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> PM Motor Parametric Design Analyses for a Hybrid Electric Vehicle Traction Drive Application — Interim Report

> > R. H. Staunton P. J. Otaduy J. W. McKeever S. C. Nelson J. M. Bailey S. Das R. L. Smith



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Engineering Science and Technology Division

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# ACRONYMS, ABBREVIATIONS, AND INITIALISMS

| AEMD     | Automotive Electric Machine Drive                                   |
|----------|---|
| BDCM     | brushless dc motor  |
| CPA      | conventional phase advance  |
| CPSR     | constant power speed ratio  |
| CRADA    | cooperative research and development agreement                      |
| CRML     | cold-rolled motor lamination  |
| DEEMS    | Delphi Energy and Engine Management Systems                         |
| DMIC     | dual mode inverter control  |
| DOE      | Department of Energy  |
| DSP      | digital signal processor  |
| EETT     | Electrical and Electronics Technical Teams                          |
| emf      | electromotive force   |
| FEA      | finite element analysis   |
| GNO      | grain non-oriented  |
| HEV      | hybrid electric vehicle   |
| IPM      | interior permanent magnet   |
| ISP      | current limit setpoint  |
| IGBT     | insulated gate bipolar transistor                                   |
| OD       | outer diameter  |
| OEM      | original equipment manufacturers                                    |
| ORNL     | Oak Ridge National Laboratory                                       |
| PEEMRC   | Power Electronics and Electric Machinery Research Center            |
| PM       | permanent magnet  |
| PMBLDC   | permanent magnet brushless dc                                       |
| PMSM     | permanent magnet synchronous motor                                  |
| PNGV     | Partnership for a New Generation of Vehicles                        |
| PWM      | pulse width modulation  |
| RFP      | request for proposals   |
| SHV      | series hybrid vehicle   |
| SPEEDCAD | Scottish Power Electronics and Electric Drive Computer-Aided Design |
| SRM      | switched reluctance motor   |
|          |   |

# **EXECUTIVE SUMMARY**

The Department of Energy's (DOE) Office of FreedomCAR (Cooperative Automotive Research) and Vehicle Technologies has a strong interest in making rapid progress in permanent magnet (PM) machine development. The program is directing various technology development projects that will advance the technology and lead to request for proposals (RFP) for manufacturer prototypes. This aggressive approach is possible because the technology is clearly within reach and the approach is deemed essential, based on strong market demand, escalating fuel prices, and competitive considerations.

In response, this study began parallel development paths that included a literature search/review, development and utilization of multiple parametric models to determine the effects of design parameters, verification of the modeling methodology, development of an interior PM (IPM) machine baseline design, development of alternative machine baseline designs, and cost analyses for several candidate machines. This interim progress report summarizes the results of these activities as of June 2004.

This report provides background and summary information for recent machine parametric studies and testing programs that demonstrate both the potential capabilities and technical limitations of

- brushless PM machines (axial gap and radial gap),
- the IPM machine,
- the surface-mount PM machines (interior or exterior rotor),
- induction machines, and
- switched reluctance machines.

The FreedomCAR program, while acknowledging the progress made by Oak Ridge National Laboratory, Delphi, Delco-Remy International, and others in these programs, has redirected efforts toward a "short path" to a marketable and competitive PM motor for hybrid electric vehicle traction applications. The program has developed a set of performance targets for the type of traction machine desired. The short-path approach entails a comprehensive design effort focusing on the IPM machine and meeting the performance targets. The selection of the IPM machine reflects industry's confidence in this market-proven design that exhibits a power density surpassed by no other machine design.

#### Preliminary Conclusions

In order to meet the machine target specifications provided by the OEMs to the maximum extent possible, machine designers and analysts must explore the following:

- 1. Higher voltages (closer to 600 V versus the 200–450 specified) should be considered, at least during low-speed operation, to prevent violation of the IPM machine current limit and to achieve the high efficiency requirements;
- 2. New rotor configurations and innovative lamination materials should be explored for potential performance advantages;

- 3. The use of injected magnets should be evaluated as a means of more fully meeting the cost per kW requirement; and
- 4. Field weakening is a requirement.

