0.790	0.843		
	2	0.844	0.801	0.770	0.757	0.757	0.752	0.762	0.816		
	1	0.995	1.044	1.070	1.137	1.183	1.130	1.059	1.020		

Data in Table 3.1 as well as in Tables 3.2 through 3.4 were calculated with the MCNP-V code using a HFIR model documented in Ref. 31. End-of-life power profiles were determined by incorporating the HFIR MCNP model into the ALEPH [32] Monte Carlo depletion code system.

Table 3.2. Relative power distribution for the inner fuel element, HEU, end-of-cycle

	Power Level Distribution Inner Fuel Element: HEU Fuel											
				Rad	ial Mesh							
	No.	1	2	3	4	5	6	7	8			
	19	0.658	0.788	0.906	1.038	1.112	1.094	1.020	0.940			
	18	0.643	0.738	0.805	0.850	0.853	0.837	0.823	0.818			
	17	0.654	0.754	0.815	0.846	0.844	0.833	0.829	0.827			
	16	0.682	0.808	0.897	0.950	0.962	0.946	0.931	0.909			
	15	0.698	0.847	0.965	1.051	1.074	1.055	1.024	0.987			
	14	0.695	0.867	1.015	1.131	1.166	1.140	1.102	1.047			
	13	0.685	0.872	1.035	1.175	1.230	1.209	1.159	1.089			
	12	0.678	0.875	1.053	1.209	1.278	1.245	1.194	1.112			
Axial	11	0.674	0.874	1.061	1.226	1.299	1.274	1.212	1.122			
Mesh	10	0.673	0.875	1.060	1.233	1.310	1.283	1.217	1.126			
	9	0.676	0.877	1.060	1.231	1.300	1.273	1.207	1.125			
	8	0.678	0.877	1.054	1.211	1.273	1.248	1.189	1.110			
	7	0.686	0.874	1.036	1.176	1.238	1.210	1.158	1.087			
	6	0.694	0.871	1.012	1.122	1.164	1.145	1.103	1.052			
	5	0.694	0.844	0.963	1.045	1.072	1.055	1.024	0.988			
	4	0.681	0.806	0.895	0.945	0.958	0.943	0.926	0.905			
	3	0.664	0.760	0.818	0.846	0.839	0.829	0.829	0.824			
	2	0.650	0.742	0.802	0.841	0.843	0.826	0.818	0.816			
	1	0.667	0.789	0.907	1.024	1.117	1.080	1.012	0.942			

The computer code allows the user to define multiple core regions with its own specified power generation levels as well as its own reactivity feedback intensity factors for the moderator and the fuel, as described by Obenchain [8]. Each of these core regions are independent from each other in terms of the hydrodynamic and heat transfer aspect, but coupled to all other regions defined in terms of the reactor kinetics and reactivity feedback effects. This is very important, given that PARET does not consider the spatial effects of the core in general for the computation. In fact, in PARET, the geometric configuration of the core, cylindrical or rectangular, is only used in the determination of the total heat transfer area and, consequently, the total heat flux. However, it is important to specify the appropriate equivalent diameter for the core region being defined (the "element") since this will determine the coolant flow velocity in that particular region.

Table 3.3. Relative power distribution for the outer fuel element, HEU, beginning-of-cycle

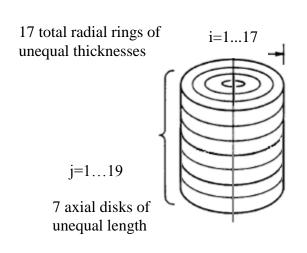
Power Level Distribution Outer Fuel Element: HEU Fuel											
					Radial N	Aesh					
	No.	9	10	11	12	13	14	15	16	17	
	19	1.141	1.177	1.195	1.173	1.020	0.781	0.586	0.467	0.354	
	18	0.908	0.847	0.800	0.733	0.624	0.509	0.416	0.352	0.291	
	17	0.935	0.875	0.826	0.755	0.642	0.529	0.438	0.375	0.314	
	16	1.087	1.029	0.978	0.901	0.778	0.655	0.553	0.478	0.409	
	15	1.244	1.177	1.124	1.048	0.923	0.805	0.712	0.654	0.592	
	14	1.383	1.319	1.263	1.179	1.053	0.943	0.859	0.807	0.756	
	13	1.504	1.429	1.369	1.286	1.161	1.047	0.966	0.917	0.866	
	12	1.590	1.508	1.444	1.364	1.235	1.128	1.055	1.011	0.964	
Axial	11	1.637	1.561	1.499	1.414	1.289	1.202	1.144	1.112	1.079	
Mesh	10	1.645	1.561	1.501	1.418	1.300	1.220	1.174	1.156	1.127	
	9	1.620	1.542	1.480	1.395	1.272	1.177	1.116	1.082	1.045	
	8	1.555	1.479	1.425	1.335	1.205	1.092	1.008	0.954	0.893	
	7	1.455	1.386	1.332	1.248	1.111	0.996	0.913	0.857	0.798	
	6	1.332	1.267	1.211	1.129	1.002	0.890	0.809	0.754	0.698	
	5	1.187	1.122	1.069	0.996	0.866	0.742	0.646	0.585	0.520	
	4	1.029	0.970	0.922	0.841	0.713	0.573	0.456	0.376	0.297	
	3	0.879	0.819	0.768	0.693	0.577	0.457	0.357	0.289	0.221	
	2	0.847	0.787	0.739	0.665	0.554	0.430	0.332	0.265	0.200	
	1	1.063	1.079	1.098	1.060	0.887	0.655	0.472	0.353	0.244	

Fig. 3.6 shows a "cylindrical" representation of HFIR that is to be converted into a "nested tube in slab geometry" option for the PARET computational model. The core is divided into 17 radial regions, each having its own power generation, coolant flow rate, hydraulic parameters, etc. and each represented by a single fuel plate plus its associated coolant channel. Each of the radial regions is further subdivided into 19 axial sections (one less than the maximum available in the PARET code). Each of these 17 radial regions is termed an "element" in the vocabulary of the PARET documentation [8, 9]. Materials Test Reactor-type of research reactors do, indeed, have cores composed of physically separate fuel elements. For HFIR, the designation is artificial and necessary in order to model the graded fuel thickness inside each fuel plate (see Fig. 3.2).

Table 3.5 shows the radial mesh spacing for the PARET model corresponding to Fig. 3.6. The mesh spacing differs from that shown in Fig. 3.4 and 3.5 because the central target region of the reactor is not modeled and, since PARET does not consider three dimensional spatial effects for the thermal conduction or neutronic aspects of the calculation, there is no need for separate models of the inner and outer element fuel plates. However, consistency in defining the two dimensional distribution of the core regions (horizontal core cross section) is important since the heat removal capacity will be calculated from this parameters. Note that the radial mesh spacing in Table 3.5 is the radial mesh for the "elements" (PARET terminology). There are no nodes between identified mesh points. The fuel plate model for each "element", i.e. the mesh inside a fuel plate channel – limited to 43 mesh points – is described subsequently.

Table 3.4. Relative power distribution for the outer fuel element, HEU, end-of-cycle

Power Level Distribution Outer Fuel Element: HEU Fuel												
	Radial Mesh											
	No.	9	10	11	12	13	14	15	16	17		
	19	1.001	1.090	1.171	1.235	1.168	1.028	0.892	0.802	0.713		
	18	0.843	0.848	0.839	0.810	0.761	0.727	0.707	0.696	0.677		
	17	0.843	0.849	0.843	0.811	0.764	0.754	0.752	0.751	0.738		
	16	0.928	0.955	0.958	0.929	0.884	0.868	0.859	0.843	0.806		
	15	1.007	1.047	1.059	1.044	0.998	0.975	0.950	0.916	0.853		
	14	1.070	1.130	1.153	1.136	1.084	1.053	1.012	0.956	0.864		
	13	1.114	1.184	1.219	1.209	1.151	1.112	1.054	0.977	0.856		
	12	1.136	1.226	1.271	1.258	1.199	1.154	1.082	0.989	0.850		
Axial	11	1.155	1.243	1.290	1.285	1.227	1.179	1.097	0.993	0.844		
Mesh	10	1.155	1.257	1.299	1.302	1.234	1.185	1.096	0.993	0.844		
	9	1.153	1.244	1.296	1.289	1.226	1.176	1.094	0.992	0.844		
	8	1.139	1.226	1.269	1.258	1.199	1.152	1.080	0.987	0.847		
	7	1.114	1.186	1.220	1.211	1.154	1.115	1.057	0.976	0.856		
	6	1.070	1.132	1.154	1.138	1.084	1.052	1.017	0.962	0.867		
	5	1.009	1.051	1.063	1.045	0.991	0.971	0.953	0.917	0.854		
	4	0.928	0.957	0.958	0.932	0.884	0.873	0.865	0.851	0.812		
	3	0.839	0.844	0.836	0.807	0.763	0.753	0.755	0.755	0.740		
	2	0.841	0.844	0.836	0.808	0.754	0.720	0.697	0.683	0.663		
	1	1.000	1.097	1.165	1.220	1.151	1.001	0.869	0.770	0.672		



Center cylinder plus 7 next rings represent the inner fuel element. Next 9 rings represent the outer fuel element. Ascending order from inner to outer for mesh nomenclature

Bottom axial disk is number 1 and increases in ascending order until disk number 19 at the top.

Fig. 3.6. PARET model spatial discretization.

The justification for not modeling the central target region or between-element gap is that, since thermal conduction is not incorporated in PARET, the amount of cooling provided by these two channels is neglected. Similarly, since PARET employs point kinetics, reactivity feedback given by these two channels cannot be modeled. It is noteworthy that an optimal void within the flux trap is the maximum reactivity worth accident that can be speculated to occur. Such scenario is not considered in the present study.

The area of flow of each horizontal cross section core region of the PARET model is equal to that of its corresponding core region of the HFIR reactor core. This is a necessary constraint in order to preserve coolant speed, which at the same time preserves Reynolds numbers and other flow regime indicators from the real conditions.

Table 3.5. Equivalent diameter for each core region in PARET HEU model

Table 3.5. Equivalent diameter for each core region in FARE1 field model										
P	PARET Cylindrical Model Equivalent Diameter Table									
Core Region	Equivalent Hydraulic	Radial mesh yielding equivalent area								
	Diameter (cm) ^a	to meshes in Fig. 3.4 and 3.5								
1		2.296								
2		1.313								
3		1.004								
4		1.576								
5		1.498								
6		1.346								
7		0.631								
8		0.690								
9	0.254	0.491								
10		0.656								
11		0.651								
12		1.264								
13		1.276								
14		1.237								
15		0.605								
16		0.577								
17		0.549								

^a Diameter computed as (4 * flow cross section area) / wetted perimeter. Parallel, involute plates result in same hydraulic diameter regardless of position along plate.

For the LEU neutronics model, the radial and axial discretization were unchanged from the one previously presented for the HEU fuel. The power density profile distributions for the LEU model at beginning-of-life are provided in Tables 3.6 and 3.7. End-of-life distributions for LEU are shown in Tables 3.8 and 3.9.

Table 3.6 Relative power distribution for the inner fuel element, LEU, beginning-of-cycle

	Power Level Distribution Inner Fuel Element										
				Rad	ial Mesh						
	No.	1	2	3	4	5	6	7	8		
	19	0.706	0.797	0.898	0.901	0.887	0.859	0.790	0.783		
	18	0.638	0.673	0.711	0.700	0.691	0.713	0.696	0.699		
	17	0.596	0.595	0.594	0.570	0.569	0.621	0.624	0.632		
	16	0.554	0.531	0.501	0.466	0.476	0.544	0.567	0.570		
	15	1.017	0.899	0.795	0.725	0.743	0.884	0.989	1.025		
	14	1.105	0.960	0.834	0.761	0.780	0.926	1.029	1.065		
	13	1.343	1.167	1.013	0.921	0.951	1.115	1.226	1.259		
	12	1.617	1.400	1.218	1.116	1.149	1.350	1.482	1.526		
	11	1.750	1.516	1.319	1.215	1.247	1.468	1.613	1.659		
Axial	10	1.748	1.521	1.329	1.220	1.253	1.470	1.616	1.664		
Mesh	9	1.735	1.504	1.307	1.201	1.235	1.450	1.595	1.641		
WICSH	8	1.574	1.368	1.191	1.091	1.119	1.317	1.446	1.484		
	7	1.296	1.121	0.971	0.888	0.912	1.068	1.172	1.209		
	6	1.070	0.923	0.796	0.724	0.741	0.877	0.970	0.997		
	5	0.988	0.871	0.761	0.689	0.703	0.828	0.919	0.954		
	4	0.537	0.509	0.475	0.441	0.445	0.505	0.523	0.535		
	3	0.569	0.566	0.557	0.530	0.528	0.577	0.581	0.585		
	2	0.611	0.638	0.673	0.649	0.643	0.663	0.650	0.656		
	1	0.674	0.751	0.841	0.836	0.823	0.793	0.721	0.727		

The regions identified by the radial mesh – the 17 "element" regions in Table 3.5 - are actually a set of independent, single channel models all of which are linked to a common point kinetics model (see Fig. 1.1). A representation of a plate model is shown in Fig. 3.7 from [8]. Note that the coolant channel is represented by a single zone.

Table 3.7. Relative power distribution for the outer fuel element, LEU, beginning-of-cycle

Power Level Distribution Outer Fuel Element										
		Radial Mesh								
	No.	9	10	11	12	13	14	15	16	17
	19	0.821	0.835	0.873	0.924	0.892	0.770	0.526	0.353	0.293
	18	0.733	0.725	0.703	0.691	0.660	0.587	0.441	0.328	0.282
	17	0.648	0.643	0.596	0.555	0.526	0.486	0.397	0.317	0.279
	16	0.584	0.566	0.511	0.464	0.438	0.417	0.363	0.314	0.281
	15	1.034	0.952	0.797	0.703	0.667	0.650	0.611	0.584	0.558
	14	1.060	0.994	0.835	0.744	0.712	0.703	0.677	0.672	0.646
	13	1.271	1.190	1.017	0.920	0.892	0.895	0.886	0.899	0.871
	12	1.535	1.440	1.239	1.137	1.121	1.161	1.223	1.310	1.292
	11	1.658	1.560	1.348	1.236	1.228	1.285	1.371	1.480	1.462
Axial	10	1.668	1.570	1.355	1.244	1.237	1.293	1.381	1.491	1.474
Mesh	9	1.648	1.551	1.339	1.230	1.217	1.273	1.352	1.457	1.442
MCSII	8	1.492	1.400	1.203	1.098	1.078	1.106	1.151	1.218	1.199
	7	1.205	1.132	0.966	0.870	0.834	0.820	0.784	0.767	0.732
	6	0.997	0.933	0.785	0.699	0.664	0.641	0.605	0.584	0.554
	5	0.960	0.887	0.743	0.650	0.608	0.566	0.507	0.468	0.438
	4	0.544	0.526	0.474	0.422	0.389	0.352	0.280	0.221	0.193
	3	0.598	0.591	0.544	0.498	0.458	0.397	0.286	0.195	0.161
	2	0.667	0.664	0.634	0.612	0.563	0.473	0.310	0.192	0.151
	1	0.747	0.763	0.785	0.813	0.763	0.617	0.369	0.209	0.157

One method of modeling HFIR would be to compute an average fuel thickness, create an "average" fuel plate – an equivalent involute plate with a constant fuel thickness along its length equal to the volumetric average of the real fuel distribution – and use that plate in each of the cylindrical regions representing the reactor core. For such a plate, PARET requires the input of a fuel half thickness and a plate half thickness. The computer code assumes symmetry about the center plane of the 'flat' plate; however, the HFIR fuel plate is not symmetric about the center plane. An average fuel thickness is calculated for each type of plate, and a new thickness is averaged between the two fuel elements weighted with the number of plates in each fuel element. A given fuel plate can be treated as two different half-plates, where each has a different fuel meat thickness. Then the correct temperature profile across the thickness of the plate is obtained (provided that the ratio of plate thickness to radius of curvature is <0.1).

Table 3.8. Relative power distribution for the inner fuel element, LEU, end-of-cycle

	Power Level Distribution Inner Fuel Element								
	Radial Mesh								
	No.	1	2	3	4	5	6	7	8
	19	0.495	0.650	0.835	0.881	0.877	0.816	0.713	0.725
	18	0.485	0.616	0.749	0.760	0.753	0.730	0.664	0.671
	17	0.472	0.578	0.659	0.642	0.638	0.656	0.616	0.627
	16	0.460	0.531	0.562	0.529	0.533	0.578	0.564	0.575
	15	0.858	0.926	0.888	0.804	0.813	0.936	0.982	1.026
	14	0.888	0.944	0.885	0.794	0.807	0.926	0.983	1.045
	13	0.977	1.083	1.037	0.935	0.944	1.067	1.114	1.186
	12	1.050	1.229	1.217	1.096	1.100	1.231	1.265	1.360
	11	1.077	1.293	1.302	1.175	1.179	1.310	1.344	1.447
Axial	10	1.075	1.295	1.307	1.181	1.184	1.320	1.357	1.454
Mesh	9	1.075	1.295	1.299	1.171	1.177	1.308	1.343	1.445
WICSH	8	1.048	1.224	1.210	1.091	1.098	1.228	1.263	1.357
	7	0.968	1.071	1.028	0.925	0.933	1.055	1.103	1.175
	6	0.882	0.936	0.871	0.778	0.789	0.910	0.966	1.023
	5	0.858	0.918	0.871	0.782	0.795	0.907	0.960	1.005
	4	0.457	0.528	0.551	0.520	0.521	0.563	0.552	0.564
	3	0.468	0.571	0.639	0.623	0.621	0.643	0.604	0.612
	2	0.477	0.608	0.725	0.733	0.730	0.720	0.655	0.658
	1	0.489	0.637	0.807	0.849	0.850	0.798	0.696	0.700

For this work though, the cylindrical-core-geometry option was not chosen. If the "nested tube" option in PARET is selected rather than the "cylindrical" option, then the variable fuel meat transverse width can be modeled by the use of multiple channels. The "nested tube" option requires rectangular geometry description for the reactor core. However, in PARET, the geometric configuration of the core, cylindrical or rectangular, is only used in the determination of the total heat transfer area and, consequently, the total heat flux. To accommodate the rectangular geometry requirement, the "along-the-plate" fuel thickness variation in the HFIR fuel plates can be modeled by creating separate plate models for each of the PARET "elements" with the fuel thickness in a given plate model corresponding to the radial location along the real, HFIR involute plate. Interactions between channels are ignored. Each portion of the involute plate can be modeled as a flat plate with little error because when the tube thickness to radius ratio is less than 0.1 as the temperature profile across the thickness of the tube approaches the flat plate solution.

Table 3.9. Relative power distribution for the outer fuel element, LEU, end-of-cycle

Power Level Distribution Outer Fuel Element										
	Radial Mesh									
	No.	9	10	11	12	13	14	15	16	17
	19	0.749	0.774	0.872	0.996	1.040	0.978	0.740	0.541	0.463
	18	0.694	0.699	0.737	0.778	0.797	0.777	0.649	0.516	0.449
	17	0.638	0.633	0.632	0.628	0.633	0.642	0.585	0.494	0.441
	16	0.581	0.567	0.543	0.514	0.517	0.545	0.529	0.478	0.437
	15	1.037	0.956	0.840	0.761	0.754	0.813	0.871	0.876	0.851
	14	1.052	0.957	0.841	0.772	0.769	0.827	0.905	0.922	0.895
	13	1.199	1.087	0.980	0.910	0.909	0.977	1.047	1.025	0.983
	12	1.379	1.245	1.139	1.063	1.065	1.142	1.200	1.127	1.071
	11	1.463	1.318	1.215	1.137	1.139	1.218	1.272	1.178	1.115
Axial	10	1.473	1.323	1.220	1.143	1.141	1.224	1.279	1.180	1.117
Mesh	9	1.458	1.318	1.212	1.133	1.134	1.215	1.270	1.172	1.112
Wiesii	8	1.374	1.239	1.132	1.058	1.059	1.135	1.191	1.119	1.065
	7	1.187	1.078	0.966	0.902	0.903	0.969	1.031	1.004	0.965
	6	1.040	0.947	0.830	0.759	0.754	0.808	0.878	0.890	0.861
	5	1.017	0.935	0.821	0.738	0.725	0.767	0.819	0.814	0.784
	4	0.572	0.553	0.524	0.493	0.491	0.507	0.482	0.425	0.385
	3	0.619	0.612	0.610	0.603	0.596	0.593	0.516	0.420	0.372
	2	0.675	0.671	0.710	0.741	0.747	0.709	0.564	0.425	0.370
	1	0.725	0.742	0.839	0.945	0.976	0.889	0.641	0.448	0.378

Peak fuel temperature should be more accurately calculated with the "nested tube" model than with the "cylindrical" model. However the requirement that the PARET fuel plate model be symmetrical when the HFIR fuel plate is not symmetrical coupled with the thinness of the HFIR plate could render either representation as being equally acceptable. The asymmetry of the HFIR fuel plates can be treated as two different half-plates.

Fig. 3.8 illustrates the conversion of a HFIR involute plate to the "nested tube" model. The approximation represented in Fig. 3.8 is appropriate when the plate thickness to segment-length ratio is much less than one. That is, heat conduction and temperature variation through the plate is much greater than the variation between the segments that lie along the plate as shown in Fig. 3.8 (segments divided by bars). Note that these segment lengths are directly related to radial distance from the center of the core as well as the absolute difference between segment boundaries, i.e. in an involute plate, equal radial intervals generate different along-the-plate segment lengths.

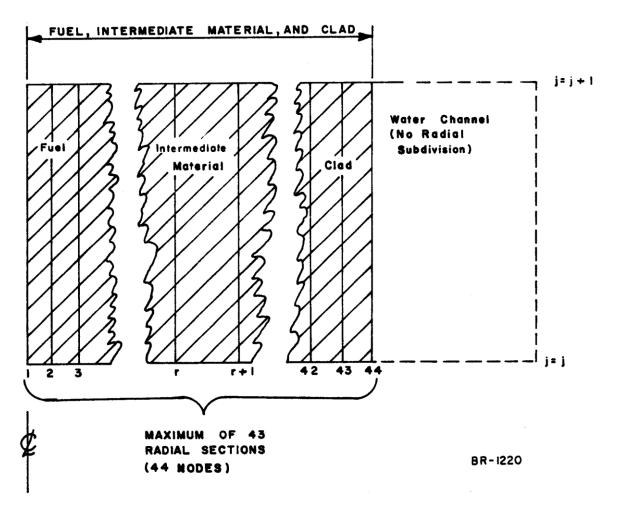


Fig. 3.7. Plate radial subsectioning used in thermal hydraulic calculation in PARET (same plate in each radial element in reactor model).

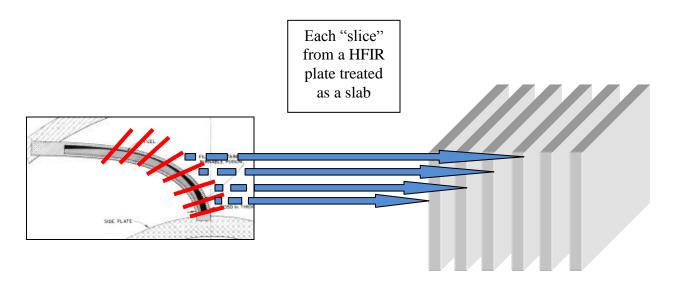


Fig. 3.8. Conversion of HFIR involute plate to "nested tube" model.

A fuel "meat" thickness must be identified for each of the 17 plate models corresponding to the 17 slab elements that have been partitioned from an inner plate (8 regions) and an outer plate (9 regions). Figure 3.9 shows the fuel meat thickness variation in inner fuel plates for both HEU and LEU fuels.

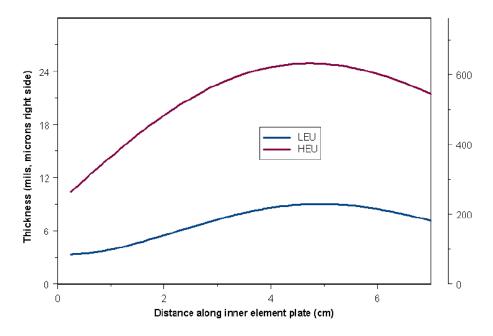


Fig. 3.9. Fuel thicknesses inside plates for inner element.

Fig. 3.10 shows the fuel meat thickness variation inside the outer element fuel plates. The radial mesh spacing in Table 3.5 identifies the location along the plates at which the fuel thicknesses are selected for the 17 elements in the "nested tube" model. The width of the slabs is the quotient of the area of the zone divided by the plate thickness. The equivalent hydraulic diameter is the same as in Table 3.5. Derived values are in Table 3.10.

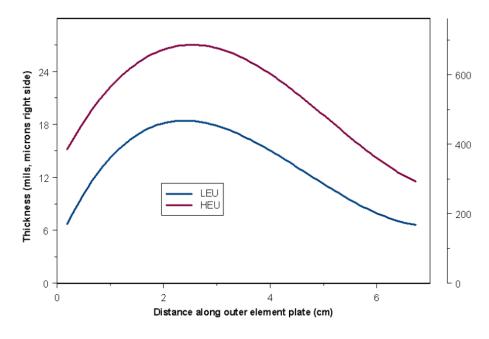


Fig. 3.10. Fuel thicknesses inside plates for outer fuel elements.

Table 3.10.	Nested	tube	model	dima	encione
Table 3.10.	resteu	Lune	mouei	umi	EHDIVHS

Core	Plate Equiv. Hyd.	Slab Dimer	nsions (cm)	Plate fuel thickness (microns)		
Region	Diam. (cm) ^a	Thickness	Length	HEU	LEU	
1		2.296	7.21	259	127	
2		1.313	18.55	295	127	
3		1.004	25.83	394	188	
4		1.576	35.87	521	257	
5		1.498	41.93	620	300	
6		1.346	51.36	625	310	
7		0.631	58.53	546	277	
8		0.690	67.17	472	213	
9	0.254	0.491	70.51	389	229	
10		0.656	75.36	396	251	
11		0.651	78.43	429	356	
12		1.264	84.48	584	457	
13		1.276	88.60	688	457	
14		1.237	96.42	648	401	
15		0.605	102.45	526	259	
16		0.577	110.14	373	170	
17		0.549	113.86	292	135	

^a See Table 3.5

Finally, it is also necessary to discretize the fuel slab and its cladding such that heat transfer calculations can be appropriately done. Figure 3.11 shows the adopted discretization scheme.

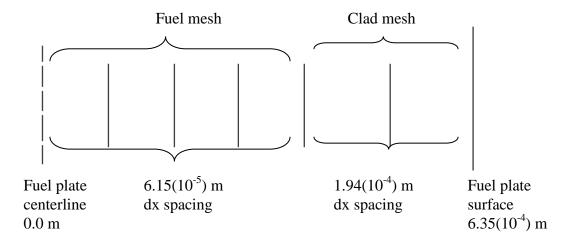


Fig. 3.11. Fuel plate discretization.

PARET requires as input the total volume of fuel in the reactor as well as the total area of flow. The first calculation is relatively simple, based on the known mass of fuel per plate, the total number of plates and the density of the fuel. The second calculation requires a more heuristic approach. It is known that the channel thickness is the same as the fuel plate thickness, then the area of flow must be half of the total area available between the two fuel elements. Table 3.11 summarizes the geometric properties of the fuel and the core.