### IPM Design Considerations

The major focuses of this study were the complex mechanical and electro-magnetic design issues of a high-speed, high-power-density IPM machine. For instance, at high speeds, rotor structural integrity and mechanical balance are critical design issues. Also, a low-voltage, IPM machine requires a reduced number of turns in the stator poles or flux weakening to deliver the same amount of power at low and high rotor speeds. In order to conserve PM energy, the rotor's bridge must operate in a saturated state even at zero stator current condition. If this is not the case, a very significant percentage of the PM flux is wasted.

Any Hybrid Electric Vehicle (HEV) traction motor application tends to place restrictions on machine weight, size, source voltage, maximum current, available cooling, etc. It has become clear during the IPM design process that high stator currents are a characteristic of low-speed operation where a limited-duration, peak-power capability is required. Direct results of high current operation are the significant zones of saturation or near-saturation conditions that result in the stator and rotor. Of course, this is expected in any well-designed, high-power-density, IPM machine.

An important conclusion reached during the design process is that machine performance goals need to reconcile conflicting design impacts such as efficiency and high power density during low-speed, peak power operation. It will be difficult to meet all of the performance targets simultaneously. Also, the analysts believe that a significant improvement in performance can be achieved with the use of bi-state and improved ferromagnetic materials that are able to minimize the parasitic magnetic flux paths in the rotor and reduce saturation levels in the stator.

#### **IPM Machine Modeling**

This study relied on numerous, complex executions of lumped-parameter and finite element analysis (FEA) models where scripting subroutines were necessary for varying numerous parameters to arrive at designs with optimized performance. The results of the FEAs were used to improve the accuracy of the lumped parameter model results. The modeling effort first required that both the models and the modeling approach be verified by considering a machine with known performance characteristics. The only commercially available IPM machine filling this requirement was the traction motor used in the Toyota Prius. The 2004 Prius traction motor was used in this task as the "baseline case" motor. After many SPEEDCAD and Flux2D runs, the analysts were able to use FEA model results effectively in "fine-tuning" the lumped parameter model to account for magnetic saturation and other phenomena that were not fully captured.

Next, the IPM machine was scaled down in size to one that would operate at the target design specification speed of >10,000 rpm, and an FEA was used to evaluate mechanical stresses and retention of the PMs. Then the study used the adjusted lumped parameter model to simulate the

high-speed IPM machine at speeds ranging from 2,000 to 10,000 rpm. The high-speed IPM machine was shown to have an overall efficiency similar to that of the baseline case, and the overall performance is promising in that most performance targets were reached over much of the speed range. Although it is not a major concern, the results indicate that in the extended high-speed range, efficiency dropped to 90% at 8,000 rpm and 86% at 10,000 rpm. The analysis results also indicated high current levels, especially at low speeds; these data make a strong case for increasing the source voltage—to be pursued in the coming months.

The study will continue, using the modeling tools to analyze other selected alternative machines of high interest, including (1) IPM machines whose rotors contain layered magnets and (2) 12-pole PM machines featuring surface magnets with mechanical locking tabs for magnet retention (such as used in the Honda Fuel Cell Vehicle). The study also plans to explore the use of relatively weak, but less expensive, injected magnets in selected machine configurations.

### Non-IPM Designs

Because the FreedomCAR project retains a strong interest in alternative machine designs, lumped parameter modeling of the following PM machines was performed:

- four 18-pole, radial gap (with cost study),
- three 8-pole, radial gap (with cost study),
- one outer-rotor,
- one fractional-slot winding,
- one Honda-type (T-shaped PMs with tabs for retention), and
- one axial gap.

These machines were designed to have a base speed of 1500 rpm, a constant power speed ratio (CPSR) of 4, and a base power of 30 kW to reflect performance targets that were in effect earlier in the study when much of the work took place. Some type of field weakening was used in each design between 1500 and 6000 rpm.

Although a study with fully integrated lumped parameter/FEA analysis was not performed for these machines, as it was for the IPM, modeling has produced limited results for most of the listed machine types. The Honda-type machine with T-shaped PMs was also analyzed using an FEA to determine stresses in the PMs. Analyses will continue for assessing PM-retention rotor wraps and machine performance in general.

#### Cost Study

The cost estimation in this study assumes a bottom-up approach in a large-scale motor manufacturing facility with favorable and realistic economic conditions. The cost structure for a motor manufacturing facility was developed based on conversations held with appropriate manufacturers. Each motor is considered at the major component level, where it comprises *seven* main constituent elements. Motor component sizing information, obtained from parametric modeling runs, is used as essential input for the cost estimation.