Table 3.11. Core and fuel plate geometric data

HFIR fuel plate geometric data						
Component	HEU	LEU				
Total fuel 'meat' volume in core	0.00980 m^3	0.00534 m^3				
Nominal fuel half thickness	0.2460 mm	0.1341 mm				
Nominal "intermediate" filler half thickness	0.3810 mm	0.3810 mm				
Plate half thickness	0.6350 mm	0.6350 mm				
Fuel – clad gap	0.0 m	0.0 m				
Active fuel length	0.508 m	0.508 m				
Center of fuel – center of coolant channel distance	1.27 cm	1.27 cm				
Total area of flow	0.0498 m^2	0.0498 m^2				
Fraction of fission heat deposited	0.975	0.975				
in the fuel assembly	0.973	0.773				

3.2 Core Materials Description

The reactor core of the HFIR operates with pressurized light water and is fueled with highly enriched uranium clad in aluminum metal and possesses a variety of control systems for criticality. It is important to define precisely the materials which make up the core in order to accurately predict property changes under transients, however, the HFIR model requires only the properties of the basic components of the core, namely, the fuel, the cladding, and the coolant. Given that PARET targets the analysis of thermal transients as part as the safety analysis, the thermal properties are defined only for the materials mentioned.

Clearly, the thermal properties of materials are different when they are at different temperatures. For this reason, PARET utilizes a system that allows this temperature variation to be taken into account. It is assumed that the property can be represented by a polynomial function with exponents ranging from -1 to 2. Namely, the properties can be established by declaring the coefficients alpha and beta in two functions. The alpha_n, (n = 1,2, ..., 5) are the thermal conductivity coefficients of the material for an

equation of the form $k_{n+1/2}^m = \alpha_1 T^2 + \alpha_2 T + \alpha_3 + \frac{\alpha_4}{T}$. The beta_n (n = 1, 2,..., 5) are the volumetric heat capacity coefficients of the material for an equation of the form

$$g_{n+1/2}^{m} = \beta_1 T^2 + \beta_2 T + \beta_3 + \frac{\beta_4}{T}.$$

It can be easily observed from the mathematical relations above that the conductive heat transfer coefficient and the volumetric heat capacity variation can be easily established for the specified operating conditions. Figure 3.12 shows the dependence of the conductive heat transfer coefficient on the temperature for various levels of enrichment of U-Al fuels as reported by Ref. 21.

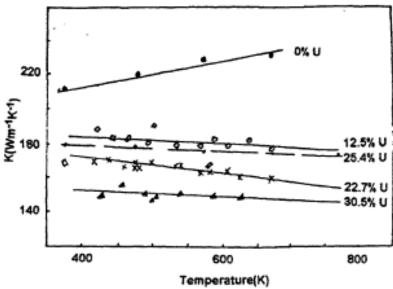


Fig. 3.12. Thermal conductivity variation as a function of temperature for typical U-Al fuel for various enrichments.

It can be inferred from the graph above that the thermal conductivity changes linearly with temperature, however the value almost seems constant over such large temperature range, especially for the high enrichment case, as it is the case with HFIR. Thus, it seems reasonable to assume a constant k coefficient. Similarly, it can be shown that the volumetric heat capacity does not change much over large temperatures, therefore constant thermal properties for the fuel plates. HFIR, though, having fuel that is a mixture of U3O8 and Al has somewhat lower thermal conductivity than shown in Fig. 3.12. Table 3.12 summarizes the data obtained from Refs. 21 and 30 and utilized in PARET for both the fuel and the cladding.

Table 3.12. Fuel and clad material thermal property coefficients

	HFIR fuel thermal properties						
Coefficient	HEU Value	LEU Value (U-10Mo)					
$\alpha_1, \alpha_2, \alpha_4, \alpha_5$ (T in Kelvin)	All 0.0	0.0, 0.0240, 0.0, 0.0					
α_3	174.5 W/m °K [Ref. 30a values are 132.8 inner element; 110.0 outer element]	11.36					
$\beta_1, \beta_2, \beta_4, \beta_5$	All 0.0	2.82, -578, 0, 0					
β_3	$6.81(10^5) \text{ J/m}^{3 \text{ o}} \text{K}$	$19.4(10^5) \text{ J/m}^3\text{K}$					

HFIR clad thermal properties

Coefficient	Value
$\alpha_1, \alpha_2, \alpha_4, \alpha_5$	0.0
α_3	186.9 W/mK
$\beta_1, \beta_2, \beta_4, \beta_5$	0.0
$ \beta_3$	$7.64(10^5) \text{ J/m}^3 \text{K}$
thermal expansion coefficient	$2.43(10^{-5}) \text{ cm/(cm}^{\circ}\text{C})$

For coolant thermal properties, PARET utilizes a library that includes more thermal properties than those specified for the fuel or the clad. The code only requires the input of a reference coolant density, temperature and pressure as a starting point of the transient.

3.3 Neutronic Parameters

The model requires the input of certain neutronic parameters of the reactor core. Since PARET is a reactor kinetics code, the amount of information necessary to be input is much less than that if the code had been a neutron diffusion or transport code, in which case cross sections would have been necessary, among other parameters. Table 3.13 contains the neutronic parameters assumed for HEU fuel. The delayed neutron fraction data are from ENDF/B-VI via the methodology described in Appendix A. The values for the parameters for low enriched uranium (LEU) fuel were also derived via the methodology described in Appendix A. ENDF/B-VII data are reported for LEU in Table 3.14.

Table 3.13. Reactor kinetics parameters for HEU fuel

Table 3.13. Reactor kinetics parameters for the cruci							
P	Parameter						
No. of delayed gro	6						
	$\beta_1, \lambda_1 (s^{-1})$	0.031976, 0.012495					
	$\beta_2, \lambda_2 (s^{-1})$	0.166406, 0.031833					
relative delayed neutron	$\beta_3, \lambda_3 (s^{-1})$	0.161350, 0.109416					
fraction, decay constant (from Appendix A)	$\beta_4, \lambda_4 (s^{-1})$	0.459789, 0.317095					
Appendix A)	$\beta_5, \lambda_5 (s^{-1})$	0.133571, 1.354406					
	$\beta_6, \lambda_6 (s^{-1})$	0.046908, 8.639475					
Effective delayed neutron fract	0.00762, 0.00752						
Prompt neutron lifetime Λ [B	52, 94						
Fuel Doppler t	emperature coefficient	$-2.41(10^{-6}), -2.46(10^{-6})$					
[BOL, EOL; c	orrected from Ref. 1†]	(δk/k)/°C					
Coolant tammanatuma faa	dheelr coefficient (from Def. 10)	-1.71(10 ⁻⁴) (δk/k)//°C					
Coolant temperature fee	Coolant temperature feedback coefficient (from Ref. 19)						
Coolant void feedback	-0.243 \$/% void,						
[BOL, E	-0.179 \$/% void						
Coolant void feedback	-0.101 \$/% void,						
[BOL, E	-0.074 \$/% void						

Table 3.14. Reactor kinetics parameters for LEU fuel

P	Value				
No. of delayed gro	6				
	$\beta_1, \lambda_1 (s^{-1})$	0.031223, 0.012502			
	$\beta_2, \lambda_2(s^{-1})$	0.164661, 0.031795			
relative delayed neutron	$\beta_3, \lambda_3 (s^{-1})$	0.160244, 0.109708			
fraction, decay constant (BOL, from Appendix A)	$\beta_4, \lambda_4 (s^{-1})$	0.459758, 0.318138			
(BOL, Holli Appelluix A)	$\beta_5, \lambda_5 (s^{-1})$	0.137204, 1.353875			
	$\beta_6, \lambda_6(s^{-1})$	0.046910, 8.691927			
Effective delayed neutron fract	Effective delayed neutron fraction β_{eff} [BOL, EOL; from Appendix A]				
Prompt neutron lifetime Λ [E	Prompt neutron lifetime Λ [BOL, EOL; (10^{-6}) s, from Appendix A]				
Fuel Doppler	temperature coefficient	$-2.42(10^{-5}), -2.38(10^{-5})$			
[BOL, EOL;	corrected from Ref. 1]	$(\delta k/k)/^{\circ}C$			
Coolent temperature feedba	ck coefficient (from G. Ilas, ORNL)	$-0.78(10^{-4}) (\delta k/k)/^{\circ}C$			
Coorant temperature reedoa	$(at T = 27 {}^{\circ}C)$				
Coolant void feedback	-0.208 \$/% void,				
[BOL, E	-0.189 \$/% void				
Coolant void feedback	-0.105 \$/% void,				
[BOL, E	OL; from Ref. 1]	-0.095 \$/% void			

 $[\]dagger$ R. J. Ellis, ORNL, reported that the %dk/k in Ref. 1 should be dk/k. The heu_ref case (with fuel temp = 300K; all other temps = 299.8K) -> k=0.99909 at BOC; k=1.00879 at EOC (controlled). The heu_ref case (with fuel temp = 500K; all other temps = 299.8K) -> k=0.99861 at BOC; k=1.00829 at EOC (controlled). This gives the fuel temp (Doppler) coefficients for HEU of: at BOC: -4.811E-4 dk per 200°C = -2.41E-6 dk/k/°C (or -1.34E-6 dk/k/°F) and at EOC: -4.916E-4 dk per 200°C = -2.46E-6 dk/k/°C (or -1.37E-6 dk/k/°F). Though Doppler and moderator temperature coefficients are negative for HFIR, for PARET input, these are entered as positive values.

3.4 Operating Parameters

Various parameters of operation are needed for modeling transients for the core of the HFIR. Table 3.15 includes steady state reactor operation data, however, most of these parameters will change depending on the analysis of each accident scenario being performed. Note that for equivalent flux performance at experimental facilities, the LEU fuel must operate at 100 MW whereas the HEU fuel operates at 85 MW.

Table 3.15. Assumed operational parameters

Parameter	Nominal Operating Data
Power	85 MW (HEU); 100 MW (LEU)
Inlet Pressure	3.227 MPa
Outlet Pressure	2.482 MPa
Temperature	49 °C
Reference Coolant Density	993.0 kg/m^3
Coolant primary mass flux	$2.088(10^4) \text{ kg/cm}^2\text{s}$
Core average heat flux	$2.0808(10^6) \text{ W/m}^2 \text{ (HEU)}; 2.448(10^6) \text{ W/m}^2 \text{ (LEU)}$

3.5 Control Systems

The control system of the HFIR is composed of the control cylinder and the safety plates. The control cylinder is a movable cylinder which is located between the beryllium reflector and the outer fuel element and is inserted from the bottom of the reactor. The safety plates consist of four plates that are quadrants of a cylinder of larger inner diameter than the control cylinder and are inserted in the core from the top of the reactor. Each safety plate is independent of the other plates, and only one plate is necessary to scram the reactor at any fuel cycle stage. Since PARET does not consider these three dimensional effects of the control systems, it is sufficient to establish rod worth at certain locations along the core. The system also requires the input of the nominal control rod insertion speed and the delayed time from reactor scram to start of insertion.

In addition, PARET was constructed such that the user can specify external reactivity insertions (i.e. control rod drop) or actually scram the reactor as a consequence of certain limit being exceeded (overpower, underflow of coolant). Furthermore, the user is also able to specify hydrodynamic changes in order to explore the reactivity feedback effect of changes as such primary coolant pressure changes and mass flux changes. Notice in this case, the control rod worth is specified as a function of length inserted. In this case, PARET assumes linearity between the reactivity inserted as a function of time between two points. Then, a non linear relation may be input with the use of more than one pair of data points. Tables 3.16 and 3.17 provide data regarding operation of the control system.

Table 3.16. Control systems data for HEU model

Parameter	Value
Safety plate insertion rate	1.524 m/s
Time delay of rod drop	0.01 s
Overpower trip	HEU 89.0 MW; LEU 105 MW
Low flow trip	76.9 % of nominal full power flow
Safety plate worth	-\$15.00
Length of plate where this worth is reached	0.508 m

Table 3.17. Control systems reactivity worth for HEU fuel

Control/safety p	late position	Differential reactivity worth (combined control and safety plates; \$/inch)				
(inches withdrawn)	(cm from top)	$\mathbf{HEU^a}$	LEU ^b			
16	27.94	3.17	2.44			
17	25.4	3.00	-			
18	22.86	2.79	2.76			
19	20.32	2.57	-			
20	17.78	2.31	2.44			
21	15.24	2.06	-			
22	12.7	1.80	1.78			
23	10.16	1.50	-			
24	7.62	1.20	1.06			
25	5.08	0.91	-			
26	2.54	0.66	0.65			
27	0	0.40	-			

^a Ref. 26a.

Since control/safety element differential worth for LEU fuel is essentially the same as HEU fuel, the HEU worth values were used in LEU studies. The difference in worth at 16 inches withdrawn is likely due to differing critical configurations at beginning-of-life for the two fuels.

3.6 Thermal Hydraulic Parameters

PARET requires the input of certain hydrodynamic and heat-transfer data to the model; some related to the geometry of the reactor core. Table 3.18 shows the geometric data and assumptions input to PARET calculations reported subsequently.

^b Ref. 1a.

Table 3.18. Thermal hydraulic data and correlations used

Tuble Citor Thermal by arabine and and correlations about							
Parameter	Value						
Inlet non-fueled length	0.0508 m						
Outlet non-fueled length	0.0508 m						
Inlet to plenum area ratio	0.5						
Outlet to plenum area ratio	0.5						
Length inlet plenum	>1.0 m						
Length outlet plenum	>1.0 m						
Single phase correlation	Sieder Tate						
Two phase correlation	McAdams						
Transient two phase scheme	Original Model						
DNB and flow stability correlation	Original DNB						
Single phase heat transfer subroutine	Original						
Average core heat flux	HEU 4.035(10 ⁵) W/m ²						
(used by certain correlations only)	LEU 4.747(10 ⁵) W/m ²						

3.7 Channel Dependent Flow Rates

In [9], the author notes that the output of the PLTEMP [29] computer program is needed to establish relative flow rates among the channels of the nested tube model. For HFIR, the HFIR Steady State Heat Transfer Code (HSSHTC) [30] provides the flow rate data (as well as other parameters) that correspond to the data generated by PLTEMP for various reactors studied by the RERTR program.

The involute plate design for HFIR was chosen, in part, to assure that the coolant flow rate through the core would not be position dependent – the coolant channel-to-fuel plate area ratio is constant throughout the core. If one is only interested in transient response at beginning-of-life, the detailed core representation discussed in this section is not needed. Only the hot channel need be identified from the neutronics calculation and then only that single channel modeled. A second, "average" channel is needed for reactivity feedback from core heatup. However, given that the power distribution changes over time during a fuel cycle and given that phenomena such as oxide growth, radiation swelling, thermal-induced bowing of fuel plates, fuel clad interactions and other physical phenomena occur, then if one wishes to calculate the transient response at various times during the fuel cycle, the multichannel representation developed in this section is useful. Unlike beginning-of-life, due to the various factors, it may not be obvious which of the channels will be limiting in terms of peak temperature. Having a multichannel representation allows one to couple the output of timedependent neutronics calculations and the output from plate modeling codes such as PLTEMP and HSSHTC directly to PARET with a minimum of effort from the user. Still, of course, it will be results from a single channel – the one with the highest coolant and/or fuel temperature - that will ultimately be of interest to the user.

Experience with the HSSHTC program has shown that flow rates along an involute plate in HFIR can vary by as much as 10% at end-of-cycle. This phenomena has not been included in the analyses that will be reported in the next section but could be included in future analyses with a minimum of effort.

4.0 RESULTS OF CALCULATIONS

Transients were analyzed for each HEU and LEU fuel type, and the results are plotted in the same graph, such that a comparison can be easily done. In some cases, the transients analyzed were compared to published data from the most recent Updated Safety Analysis Report (USAR) of the HFIR to further benchmark the code. In the analysis of the safety systems of the HFIR, the decrease in primary flow rate transient was studied. There are multiple scenarios within each category. The initial conditions prescribed for each scenario are detailed in the Updated Safety Analysis Report (USAR) of the HFIR [27, 28].

This family of transients refers to the sudden reduction or loss of cooling capacity in the reactor core. Various transients related to decrease in primary flow are documented in the USAR section 15.3.3 and include considerations of a loss of off-site power, primary coolant pump coast down, primary coolant pump shaft seizure and blockages of fuel element coolant channels. For this work, only the primary coolant pump shaft seizure was considered. It is defined as follows:

A mechanical failure within the primary pumps could cause a pump shaft to shear or seize. The transient resulting from this failure is similar to a single pump coastdown except that the reduction in flow is immediate. Also, a mechanical pump failure prevents operation of the associated pony motor. Primary pump seizures are virtually unknown in the power reactor industry, so this event is assumed to be an infrequent event.

[27a, p. 15.3.3-2]

Because primary pump seizure represents the most severe case of flow reduction, it was chosen for study. Table 4.1 summarizes the parameters used in this problem. Additional details regarding the description of the transient are provided subsequently.

Table 4.1. Primary coolant pump seizure initial and boundary conditions

HFIR Primary Coolant Pump Seizure				
Parameter	Value			
Transient time	100.0 s			
Reactivity insertion	None from control system; no SCRAM			
Boundary conditions	\$0.0 at 0.0 s \$0.0 at 100 s			
Flow rate (kg/m²s)	2.044(10 ⁴) from 0.0 s – 10.0 s 1.589(10 ⁴) from10.0 s – 100.0 s			
Time step (s)	$10^{-3} (0.0 \text{ s} - 9.0 \text{ s})$ $10^{-4} (9.0 \text{ s} - 29.0 \text{ s})$ $10^{-3} (29.0 \text{ s} - 100.0 \text{ s})$			

A primary pump seizure is assumed to result in an immediate drop in flow, resulting in a lack of heat removal from the core until a reactor scram, if required, can occur. This event results in a decrease in margin to critical heat flux. Possible mitigating actions for a primary pump seizure include automatic closure of the failed pump outlet check valve and the reactor scram. Letdown block valve closure is not important because a depressurization does not occur during this event. Failure of the check valve to close after the pump seizes results in some backflow of coolant through the pump body. This failure reduces the flow available to the core from the remaining two pumps. The frequency of the pump seizure/check valve failure event is approximately 1×10^{-6} per year. Nonetheless, the results of this event are included in the discussion of the bounding infrequent event. Though a SCRAM function would be initiated in such an event, the results that are presented ... show that this mitigating function is not needed because the process variables do not exceed the limiting safety system setting (LSSS) values, even if the pump outlet check valve also fails. Thus, a reactor scram failure does not need to be considered and (is not included in the model of this accident.)

To analyze the pump seizure event, the following assumptions are made:

- 1. The speed of the primary coolant pump is assumed to change from full speed to zero speed within 0.01 s to model an almost instantaneous pump seizure event.
- 2. The effects of reactivity feedback (with conservative uncertainties applied) are included in the computations.
- 3. No credit is taken for any control system functions (electric motor servo or fast air motor). The control cylinder is assumed to be stationary throughout the event.
- 4. The normal secondary actions that would follow a reactor scram are assumed to occur during the event. However, prior to reactor scram, the secondary system temperature control valve is not allowed to open beyond the steady-state position that it was at prior to the initiating event.
- 5. The check valve downstream of the seized primary coolant pump may be assumed to fail to close.
- 6. The initial conditions considered in these analyses are [27a, p. 15.3.3-21, -22]:
 - Reactor power = HEU 87.6 MW, LEU 103 MW
 - Reactor inlet temperature = 126.2°F (52.33°C)
 - Reactor inlet pressure = 406.0 psig (420.7 psia [2.9Mpa])
 - Secondary basin temperature = 88.2°F
 - Primary flow rate = 15,840 gpm
 - Letdown flow rate = ~ 120 gpm

Figs. 4.1 through 4.10 depict the power, reactivity and temperature of the fuel and the coolant for the transients. Corresponding graphs from the HFIR USAR [27] are presented for comparison. Note that the operating power of the reactor for LEU fuel is greater than that for HEU fuel.

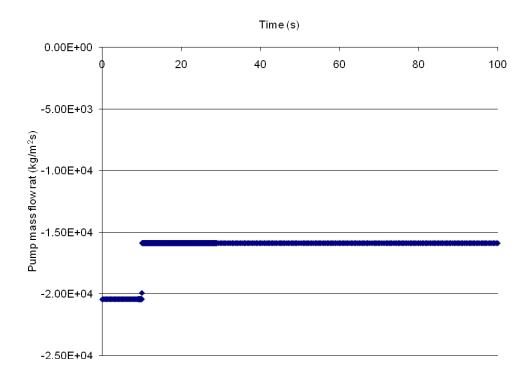


Fig. 4.1. Mass flux functions for transient in discussion. Note negative values of mass flux, as they indicate the downward direction of flow that exists in the HFIR core.

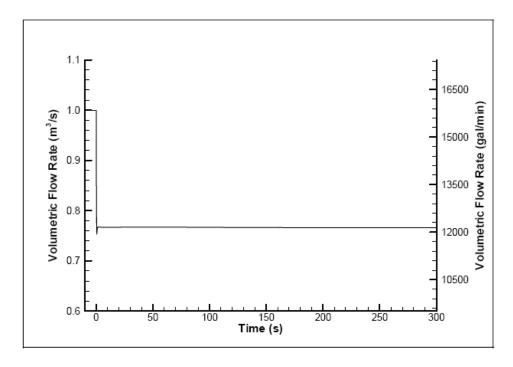


Fig. 4.2. Volumetric flow rate for this transient as found in the most recent version of the USAR of the HFIR. Both initial and final values of the flow are equivalent to the ones shown in the previous graph, only expressed in different parameters.

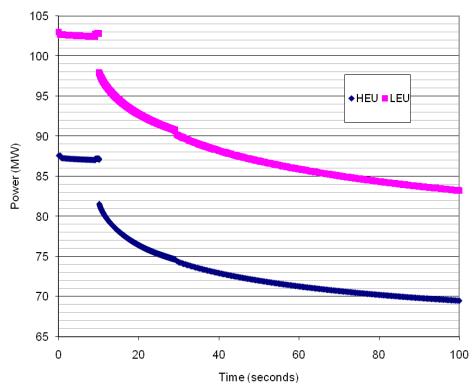


Fig. 4.3. Power profile for primary pump seizure at beginning-of-life.

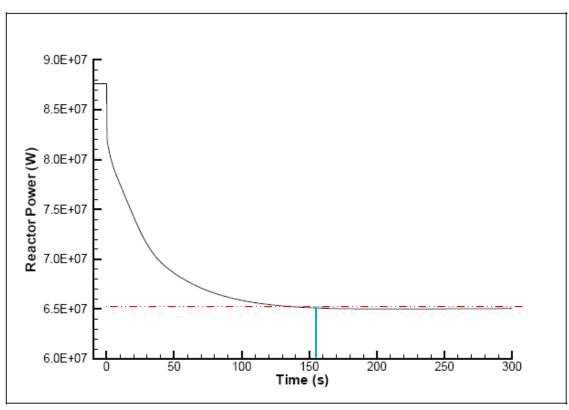


Fig. 4.4. Power profile for HEU transient as found in the USAR.

The post transient power level at 100 seconds from the current calculation is approximately 5% greater than the value reported in the HFIR safety analysis report. The feature of consequence, though, is that the time dependence of the transient for LEU fuel is very similar to that of HEU fuel but with slightly less percentage reduction in power from the pre-transient reactor condition.

Fig. 4.5 shows the reactivity change due to the transient as a function of time (data plotted are for the hot channel in the HEU and LEU cases, respectfully). Though small, the reactivity change due to the transient is greater for the HEU fuel than for the LEU fuel. The phenomenon is consistent with the percentage decrease in power for the HEU fuel being slightly greater than that for the LEU fuel.

During initial calculations, two anomalies were visible in the results shown in Fig. 4.5. During the time frame of 0-10 seconds, the PARET code was calculating some small, but negative, reactivity input, perhaps indicating inconsistencies among input parameters. Second, at the point at which the time step is changed from 1 millisecond to 0.1 millisecond, there was a slight increase in negative reactivity. During the course of this work, both anomalies were corrected and a new version of PARET (7.4) was issued by A. Olson of Argonne National Laboratory. Fig. 4.5 was generated with version 7.4 of PARET.

Fig. 4.6 provides temperature profile as a function of time for several locations in the core. Note that the peak temperature in the *fuel* is 396K. Figure 4.7 from the HFIR Safety Analysis Report shows the peak clad "wall" temperature as being 487K. The significant disparity between these two values prompted further investigation.

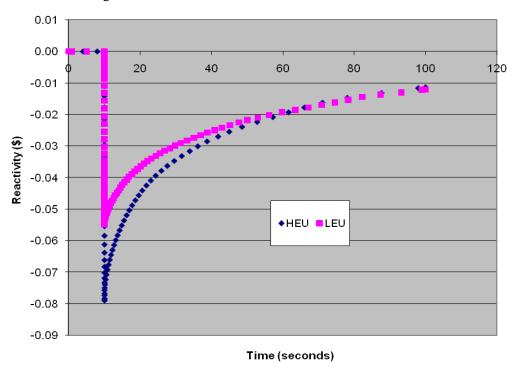


Fig. 4.5. Reactivity profile of the reduction in primary flow transient as calculated with PARET

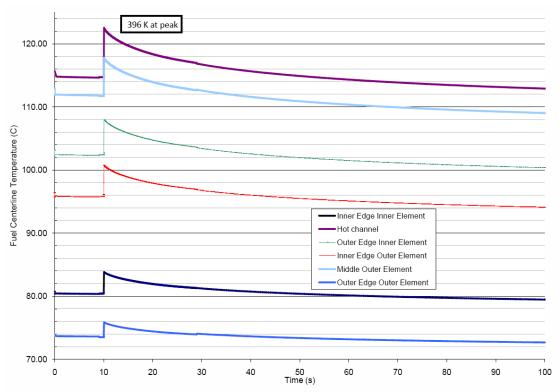


Fig. 4.6. Fuel temperature profile for several core regions for HEU for pump seizure transient.

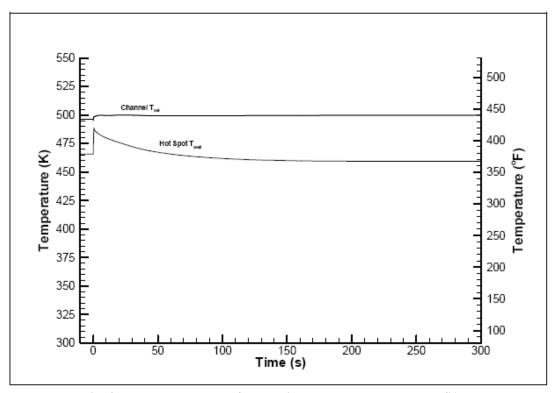


Fig. 4.7. Fuel temperature for transient as reproduced by the USAR.

Reference 24 provides information as to the assumptions that were the basis of the calculation shown in Fig. 4.7. Whereas the current work is based on the nominal power density from reactor physics calculations, the calculation reported in Fig. 4.7 included the following assumptions not made in the current calculation. The following are assumed to occur simultaneously:

- (1) uncertainty in the calculated power distribution (value for a given, calculated, local power density) -10%,
- (2) allowance for power tilt associated with experiments loaded to the reactor -9%,
- (3) tolerance on fuel loading in plates accepted from manufacturer 10% (current value is 12%),
- (4) fuel plate length uncertainty -2.5%,
- (5) non-bond of fuel meat to filler or clad -8%,
- (6) maximum allowable peak segregation of U_3O_8 from Al in fuel meat 27%, and
- (7) thermal conductivity of segregated fuel 13.0 W/m °K.

In the current, HFIR SAR methodology, these uncertainty values are assumed to be multiplicative and yield a multiplier factor of 1.85 to the local power density at the base of the fuel plate in the hot channel. A more reasonable assumption would be to assume that these individual effects are independent. If so, they can be added in quadratures, reducing the multiplier factor to about 1.13.