Based on the cost analysis, the cost for the high-speed IPM machine is \$368, compared with \$404 for the baseline IPM machine. As expected, the cost of magnets dominates the overall motor material cost distribution. The magnet material prices vary widely in the market today, increasing the uncertainty of motor cost estimates.

Cost estimates were also generated for the surface-mounted, inner rotor machine. Attractive pricing resulted for the four 18-pole machines, ranging from \$240 to \$401.

# **1. INTRODUCTION**

The goal of this study is to analyze selected electric motor designs that presently show the greatest promise for use in hybrid electric vehicle (HEV) traction drive applications. Specifically, the application is for a single source of mechanical propulsion force in a fuel-cell-powered vehicle. It is referred to as a series hybrid vehicle (SHV) application, as opposed to a parallel hybrid vehicle that uses an electric motor to supplement power from a gasoline engine primarily during acceleration.

This interim report provides the results of analyses completed in June 2004. Much of the work described in this interim report has to do with verifying models, understanding model agreement/disagreement, baselining results relative to known machine performance specifications, and evaluating results at different machine speeds. This work is essential prior to evaluating other proposed machine designs for which performance data do not exist.

The following sections describe the work for the full parametric study that is scheduled to conclude in September 2004.

#### Scope of Work

In this project, Oak Ridge National Laboratory (ORNL) engineers will use a number of analytical models and supplemental calculations to characterize new electric machine designs with the performance characteristics best suited for automotive applications. Physics-based models, recently developed models capable of analyzing new and innovative permanent magnet (PM) machine designs, and finite element analysis (FEA) methods will be used extensively in the study to evaluate the electric machines. In parallel with this effort, a closely coordinated cost study will develop baseline cost estimates for the selected machine designs. In the end, the study will effectively reduce the uncertainties pertaining to selected machine designs to allow the program to progress to the eventual selection and commercialization of an SHV traction motor design.

ORNL will assess the overall results of the study and the program status to determine what additional technical studies, if any, are needed before making a recommendation of a prototype motor. This task will consider feasibility of IPM type machines meeting performance targets, impact of parametric variations, and positive and negative attributes of various machine types.

The primary focus of this work is the interior PM (IPM) machine. In IPM machines, the PMs are fully embedded (i.e., buried) in the rotor steel structure. The study will analyze IPM machines for various design variations, using lumped parameter models to identify they key design parameters. In parallel with the IPM machine design parametric study, but with a smaller scope, analysts will evaluate other motor types, specifically surface-mounted, inner-rotor, and outer-rotor PM machines.

The scope of the study will be limited to the motors themselves while remaining fully cognizant of the motor-inverter systems. Essential inverter characteristics/effects, such as phase advance

and types of electrical waveforms, will be carefully considered in exploring the full potential of the motor. A careful approach will be used in evaluating low-induction motor designs so that high machine performance is attained without high electrical stresses and losses in the inverter system.

This study will make use of the results of other electric-machine-related studies conducted by ORNL and other organizations during the last 10 years. Results from prior cooperative research and development agreements (CRADAs) and the automotive electric machine drive (AEMD) tasks will be reviewed and applied as appropriate as a technical foundation. ORNL will also use open literature and consultation with recognized national experts to provide additional insight into efforts that have recently been investigated by industry, universities, and other government laboratories.

### Methodology

ORNL will make efficient use of lumped-parameter models, primarily Scottish Power Electronics and Electric Drive Computer-Aided Design (SPEEDCAD<sup>TM</sup>), to initially explore ranges of machine geometry, size, and other parameters to determine optimal parameters and/or sets of parameters as indicated in Fig. 1.1. The process indicated in the three central blocks of the figure is repeated until it becomes evident that an optimal design has been achieved. The model will help in obtaining the optimal design by providing the analyst with the results of both static and dynamic design results. Scripting routines are used as essential tools for varying large numbers of machine design parameters to find optimal combinations for attaining the machine performance goals. The FEA iterations are performed generally toward the middle and end of the analysis.



Fig. 1.1. Machine design process diagram.