The PARET HEU model was modified to include the reduced thermal conductivity of the fuel and the multiplier factor to account for uncertainties. The calculated *clad* surface temperature at the hot spot was 408 K, 20% less than the value shown in Fig. 4.7 but certainly in better agreement than before the uncertainties and the SAR thermal conductivity were applied. The fuel hot spot temperature for these conditions was 485 K.

Fuel temperatures at selected locations for LEU fuel in a pump seizure transient *without any multiplicative factor* are shown in Fig. 4.8. Note that the peak temperature in the LEU fuel is 41K higher than for the HEU fuel that is shown in Fig. 4.6.

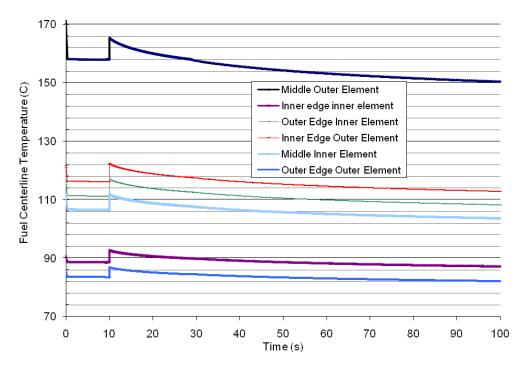


Fig. 4.8. Fuel temperature profile for several core regions for LEU for transient.

The PARET LEU model was then modified to include the multiplier factor for local power density that accounts for HEU fuel uncertainties. The uncertainty values for LEU/Mo fuel are unknown because no manufacturing experience exists for this fuel. No change was made to the thermal conductivity of the LEU fuel as segregation of the uranium from the molybdenum was not considered credible. The calculated *clad* surface temperature at the hot spot was 420 K, only 3% higher than for HEU fuel. The coolant temperature at the hot spot location (exit of hot channel) was 367 K (94 C). The fuel hot spot temperature for these conditions was 468 K, slightly lower than for HEU. The higher HEU value for hot spot conditions while lower for nominal conditions is due to the higher local power density at the exit of the HEU fuel as compared to the LEU fuel and the hot spot power density for each fuel being the same percentage increase over nominal not the same absolute increase.

5.0. CONCLUSIONS

The reduction in primary coolant flow transient that was analyzed demonstrated that LEU fuel behaves as expected. Under a sudden and large temperature change, the insertion of negative reactivity due to temperature feedback both of the fuel and the coolant causes the LEU fueled core to level off at a lower power than the HEU fuel, which is due to the large self-insertion of negative reactivity caused by the temperature excursion.

Also, based on the tests performed at the high power trip point, it can be observed that the fuel plates of the LEU model reach temperatures higher than those reached by the HEU. While this decreases the margin of safety of the reactor core under this particular transient, the highest temperatures reached (\sim 350 °C) are still acceptable, therefore the safety of the fuel is not compromised.

PARET proved itself to be a code which can be benchmarked easily against problems analyzed with more powerful tools such as RELAP, as Woodruff has demonstrated [4]. In the case of the HFIR, PARET shows an acceptable degree of agreement, but not in all cases. The computational model of the HFIR employed in PARET evolved many times, for instance, by implementing the variable fuel thickness in each of the 17 core regions in order to better represent the actual conditions and maintain flat plate geometry, instead of using half rectangle geometry. On the other hand, PARET can still be further developed. The first author of this report concludes that the restriction to 21 axial mesh segments is not enough to accommodate for large temperature gradients. Also, PARET can still be developed further to accommodate for the curved plates used at the HFIR. To this point, PARET still assumes the use of a flat plate, even while using the half rectangle geometry, which does not reflect the actual conditions.

Another way PARET can still be improved is by further developing the data collection procedures. The code uses a subroutine called POSTPROS which collects the data used in runs and stores them in text files. This subroutine works almost perfectly when the model of the core uses 4 or less core regions. In the case of the HFIR, where 17 core regions were used, this subroutine collects the data in a very cumbersome and impractical way. This is due to the old limitation of 72 characters per line that can be written, a limitation which is no longer present. Another way this data gathering subroutine can be improved is by specifying the interval where certain data points can be skipped by pointing at the time during the transient where this may take place, instead of specifying this by the time step number. In severe transients such as those studied here, small time steps can generate billions of time steps. In such a case, it is impractical to keep track of the time step number where the subroutine can skip certain data points in any given interval of time. Newer (unreleased) versions of PARET have improved filtering of individual channel output data. After the desired time is achieved, these data files are examined for relative change from time point to time point. A time point where the data change is too small compared to the previous saved time point data is filtered out automatically. These files are written as text, to enable their direct use in spread sheet and plotting programs.

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APPENDIX A

CALCULATION OF DELAYED NEUTRON PARAMETERS FOR THE HIGH FLUX ISOTOPE REACTOR

Delayed neutron parameters were computed for the High-Flux Isotope Reactor (HFIR) to support the LEU feasibility study. Parameters specified in the Safety Analysis Report (SAR) [A.1] are available for the HEU core and are used for both the conversion of reactivity values from absolute units to relative (dollar) units and for the safety analysis using the effective delayed neutron fractions and decay constants for six precursor groups. The current effective delayed neutron fraction specified in the SAR is 0.0076, which was adjusted from the original value of 0.0070 - 0.0071 [A.2] based on the value of the delayed neutron yield in ENDF/B-V.

The calculations performed for this work used nuclear data from both the ENDF/B-VI.8 and the ENDF/B-VII.0 data files [A.3]. The total fission neutron yield, delayed neutron yield, six precursor-group decay constants, relative delayed neutron yields, and delayed neutron emission spectra were extracted from the evaluated nuclear data files and processed to obtained data consistent with a 20 energy-group HFIR BOLD VENTURE model [A.4]. Data was extracted for U-235, U-238, Pu-239 and Pu-241, which are the primary fissioning nuclides in HFIR. Detailed data tables for each of these nuclides are shown in Figs. A.1 (ENDF/B-VI.8 data) and A.2 (ENDF/B-VII.0 data). The tables show small changes for the fission neutron yield at high energies for Pu-239, in addition to the delayed neutron yield for U-235. All other values (spectra, and neutron yields for other nuclides) are the same between ENDF/B-VI.8 and ENDF/B-VII.0. These data were processed and formatted into a DLAYXS interface file for use by BOLD VENTURE for calculating effective delayed neutron fractions using the PERTUBAT module [A.5].

Note that one significant change in ENDF/B-VII.0 from that of ENDF/B-VI.8 is that the delayed neutron yield at thermal energies for U-235 was reduced by about 5% to a value of 0.01585, which brings it to closer agreement with Keepin's value [A.5]. A comparison of the delayed neutron yield values is shown in Figure A.3. The ENDF/B-VI.8 evaluation held the delayed neutron yield constant at 0.0167 up to 4 MeV. The ENDF/B-VII.0 evaluation uses a value of 0.01585 up to 0.0253 eV and then ramps linearly to the ENDF/B-VII.8 value of 0.0167 at 50 keV and has this value up to 4 MeV [A.6]. Thus, the ENDF/B-VII.0 evaluation provides a different value for the U-235 delayed neutron yield at thermal and fast energies, which is consistent with previous measurements of the delay neutron yields [A.7]. The ENDF/B-VII.0 delayed neutron yield is more consistent with the data originally used in the determination of the HFIR effective delayed neutron fraction while the ENDF/B-VI.8 value is identical to that used in ENDF/B-V and is the basis for the value of the effective delayed neutron fraction in the HFIR SAR.

Using the HFIR BOLD VENTURE models of the HEU and LEU (monolithic U-10Mo fuel) cores, effective delayed neutron parameters and the prompt neutron lifetimes were calculated as a function of exposure. The PERTUBAT modules compute the importance-weighted values of these parameters. The BOLD VENTURE models were modified to perform adjoint-flux calculations at each depletion step to be used by the PERTUBAT module. The results of the calculations are provided in Table A.1 and Table A.2 for the HEU and LEU cases. Note that the effective delayed neutron fractions for the HEU core are consistent with the SAR value (0.0076) for the ENDF/B-VI.8 library and the original HFIR values (0.0071 in Ref. A.2) for the ENDF/B-VII.0 library. For the current work, the ENDF/B-VI.8 values are used to be consistent with the SAR safety analysis for the HEU core.

The prompt neutron lifetimes differ for the values quoted in the SAR and Cheverton and Sims report (33 μs in Ref. A.2 vs 50 μs in this work). This may require more investigation of the specific conditions that the neutron lifetimes were measured (ranges are given 33 – 74 μs), which likely do not correspond to the conditions calculated. In addition, different definitions of neutron lifetime are possible and they may not be consistent.

Another item of interest is the contribution of the different fissioning nuclides to the total effective delayed neutron fraction. Table A.3 provides the contributions for both the HEU and LEU cores. This table shows the larger U-238 contribution to the delayed neutron fraction for the LEU core in comparison to the HEU core. In addition, Pu-239 makes a much larger contribution at EOC for the LEU core than for the HEU core.

In addition to the total effective delayed neutron fraction, six group parameters are available for each fissioning nuclide. Given that U-235 fission for both HEU and LEU dominates the delayed neutron yield, it is reasonable to use the parameters for U-235 scaled to the appropriate total effective delayed neutron fraction.

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Delayed Neutron Data for u235 (endf/b-vi.8)
broad group
                                             delayed
                                                                        delayed neutron spectra by delayed group
                                                                        group 1 group 2 group 3 group 4 group 5 group 6 0.0000E+00 0.0000E+00 9.8234E-05 1.6147E-03 4.3022E-03 8.5630E-03
                   emax(eV)
      emin(eV)
                                 nubar
                                             nubar
                                                         beta
      2.4790E+06 2.0000E+07
                                 4.0050E+00 9.0000E-03 2.2472E-03
       1.5000E+06 2.4790E+06
                                 2.6458E+00 1.6700E-02
                                                         6.3120E-03
                                                                        2.0000E-03
                                                                                    3.2670E-03 1.0529E-02 3.5309E-02
                                                                                                                        3.8507E-02 4.8507E-02
        .7500E+05 1.5000E+06
                                 2.5517E+00 1.6700E-02 6.5446E-03
                                                                        1.0177E-01
                                                                                      2678E-01 7.3520E-02 1.6218E-01
                                                                                                                                    1.1734E-01
7.1632E-01
                                                                                                                        1.2069E-01
                                                                                                                        7.4458E-01
      8.5000E+04 8.7500E+05
                                 2.4789E+00 1.6700E-02 6.7369E-03
                                                                        7.5025E-01
                                                                                    7.7086E-01 8.2229E-01 7.2642E-01
       2.5800E+03 8.5000E+04
                                 2.4226E+00 1.6700E-02 6.8933E-03
                                                                        1.4474E-01
                                                                                      6349E-02 9.1538E-02 7.3115E-02 9.
                                                                                                                          0706E-02 1.0778E-01
      9.0000E+01 2.5800E+03
                                 2.4338E+00 1.6700E-02 6.8617E-03
                                                                        1.2158E-03
                                                                                   2.6405E-03 1.9572E-03 1.3199E-03 1.1886E-03 1.4621E-03
       2.7500E+01 9.0000E+01
                                 2.4338E+00
                                             1.6700E-02 6.8617E-03
                                                                          5486E-05
                                                                                    6.6078E-05 4.6314E-05 2.9550E-05
                                                                                                                          0073E-05 1.5841E-05
                                 2.4338E+00 1.6700E-02 6.8617E-03
                                                                                   1.9452E-05 1.3609E-05 8.6662E-06 5.8185E-06 4.4689E-06
      9.1000E+00 2.7500E+01
                                                                        4.4189E-06
       2.9700E+00 9.1000E+00
                                 2.4338E+00 1.6700E-02 6.8617E-03
                                                                        1.4580E-06
                                                                                    6.4801E-06 4.5311E-06 2.8838E-06 1.
1.3636E-06 9.5335E-07 6.0664E-07 4.
                                                                                                                          9292E-06 1.4692E-06
      1.6800E+00 2.9700E+00
                                             1.6700E-02 6.8617E-03
                                                                                                                        4.0541E-07
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                                 2.4338E+00
                                                                        3.0592E-07
                                                                                                                                     3.0792E-07
 11
      9.7500E-01 1.6800E+00
                                 2.4358E+00 1.6700E-02 6.8562E-03
                                                                        1.6706E-07
                                                                                    7.4525E-07 5.2099E-07 3.3151E-07 2.2147E-07 1.6810E-07
                                 2.4367E+00 1.6700E-02 6.8535E-03
                                                                                   3.6999E-07 2.5864E-07 1.6457E-07
      6.2500E-01 9.7500E-01
                                                                        8.2900E-08
                                                                                                                        1.0993E-07
                                                                                                                                    8.3405E-08
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       3.7500E-01 6.2500E-01
                                 2.4367E+00 1.6700E-02 6.8535E-03
                                                                        5 9201E-08 2 6427E-07 1 8474E-07 1 1755E-07 7 8512E-08 5 9555E-08
                                                                                    1.3213E-07 9.2370E-08 5.8773E-08
       2.5000E-01 3.7500E-01
                                 2.4367E+00
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      1.2500E-01 2.5000E-01
                                 2.4367E+00 1.6700E-02 6.8535E-03
                                                                        2.9593E-08 1.3213E-07 9.2370E-08 5.8770E-08 3.9250E-08 2.9767E-08
      4.0000E-02 1.2500E-01
                                 2.4367E+00 1.6700E-02 6.8535E-03
                                                                        2.0122E-08 8.9854E-08 6.2812E-08 3.9965E-08 2.6689E-08 2.0240E-08
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      7.5000E-03 4.0000E-02
2.5000E-03 7.5000E-03
                                 2 4367F±00 1 6700F=02 6 8535F=03
                                                                          .6933E-09 3.4355E-08 2.4016E-08 1.5280E-08 1.0205E-08 7.7380E-09
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                                 2.4367E+00 1.6700E-02 6.8535E-03
                                                                          1835E-09
                                                                                    5.2855E-09 3.6948E-09 2.3508E-09 1.5699E-09
                                                                       2.3671E-10 1.0571E-09 7.3896E-10 4.7017E-10 3.1398E-10 2.3809E-10 3.5270E-10 1.5751E-09 1.1010E-09 7.0055E-10 4.6785E-10 3.5476E-10
 19
      1.5000E-03 2.5000E-03
                                 2.4367E+00 1.6700E-02 6.8535E-03
       1.0000E-05 1.5000E-03
                                 2.4367E+00 1.6700E-02 6.8535E-03
                                                                        1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00
                                                                 sum
                                                    mean energy(eV)
                                                                        4.0079E+05 4.6901E+05 4.3925E+05 5.5373E+05 5.1401E+05 5.3587E+05
                                                    relative yield
                                                                        3.5008E-02 1.8070E-01 1.7251E-01 3.8678E-01 1.5858E-01 6.6427E-02
                                                                        1.3336E-02 3.2739E-02 1.2078E-01 3.0278E-01 8.4949E-01 2.8530E+00
                                                    decay constant
Delayed Neutron Data for u238 (endf/b-vi.8)
                                                                       delayed neutron spectra by delayed group
broad group
                                 total
                                             delaved
                                                         total
                                                                                   group 2 group 3 group 4
0.0000E+00 1.0683E-04 2.2494E-03
       emin(eV)
                    emax(eV)
                                 nubar
                                             nubar
                                                         beta
                                                                       group 1
                                                                       0.0000E+00
                                 4.0357E+00
                                             2.6000E-02 6.4425E-03
      2.4790E+06 2.0000E+07
                                                                                                                                   1.0223E-02
                                                                                                                       5.7624E-03
       1.5000E+06 2.4790E+06
                                 2.6339E+00 4.4000E-02 1.6705E-02
                                                                       2.4237E-03 3.7636E-03 9.7684E-03 3.9085E-02 3.9468E-02 5.1699E-02
       8.7500E+05 1.5000E+06
                                 2.5767E+00 4.4000E-02 1.7076E-02
                                                                        1.2144E-01 1.4521E-01 7.2600E-02 1.6085E-01 1.1106E-01 1.2190E-01
       8.5000E+04.8.7500E+05
                                 2.5263E+00 4.4000E-02 1.7417E-02
                                                                       7.5290E-01
                                                                                   7.6739E-01.8.1765E-01.7.1788E-01.7.4555E-01.7.1370E-01
       2.5800E+03 8.5000E+04
                                 2.4952E+00 4.4000E-02 1.7634E-02
                                                                        1.2222E-01
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       9.0000E+01 2.5800E+03
                                 2.4922E+00 4.4000E-02 1.7655E-02
                                                                        9.9841E-04 2.1617E-03 2.2262E-03 1.7166E-03 1.2631E-03 1.1290E-03
       2.7500E+01 9.0000E+01
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                                                                        1.2707E-05
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                                   .4921E+00 4.4000E-02 1.7656E-02
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       2.9700E+00 9.1000E+00
                                                                        1.1963E-06
                                                                       2.5100E-07 1.1262E-06 1.0914E-06 8.2439E-07 4.8316E-07 2.9593E-07 1.3707E-07 6.1547E-07 5.9640E-07 4.5051E-07 2.6398E-07 1.6161E-07
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       9.7500E-01 1.6800E+00
                                 2.4921E+00 4.4000E-02 1.7656E-02
                                                                       6.8018E-08 3.0555E-07 2.9609E-07 2.2365E-07 1.3104E-07 8.0202E-08
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       6.2500E-01 9.7500E-01
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       3.7500E-01 6.2500E-01
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       2.5000E-01 3.7500E-01
                                 2.4921E+00 4.4000E-02 1.7656E-02
                                                                       2.4283E-08 1.0913E-07 1.0574E-07
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       1 2500E-01 2 5000E-01
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       2.5000E-03 7.5000E-03
                                 2.4921E+00 4.4000E-02 1.7656E-02
                                                                        9.7109E-10 4.3651E-09 4.2296E-09 3.1948E-09 1.8716E-09 1.1451E-09
 18
 19
       1.5000E-03 2.5000E-03
                                 2.4921E+00 4.4000E-02 1.7656E-02
                                                                       1.9421E-10 8.7299E-10 8.4591E-10 6.3897E-10 3.7431E-10 2.2901E-10
       1.0000E-05 1.5000E-03
                                 2.4921E+00 4.4000E-02 1.7656E-02
                                                                        2.8938E-10 1.3008E-09 1.2604E-09 9.5205E-10 5.5773E-10 3.4123E-10
                                                                       1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00
                                                                 sum
                                                                       4.4090E+05 5.0662E+05 4.2594E+05 5.5192E+05 5.0645E+05 5.4802E+05
                                                    mean energy (eV)
                                                                       1.3938E-02 1.1280E-01 1.3103E-01 3.8514E-01 2.5399E-01 1.0310E-01 1.3630E-02 3.1334E-02 1.2334E-01 3.2373E-01 9.0597E-01 3.0487E+00
                                                    relative yield
                                                    decay constant
Delayed Neutron Data for pu239 (endf/b-vi.8)
broad group
                                 total
                                             delayed
                                                         total
                                                                        delayed neutron spectra by delayed group
      emin(eV)
                    emax(eV)
                                             nubar
                                                                        group 1
                                                                                   group 2
                                                                                                group 3
                                                                                                            group
                                                                        0.0000E+00
                                                                                    0.0000E+00 7.0488E-05 1.1506E-03 2.8300E-03 8.3058E-03
                                 4.5634E+00 4.3000E-03 9.4227E-04
      2.4790E+06 2.0000E+07
                                                                        2.0952E-03
                                                                        2.0952E-03 3.6845E-03 8.8427E-03 2.5493E-02 2.5151E-02 4.4540E-02 1.0618E-01 1.5938E-01 6.7873E-02 1.3179E-01 9.6010E-02 1.0396E-01
      1.5000E+06 2.4790E+06
                                 3.1752E+00 6.4500E-03 2.0314E-03
                                 3.0451E+00 6.4500E-03 2.1182E-03
      8.7500E+05 1.5000E+06
      8.5000E+04 8.7500E+05
                                 2.9453E+00 6.4500E-03 2.1899E-03
                                                                        7.5087E-01
                                                                                   7.6787E-01 8.1492E-01 7.5847E-01 7.8572E-01
                                                                                                                                    7.2605E-01
      2.5800E+03 8.5000E+04
                                 2.8983E+00 6.4500E-03 2.2254E-03
                                                                        1.3967E-01 6.7388E-02 1.0558E-01 8.1804E-02 8.9309E-02 1.1546E-01
                                2.8943E+00 6.4500E-03 2.2285E-03
2.8872E+00 6.4500E-03 2.2340E-03
                                                                        1.1647E-03 1.6259E-03 2.6257E-03 1.2614E-03 9.6021E-04 1.6605E-03 1.4837E-05 4.0676E-05 6.3258E-05 2.6733E-05 1.5428E-05 1.6836E-05
      9.0000E+01 2.5800E+03
      2.7500E+01 9.0000E+01
      9.1000E+00 2.7500E+01
                                 2.8632E+00 6.4500E-03 2.2527E-03
                                                                        4.2335E-06 1.1974E-05 1.8599E-05 7.8243E-06 4.4611E-06 4.7246E-06
      2.9700E+00 9.1000E+00
                                 2.8704E+00 6.4500E-03 2.2471E-03
                                                                        1.3968E-06
                                                                                   3.9890E-06 6.1936E-06 2.6020E-06 1.4780E-06 1.5506E-06
                                                                       2.9309E-07 8.3944E-07 1.3032E-06 5.4727E-07 3.1052E-07 3.2482E-07 1.6005E-07 4.5877E-07 7.1222E-07 2.9905E-07 1.6963E-07 1.7730E-07
 10
      1.6800E+00 2.9700E+00
                                 2.8788E+00 6.4500E-03 2.2405E-03
      9.7500E-01 1.6800E+00
                                 2.8787E+00 6.4500E-03 2.2406E-03
 11
 12
      6.2500E-01 9.7500E-01
                                 2.8746E+00 6.4500E-03 2.2438E-03
                                                                        7.9424E-08 2.2775E-07 3.5357E-07 1.4845E-07 8.4193E-08 8.7962E-08
      3.7500E-01 6.2500E-01
                                   .8654E+00 6.4500E-03 2.2510E-03
                                                                         .6718E-08 1.6268E-07 2.5255E-07 1.0603E-07 6.0129E-08
 14
      2.5000E-01 3.7500E-01
                                 2.8578E+00 6.4500E-03 2.2570E-03
                                                                       2.8354E-08 8.1342E-08 1.2628E-07 5.3014E-08 3.0062E-08 3.1396E-08
      1.2500E-01 2.5000E-01
                                 2.8631E+00 6.4500E-03 2.2528E-03
                                                                         .8352E-08 8.1342E-08 1.2628E-07 5.3014E-08 3.0060E-08
                                                                                                                                    3.1391E-08
 16
      4.0000E-02 1.2500E-01
                                 2.8739E+00 6.4500E-03 2.2443E-03
                                                                        1.9277E-08 5.5310E-08 8.5866E-08 3.6049E-08 2.0440E-08
                                                                                                                                    2.1343E-08
        .5000E-03 4.0000E-02
                                   8790E+00 6.4500E-03 2.2404E-03
                                                                         .3704E-09
                                                                                   2.1149E-08 3.2831E-08 1.3783E-08
 18
      2.5000E-03 7.5000E-03
                                 2.8804E+00 6.4500E-03 2.2393E-03
                                                                        1.1339E-09 3.2535E-09 5.0510E-09 2.1205E-09 1.2023E-09 1.2554E-09
                                                                       2.2679E-10 6.5071E-10 1.0102E-09 4.2411E-10 2.4047E-10 2.5108E-10 3.3790E-10 9.6957E-10 1.5052E-09 6.3191E-10 3.5828E-10 3.7409E-10
       1.5000E-03 2.5000E-03
                                 2.8806E+00 6.4500E-03 2.2391E-03
      1.0000E-05 1.5000E-03
                                 2.8807E+00 6.4500E-03 2.2391E-03
                                                                        1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00
                                                    mean energy(eV)
                                                                        4.0980E+05 5.2880E+05 4.1036E+05 5.0153E+05 4.6440E+05 5.1316E+05
                                                                        3.6306E-02 2.3644E-01 1.7893E-01 3.2667E-01 1.7016E-01 5.1500E-02
                                                    relative yield
                                                    decay constant
                                                                       1.3271E-02.3.0881E-02.1.1337E-01.2.9250E-01.8.5749E-01.2.7297E+00
```

Fig. A.1. Selected data from ENDF/B-VI.8 library.

Delay	red Neutron Data for pu24	1 (endf/b-v	i.8)							
broad	l group	total	delayed	total	delayed neu	tron specti	ra by delave	ed group		
grp	emin(eV) emax(eV)	nubar	nubar	beta		group 2	group 3	group 4	group 5	group 6
1	2.4790E+06 2.0000E+07	4.6174E+00	8.4000E-03	1.8192E-03	0.0000E+00					
2	1.5000E+06 2.4790E+06	3.1867E+00	1.6200E-02	5.0837E-03	2.8252E-03	3.9682E-03	8.6811E-03	2.8271E-02	3.0408E-02	4.5840E-02
3	8.7500E+05 1.5000E+06	3.0591E+00	1.6200E-02	5.2957E-03	1.4007E-01	1.7353E-01	6.8296E-02	1.3237E-01	1.0051E-01	1.1231E-01
4	8.5000E+04 8.7500E+05	2.9466E+00	1.6200E-02	5.4979E-03	7.5545E-01	7.6591E-01	8.1440E-01	7.5155E-01	7.6686E-01	7.2141E-01
5	2.5800E+03 8.5000E+04	2.9453E+00	1.6200E-02	5.5003E-03	1.0085E-01	5.5306E-02	1.0588E-01	8.4685E-02	9.7090E-02	1.1035E-01
6	9.0000E+01 2.5800E+03	2.9453E+00	1.6200E-02	5.5003E-03	7.8975E-04	1.2388E-03	2.5711E-03	1.5881E-03	1.1554E-03	1.3886E-03
7	2.7500E+01 9.0000E+01	2.9453E+00	1.6200E-02	5.5003E-03	1.0043E-05	3.1193E-05	6.1780E-05	3.5635E-05	1.9822E-05	1.6294E-05
8	9.1000E+00 2.7500E+01	2.9453E+00	1.6200E-02	5.5003E-03	2.8655E-06	9.1841E-06	1.8162E-05	1.0451E-05	5.7499E-06	4.6237E-06
9	2.9700E+00 9.1000E+00	2.9453E+00	1.6200E-02	5.5003E-03	9.4544E-07	3.0599E-06	6.0482E-06	3.4780E-06	1.9069E-06	1.5229E-06
10	1.6800E+00 2.9700E+00	2.9453E+00	1.6200E-02	5.5003E-03	1.9837E-07	6.4392E-07	1.2726E-06	7.3165E-07	4.0075E-07	3.1936E-07
11	9.7500E-01 1.6800E+00	2.9453E+00	1.6200E-02	5.5003E-03	1.0833E-07	3.5191E-07	6.9550E-07	3.9982E-07	2.1893E-07	1.7437E-07
12	6.2500E-01 9.7500E-01	2.9453E+00	1.6200E-02	5.5003E-03	5.3756E-08	1.7471E-07	3.4527E-07	1.9848E-07	1.0867E-07	8.6525E-08
13	3.7500E-01 6.2500E-01	2.9453E+00	1.6200E-02	5.5003E-03	3.8388E-08	1.2479E-07	2.4662E-07	1.4177E-07	7.7613E-08	6.1786E-08
14	2.5000E-01 3.7500E-01	2.9453E+00	1.6200E-02	5.5003E-03	1.9191E-08	6.2395E-08	1.2331E-07	7.0884E-08	3.8803E-08	3.0887E-08
15	1.2500E-01 2.5000E-01	2.9453E+00	1.6200E-02	5.5003E-03	1.9190E-08	6.2395E-08	1.2331E-07	7.0883E-08	3.8802E-08	3.0884E-08
16	4.0000E-02 1.2500E-01	2.9453E+00	1.6200E-02	5.5003E-03	1.3047E-08	4.2429E-08	8.3848E-08	4.8198E-08	2.6383E-08	2.0999E-08
17	7.5000E-03 4.0000E-02	2.9453E+00	1.6200E-02	5.5003E-03	4.9886E-09	1.6223E-08	3.2060E-08	1.8429E-08	1.0088E-08	8.0285E-09
18	2.5000E-03 7.5000E-03	2.9453E+00	1.6200E-02	5.5003E-03	7.6747E-10	2.4958E-09	4.9321E-09	2.8352E-09	1.5519E-09	1.2352E-09
19	1.5000E-03 2.5000E-03	2.9453E+00	1.6200E-02	5.5003E-03	1.5349E-10	4.9916E-10	9.8644E-10	5.6704E-10	3.1038E-10	2.4703E-10
20	1.0000E-05 1.5000E-03	2.9453E+00	1.6200E-02	5.5003E-03	2.2871E-10	7.4374E-10	1.4698E-09	8.4489E-10	4.6247E-10	3.6808E-10
				sum	1.0000E+00	1.0000E+00	1.0000E+00	1.0000E+00	1.0000E+00	1.0000E+00
			mean	energy(eV)	4.7890E+05	5.5653E+05	4.0842E+05	5.0228E+05	4.7670E+05	5.2353E+05
			rela	tive yield	1.8049E-02	2.2430E-01	1.4261E-01	3.4925E-01	1.9758E-01	6.8208E-02
			deca	y constant	1.3599E-02	2.9966E-02	1.1673E-01	3.0691E-01	8.7010E-01	3.0028E+00

Fig. A.1. Selected data from ENDF/B-VI.8 library (continued).

```
Delayed Neutron Data for u235 (endf/b-vii.0)
                                                         delayed
                                                                       total
                                                                                          delayed neutron spectra by delayed group
broad group
                                          total
        emin(eV) emax(eV)
2.4790E+06 2.0000E+07
                                         nubar nubar beta
3.9991E+00 9.0000E-03 2.2505E-03
                                                                                          group 1
0.0000E+00
                                                                                                        group 2 group 3 group 4
0.0000E+00 9.8233E-05 1.6147E-03
                                                                                                                                                     group 5 group 6
4.3023E-03 8.5630E-03
                                                                                         2.0000E-03 3.2670E-03 1.0529E-02 3.5309E-02 3.8507E-02 4.8507E-02 1.0177E-01 1.2678E-01 7.3520E-02 1.6218E-01 1.2069E-01 1.1734E-01
        1.5000E+06 2.4790E+06
                                         2.6522E+00 1.6700E-02 6.2967E-03
        8.7500E+05 1.5000E+06
                                         2.5554E+00
                                                        1.6700E-02 6.5351E-03
        8.5000E+04.8.7500E+05
                                         2.4826E+00.1.6700E-02.6.7267E-03
                                                                                          7.5025E-01
                                                                                                        7.7086E-01.8.2229E-01.7.2642E-01.7.4458E-01
                                                                                                                                                                     7.1632E-01
        2.5800E+03 8.5000E+04
                                         2.4236E+00 1.6594E-02 6.8470E-03
                                                                                          1.4474E-01 9.6349E-02 9.1538E-02 7.3115E-02 9.0706E-02 1.0778E-01
        9.0000E+01 2.5800E+03
                                         2.4338E+00 1.5873E-02 6.5218E-03
                                                                                          1.2158E-03 2.6405E-03 1.9572E-03 1.3199E-03 1.1886E-03 1.4621E-03
                                                                                          1.5486E-05 6.6078E-05 4.6314E-05 2.9550E-05 2.0073E-05 1.5841E-05
        2.7500E+01 9.0000E+01
                                         2.4351E+00 1.5851E-02 6.5093E-03
        9.1000E+00 2.7500E+01
                                         2.4364E+00 1.5850E-02 6.5055E-03
                                                                                          4.4189E-06 1.9452E-05 1.3609E-05 8.6662E-06 5.8185E-06 4.4689E-06
        2.9700E+00 9.1000E+00
                                         2.4367E+00
                                                        1.5850E-02 6.5047E-03
                                                                                          1.4580E-06 6.4801E-06 4.5311E-06 2.8838E-06 1.9292E-06 1.4692E-06
  10
        1.6800E+00.2.9700E+00
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          3.0592E-07 1.3636E-06 9.5335E-07 6.0664E-07 4.0541E-07 3.0792E-07
                                                                                                        7.4525E-07 5.2099E-07 3.3151E-07
        9.7500E-01 1.6800E+00
                                         2.4367E+00
                                                         1.5850E-02 6.5047E-03
                                                                                          1.6706E-07
                                                                                                                                                     2.2147E-07
                                                                                                                                                                      1.6810E-07
  11
  12
        6.2500E-01 9.7500E-01
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          8.2900E-08 3.6999E-07 2.5864E-07 1.6457E-07 1.0993E-07
                                                                                                                                                                     8.3406E-08
        3.7500E-01 6.2500E-01
  14
        2.5000E-01 3.7500E-01
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          2.9597E-08 1.3213E-07 9.2370E-08 5.8773E-08 3.9252E-08 2.9771E-08
        1.2500E-01 2.5000E-01
                                                                                                        1.3213E-07 9.2370E-08 5.8771E-08
                                         2.4367E+00
                                                         1.5850E-02 6.5047E-03
                                                                                            9593E-08
                                                                                                                                                         9250E-08
  16
        4.0000E-02 1.2500E-01
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          2.0122E-08 8.9854E-08 6.2812E-08 3.9964E-08 2.6689E-08 2.0240E-08
         7.5000E-03 4.0000E-02
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          7.6933E-09 3.4355E-08 2.4016E-08 1.5280E-08 1.0205E-08
        2.5000E-03 7.5000E-03
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          1.1835E-09 5.2855E-09 3.6948E-09 2.3508E-09 1.5699E-09 1.1905E-09
  18
                                                                                          2.3671E-10 1.0571E-09 7.3896E-10 4.7017E-10 3.1398E-10 2.3809E-10
        1.5000E-03 2.5000E-03
                                         2.4367E+00 1.5850E-02 6.5047E-03
 20
        1.0000E-05 1.5000E-03
                                         2.4367E+00 1.5850E-02 6.5047E-03
                                                                                          3.5270E-10 1.5751E-09 1.1010E-09 7.0055E-10 4.6785E-10 3.5476E-10
                                                                                          1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00
                                                                                          4.0079E+05 4.6901E+05 4.3925E+05 5.5373E+05 5.1401E+05 5.3587E+05
                                                                 mean energy(eV)
                                                                                         3.1973E-02 1.6637E-01 1.6131E-01 4.5965E-01 1.3350E-01 4.7200E-02 1.2491E-02 3.1824E-02 1.0938E-01 3.1699E-01 1.3540E+00 8.6364E+00
                                                                 relative vield
                                                                 decay constant
Delayed Neutron Data for u238 (endf/b-vii.0)
broad group
                                         total
                                                        delayed
                                                                       total
                                                                                         delayed neutron spectra by delayed group
                                                        nubar
                                                                                         group 1 group 2 group 3 group 4
0.0000E+00 0.0000E+00 1.0683E-04 2.2494E-03
                         emax(eV)
                                         nubar
                                                                                                                                                      group 5
                                         4.0282E+00 2.6000E-02 6.4544E-03
                                                                                                                                                     5.7624E-03 1.0223E-02
        2.4790E+06 2.0000E+07
                                                                                         2.4237E-03 3.7636E-03 9.7684E-03 3.9085E-02 3.9468E-02 5.1699E-02 1.2144E-01 1.4521E-01 7.2600E-02 1.6085E-01 1.1106E-01 1.2190E-01
        1.5000E+06 2.4790E+06
                                         2.6339E+00 4.4000E-02 1.6705E-02
        8.7500E+05 1.5000E+06
                                         2.5767E+00 4.4000E-02 1.7076E-02
        8.5000E+04 8.7500E+05
                                         2.5263E+00 4.4000E-02 1.7417E-02
                                                                                          7.5290E-01 7.6739E-01 8.1765E-01 7.1788E-01 7.4555E-01
                                                                                                                                                                     7.1370E-01
                                                                                         1.2222E-01 8.1389E-02 9.7568E-02 7.8163E-02 9.6863E-02 1.0132E-01
        2.5800E+03 8.5000E+04
                                         2.4952E+00 4.4000E-02 1.7634E-02
        9.0000E+01 2.5800E+03
                                         2.4922E+00 4.4000E-02 1.7655E-02
                                                                                            .9841E-04 2.1617E-03 2.2262E-03 1.7166E-03 1.2631E-03 1.1290E-03
        2.7500E+01 9.0000E+01
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         1.2707E-05 5.4550E-05 5.3003E-05 4.0074E-05 2.3760E-05 1.4931E-05
        9.1000E+00 2.7500E+01
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         3.6257E-06 1.6062E-05 1.5577E-05 1.1770E-05 6.9209E-06 4.2705E-06
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         1.1963E-06 5.3515E-06 5.1869E-06 3.9183E-06 2.2982E-06 1.4101E-06
        2.9700E+00 9.1000E+00
                                        2.4921E+00 4.4000E-02 1.7656E-02
2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         2.5100E-07 1.1262E-06 1.0914E-06 8.2439E-07 4.8316E-07 2.9593E-07 1.3707E-07 6.1547E-07 5.9640E-07 4.5051E-07 2.6398E-07 1.6161E-07
        1.6800E+00 2.9700E+00
        9.7500E-01 1.6800E+00
  11
                                                                                         6.8018E-08 3.0555E-07 2.9609E-07 2.2365E-07 1.3104E-07 8.0202E-08 4.8572E-08 2.1825E-07 2.1149E-07 1.5975E-07 9.3592E-08 5.7275E-08
        6.2500E-01 9.7500E-01
                                         2.4921E+00 4.4000E-02 1.7656E-02
 12
        3.7500E-01 6.2500E-01
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                                                                                     9.3592E-08
  13
        2.5000E-01 3.7500E-01
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         2.4283E-08 1.0913E-07 1.0574E-07 7.9874E-08 4.6794E-08 2.8634E-08
                                         2.4921E+00 4.4000E-02 1.7656E-02
        1.2500E-01 2.5000E-01
                                                                                            4280E-08 1.0913E-07 1.0574E-07 7.9870E-08 4.6791E-08
        4.0000E-02 1.2500E-01
                                         2.4921E+00.4.4000E-02.1.7656E-02
                                                                                         1.6509E-08 7.4208E-08 7.1905E-08 5.4314E-08 3.1818E-08 1.9468E-08
 16
        7.5000E-03 4.0000E-02
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         6.3121E-09 2.8373E-08 2.7493E-08 2.0766E-08 1.2165E-08
                                                                                                                                                                     7.4430E-09
  17
 18
        2.5000E-03 7.5000E-03
                                        2.4921E+00 4.4000E-02 1.7656E-02
2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         9.7109E-10 4.3651E-09 4.2296E-09 3.1948E-09 1.8716E-09 1.1451E-09
                                                                                          1.9421E-10 8.7299E-10 8.4591E-10 6.3897E-10 3.7431E-10 2.2901E-10
        1.0000E-05 1.5000E-03
                                         2.4921E+00 4.4000E-02 1.7656E-02
                                                                                         2.8938E-10 1.3008E-09 1.2604E-09 9.5205E-10 5.5773E-10 3.4123E-10
                                                                                          1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00 1.0000E+00
                                                                                         4.4090E+05 5.0662E+05 4.2594E+05 5.5192E+05 5.0645E+05 5.4802E+05
                                                                 mean energy(eV)
                                                                relative vield
                                                                                         1.0341E-02 1.1482E-01 1.2781E-01 4.5184E-01 2.3351E-01 6.1689E-02
                                                                decay constant
                                                                                         1.2494E-02 3.0255E-02 1.1594E-01 3.4148E-01 1.3186E+00 9.9790E+00
Delayed Neutron Data for pu239 (endf/b-vii.0)
                                                        delayed
                                         total
                                                                                          delayed neutron spectra by delayed group
broad group
                                                                       total
       emin(eV)
                        emax(eV)
                                                                                          group 1 group 2 group 3 group 4 group 5 group 6 0.0000E+00 0.0000E+00 7.0488E-05 1.1506E-03 2.8300E-03 8.3058E-03 2.0952E-03 3.6845E-03 8.8427E-03 2.5493E-02 2.5151E-02 4.4540E-02
                                         nubar
                                                        nubar
                                                                       beta
grp
                                         4.5568E+00 4.3000E-03 9.4365E-04
3.1764E+00 6.4500E-03 2.0306E-03
       2.4790E+06 2.0000E+07
        1.5000E+06 2.4790E+06
        8.7500E+05 1.5000E+06
                                         3.0440E+00 6.4500E-03 2.1189E-03
                                                                                          1.0618E-01
                                                                                                        1 5938E-01 6 7873E-02 1 3179E-01 9 6010E-02 1 0396E-01
        8.5000E+04 8.7500E+05
                                         2.9430E+00 6.4500E-03 2.1916E-03
                                                                                          7.5087E-01
                                                                                                        7.6787E-01 8.1492E-01 7.5847E-01
                                                                                                                                                      7.8572E-01
        2.5800E+03.8.5000E+04
                                         2.8956E+00 6.4500E-03 2.2275E-03
                                                                                          1.3967E-01 6.7388E-02 1.0558E-01 8.1804E-02 8.9309E-02 1.1546E-01
                                                                                          1.1647E-03 1.6259E-03 2.6257E-03 1.2614E-03 9.6021E-04 1.6605E-03
                                         2.8943E+00 6.4500E-03 2.2285E-03
        9.0000E+01 2.5800E+03
        2.7500E+01 9.0000E+01
                                         2.8872E+00 6.4500E-03 2.2340E-03
                                                                                         1.4837E-05 4.0676E-05 6.3258E-05 2.6733E-05 1.5428E-05 1.6836E-05
        9.1000E+00 2.7500E+01
                                         2.8632E+00 6.4500E-03 2.2527E-03
                                                                                          4.2335E-06 1.1974E-05 1.8599E-05 7.8243E-06 4.4611E-06 4.7246E-06
        2.9700E+00 9.1000E+00
                                         2.8704E+00 6.4500E-03 2.2471E-03
                                                                                          1.3968E-06.3.9890E-06.6.1936E-06.2.6020E-06.1.4780E-06.1.5506E-06
        1.6800E+00 2.9700E+00
                                         2.8788E+00 6.4500E-03 2.2405E-03
                                                                                          2.9309E-07
                                                                                                        8.3944E-07 1.3032E-06 5.4727E-07
                                                                                                                                                      3.1052E-07
                                                                                                                                                                     3.2482E-07
 11
        9.7500E-01 1.6800E+00
                                         2.8787E+00 6.4500E-03 2.2406E-03
                                                                                          1.6005E-07 4.5877E-07 7.1222E-07 2.9905E-07 1.6963E-07 1.7730E-07
                                         2.8746E+00 6.4500E-03 2.2438E-03
                                                                                            .9424E-08 2.2775E-07 3.5357E-07 1.4845E-07
 13
        3.7500E-01 6.2500E-01
                                         2.8654E+00 6.4500E-03 2.2510E-03
                                                                                         5.6718E-08 1.6268E-07 2.5255E-07 1.0603E-07 6.0129E-08 6.2806E-08
        2.5000E-01 3.7500E-01
                                                                                                         8.1342E-08 1.2628E-07 5.3014E-08
                                         2.8578E+00 6.4500E-03 2.2570E-03
                                                                                          2.8354E-08
 15
        1.2500E-01 2.5000E-01
                                         2.8631E+00 6.4500E-03 2.2528E-03
                                                                                          2.8352E-08 8.1342E-08 1.2628E-07 5.3014E-08 3.0060E-08 3.1391E-08
        4.0000E-02 1.2500E-01
                                         2.8739E+00 6.4500E-03 2.2443E-03
                                                                                          1.9277E-08 5.5310E-08 8.5866E-08 3.6049E-08 2.0440E-08 2.1343E-08
 16
 17
        7.5000E-03 4.0000E-02
2.5000E-03 7.5000E-03
                                         2.8790E+00 6.4500E-03 2.2404E-03
                                                                                          7.3704E-09 2.1149E-08 3.2831E-08 1.3783E-08 7.8151E-09 8.1600E-09
                                         2.8804E+00 6.4500E-03 2.2393E-03
                                                                                          1.1339E-09
                                                                                                        3.2535E-09 5.0510E-09 2.1205E-09 1.2023E-09 1.2554E-09
 19
        1.5000E-03 2.5000E-03
                                         2.8806E+00 6.4500E-03 2.2391E-03
                                                                                         2.2679E-10 6.5071E-10 1.0102E-09 4.2411E-10 2.4047E-10 2.5108E-10
                                                                                         3.3790E-10 9.6957E-10 1.5052E-09 6.3191E-10 3.5828E-10 3.7409E-10 1.0000E+00 
        1.0000E-05 1.5000E-03
                                         2.8807E+00 6.4500E-03 2.2391E-03
                                                                                 sum
                                                                 mean energy(eV)
                                                                                          4.0980E+05 5.2880E+05 4.1036E+05 5.0153E+05 4.6440E+05 5.1316E+05
                                                                                         3.3084E-02 2.6807E-01 1.8711E-01 3.9075E-01 1.0395E-01 1.7041E-02 1.2481E-02 2.9947E-02 1.0716E-01 3.1762E-01 1.3524E+00 1.0691E+01
                                                                 decay constant
```

Fig. A.2. Selected data from ENDF/B-VII.0 library.

Delay	yed Neutron Data for pu24	11 (endf/b-vii.	.0)							
broad	d group	total de	elayed	total	delayed neu	itron specti	ra by delaye	ed group		
grp	emin(eV) emax(eV)	nubar nu	ubar	beta	group 1	group 2	group 3	group 4	group 5	group 6
1	2.4790E+06 2.0000E+07	4.6174E+00 8.	.4000E-03	1.8192E-03	0.0000E+00	0.0000E+00	8.2553E-05	1.4878E-03	3.9495E-03	8.6683E-03
2	1.5000E+06 2.4790E+06	3.1867E+00 1.	.6200E-02	5.0837E-03	2.8252E-03	3.9682E-03	8.6811E-03	2.8271E-02	3.0408E-02	4.5840E-02
3	8.7500E+05 1.5000E+06	3.0591E+00 1.	.6200E-02	5.2957E-03	1.4007E-01	1.7353E-01	6.8296E-02	1.3237E-01	1.0051E-01	1.1231E-01
4	8.5000E+04 8.7500E+05	2.9466E+00 1.	.6200E-02	5.4979E-03	7.5545E-01	7.6591E-01	8.1440E-01	7.5155E-01	7.6686E-01	7.2141E-01
5	2.5800E+03 8.5000E+04	2.9453E+00 1.	.6200E-02	5.5003E-03	1.0085E-01	5.5306E-02	1.0588E-01	8.4685E-02	9.7090E-02	1.1035E-01
6	9.0000E+01 2.5800E+03	2.9453E+00 1.	.6200E-02	5.5003E-03	7.8975E-04	1.2388E-03	2.5711E-03	1.5881E-03	1.1554E-03	1.3886E-03
7	2.7500E+01 9.0000E+01	2.9453E+00 1.	.6200E-02	5.5003E-03	1.0043E-05	3.1193E-05	6.1780E-05	3.5635E-05	1.9822E-05	1.6294E-05
8	9.1000E+00 2.7500E+01	2.9453E+00 1.	.6200E-02	5.5003E-03	2.8655E-06	9.1841E-06	1.8162E-05	1.0451E-05	5.7499E-06	4.6237E-06
9	2.9700E+00 9.1000E+00	2.9453E+00 1.	.6200E-02	5.5003E-03	9.4544E-07	3.0599E-06	6.0482E-06	3.4780E-06	1.9069E-06	1.5229E-06
10	1.6800E+00 2.9700E+00	2.9453E+00 1.	.6200E-02	5.5003E-03	1.9837E-07	6.4392E-07	1.2726E-06	7.3165E-07	4.0075E-07	3.1936E-07
11	9.7500E-01 1.6800E+00	2.9453E+00 1.	.6200E-02	5.5003E-03	1.0833E-07	3.5191E-07	6.9550E-07	3.9982E-07	2.1893E-07	1.7437E-07
12	6.2500E-01 9.7500E-01	2.9453E+00 1.	.6200E-02	5.5003E-03	5.3756E-08	1.7471E-07	3.4527E-07	1.9848E-07	1.0867E-07	8.6525E-08
13	3.7500E-01 6.2500E-01	2.9453E+00 1.	.6200E-02	5.5003E-03	3.8388E-08	1.2479E-07	2.4662E-07	1.4177E-07	7.7613E-08	6.1786E-08
14	2.5000E-01 3.7500E-01	2.9453E+00 1.	.6200E-02	5.5003E-03	1.9191E-08	6.2395E-08	1.2331E-07	7.0884E-08	3.8803E-08	3.0887E-08
15	1.2500E-01 2.5000E-01	2.9453E+00 1.	.6200E-02	5.5003E-03	1.9190E-08	6.2395E-08	1.2331E-07	7.0883E-08	3.8802E-08	3.0884E-08
16	4.0000E-02 1.2500E-01	2.9453E+00 1.	.6200E-02	5.5003E-03	1.3047E-08	4.2429E-08	8.3848E-08	4.8198E-08	2.6383E-08	2.0999E-08
17	7.5000E-03 4.0000E-02	2.9453E+00 1.	.6200E-02	5.5003E-03	4.9886E-09	1.6223E-08	3.2060E-08	1.8429E-08	1.0088E-08	8.0285E-09
18	2.5000E-03 7.5000E-03	2.9453E+00 1.	.6200E-02	5.5003E-03	7.6747E-10	2.4958E-09	4.9321E-09	2.8352E-09	1.5519E-09	1.2352E-09
19	1.5000E-03 2.5000E-03	2.9453E+00 1.	.6200E-02	5.5003E-03	1.5349E-10	4.9916E-10	9.8644E-10	5.6704E-10	3.1038E-10	2.4703E-10
20	1.0000E-05 1.5000E-03	2.9453E+00 1.	.6200E-02	5.5003E-03	2.2871E-10	7.4374E-10	1.4698E-09	8.4489E-10	4.6247E-10	3.6808E-10
				sum	1.0000E+00	1.0000E+00	1.0000E+00	1.0000E+00	1.0000E+00	1.0000E+00
			mean	energy(eV)	4.7890E+05	5.5653E+05	4.0842E+05	5.0228E+05	4.7670E+05	5.2353E+05
			relat	ive yield	1.8049E-02	2.2430E-01	1.4261E-01	3.4925E-01	1.9758E-01	6.8208E-02
			decay	constant	1.3599E-02	2.9966E-02	1.1673E-01	3.0691E-01	8.7010E-01	3.0028E+00
			_							

Fig. A.2. Selected data from ENDF/B-VII.0 library (continued).

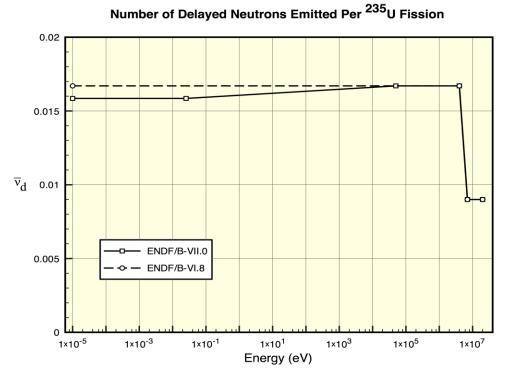


Figure A.3. Comparison of the number of delayed neutrons from 235U fission from ENDF/B-VI.8 and ENDF/B-VII.0 (ENDF/B-VII.8 is identical to ENDF/B-V data).

Table A.1. Prompt neutron lifetime and effective delayed neutron fractions for the HFIR HEU core (critical conditions throughout the cycle)

(critical conditions throughout the cycle)									
		ENDF/B-VI.8			EN	IDF/B-VII	.0		
Full Power	Prompt Neutron			Beta-eff/			Beta-eff/		
Days	Lifetime (sec)	Beta	Beta-eff	Beta	Beta	Beta-eff	Beta		
0.00	5.20E-05	6.80E-03	7.62E-03	1.12	6.46E-03	7.24E-03	1.12		
0.59	5.19E-05	6.80E-03	7.61E-03	1.12	6.46E-03	7.23E-03	1.12		
1.78	6.12E-05	6.80E-03	7.62E-03	1.12	6.46E-03	7.24E-03	1.12		
7.18	6.76E-05	6.79E-03	7.60E-03	1.12	6.45E-03	7.22E-03	1.12		
14.12	7.50E-05	6.78E-03	7.57E-03	1.12	6.44E-03	7.19E-03	1.12		
18.82	8.24E-05	6.78E-03	7.55E-03	1.11	6.44E-03	7.17E-03	1.11		
21.18	8.89E-05	6.78E-03	7.53E-03	1.11	6.44E-03	7.15E-03	1.11		
23.53	9.02E-05	6.78E-03	7.53E-03	1.11	6.44E-03	7.15E-03	1.11		
26.00	9.43E-05	6.78E-03	7.52E-03	1.11	6.44E-03	7.14E-03	1.11		

Table A.2. Prompt neutron lifetime and effective delayed neutron fractions for the HFIR LEU (monolithic U-10Mo) core (critical conditions throughout the cycle)

		ENDF/B-VI.8			EN	DF/B-VI	[.0
Full Power	Prompt Neutron			Beta-eff/			Beta-eff/
Days	Lifetime (sec)	Beta	Beta-eff	Beta	Beta	Beta-eff	Beta
0.00	4.68E-05	6.90E-03	7.49E-03	1.09	6.57E-03	7.13E-03	1.09
0.59	5.02E-05	6.90E-03	7.46E-03	1.08	6.57E-03	7.11E-03	1.08
1.78	5.71E-05	6.89E-03	7.47E-03	1.08	6.56E-03	7.12E-03	1.08
7.18	5.95E-05	6.84E-03	7.41E-03	1.08	6.52E-03	7.06E-03	1.08
14.12	6.44E-05	6.77E-03	7.31E-03	1.08	6.45E-03	6.97E-03	1.08
18.82	7.04E-05	6.72E-03	7.24E-03	1.08	6.41E-03	6.90E-03	1.08
21.18	7.11E-05	6.70E-03	7.22E-03	1.08	6.39E-03	6.88E-03	1.08
23.53	7.14E-05	6.68E-03	7.19E-03	1.08	6.36E-03	6.85E-03	1.08
26.00	7.17E-05	6.65E-03	7.17E-03	1.08	6.34E-03	6.83E-03	1.08

Table A.3. Contributions to effective delayed neutron fraction by nuclide for the HEU and LEU cores computed with ENDF/B-VII.0 data

for the TIEC and EEC cores computed with ENDI/B-VII.0 data								
	HE	U	LEU					
	ВОС	EOC	BOC	EOC				
U-235	7.24E-03	7.12E-03	6.88E-03	6.43E-03				
U-238	2.19E-06	2.09E-06	2.56E-04	2.58E-04				
Pu-239	3.69E-08	1.23E-05	3.50E-08	1.26E-04				
Pu-241	3.91E-09	5.30E-06	3.70E-09	1.29E-05				
Total	7.24E-03	7.14E-03	7.13E-03	6.83E-03				

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