The analyses will provide estimates of performance and the magnetic field distribution within the electric machine. The low-speed torque and constant power range will be maximized and correlated with an analysis of current, supplied voltage, and back–electromagnetic force (emf). Inductance and torque variations according to rotor position will be assessed. Electrical circuit parameters will be determined for the electric machine being evaluated and optimization of parameters will be performed.

FEA methods will be used to derive a detailed model of the selected electric machines and to confirm and refine the selected designs. FEA methods will be used to evaluate flux density,

relative permeability, and isoflux mapping based on the size, shape, and type of PMs. The PM demagnetization curve will be determined and utilized in the FEA to calculate concentrations of magnetic flux density throughout the machine. Machine saturation effects, inductances, and torque variation according to rotor position will be determined.

The FEA will also evaluate detailed machine features, including the geometry and lamination stack length. The analyses will also consider stator winding layout, including coil pitch, interconnections, number of turns, etc. However, the greatest emphasis will be parameters pertaining to the rotor, which will be modeled rigorously. The designs will be assessed for any potential problems requiring resolution, and motor designs with attractive performance specifications will be determined.

A cost study will be prepared on the baseline IPM motor design and will include a trade-off study of machine cost vs. variations in selected design characteristics or operational limits. These variations include PM quality, laminate design, saturation limits, machine speed, machine diameter, and stack length. The analysis will then be repeated in lesser detail for the other machine configurations included in the study.

For a machine design to be considered commercially viable at low risk, some assurance is needed that reliability and cost goals for a given traction motor drive design are attainable. The electric motor's lifetime can be considered to be a function of the material used in the motor, such as the stator insulation, and the operational stresses imposed on the unit. Aging of insulation is normally viewed as a chemical process that occurs more rapidly at higher temperatures. Thus, the life of the machine can be increased by reducing the normal operating temperature of the stator and rotor by reducing losses, improving heat transfer, and minimizing any temperature excursions experienced by the machine. These considerations will be integrated into the study.

# 2. BACKGROUND

The U.S. Department of Energy (DOE) directed the AEMD task efforts over several years to improve technology in many critical areas in support of the HEV. ORNL and other AEMD technical development teams were contracted to conduct research on different machine designs, primarily in the 15–30 kW range, and their progress was assessed during quarterly DOE/Technical Team meetings. As part of the DOE-AEMD contracts, axial-gap PM motors, radial-gap PM motors with an outer-rotor configuration, and induction machine designs were explored (see Appendices A, B, and C). Electric machines were researched in analytical studies, experimental prototypes were constructed, and tests were conducted for both the series and parallel HEV applications.

Another important initiative was the Partnership for a New Generation of Vehicles (PNGV). PNGV's goal was to manufacture an affordable family car that attains 80 miles per gallon, with production of a prototype by 2004. However, in January 2002, Secretary Abraham announced that the FreedomCAR (CAR = Cooperative Automotive Research) initiative would take the place of the PNGV.

As the last of the AEMD tasks are completed, the ongoing HEV development effort is now largely supported under the FreedomCAR program, which is funded by DOE's FreedomCAR and Vehicle Technologies Office. FreedomCAR seeks to support research and development for *all* promising traction motor designs/configurations, in addition to supporting development in many related technology areas that are of crucial importance, including thermal management, power electronics, and system integration. The broader FreedomCAR program is also supporting research in associated areas such as fuel cells, hydrogen cost reduction, and hydrogen storage. Thus, FreedomCAR is an industry/government research initiative focused on collaborative, high-risk research to develop the component technologies necessary to provide a range of affordable vehicles that will free the United States from petroleum dependence and harmful emissions sources. The program intends to accomplish this without sacrificing freedom of either mobility or vehicle choice.

Several automotive original equipment manufacturers (OEM), that are members of FreedomCAR's Electrical and Electronics Technical Teams (EETTs), are recommending that analysts begin to narrow their focus to the development of IPM motors to meet FreedomCAR goals. This recommendation reflects the rapidly growing desire of the OEMs to select and commercialize a viable design in the near future. This OEM priority will be accommodated in the present study through a strong emphasis on the IPM while preserving serious consideration of other machine designs that merit continued interest in the program.

The FreedomCAR goals and specifications have been established to provide direction and guidance for the electric machine design goals set for this task. These design goals were subsequently reviewed and modified to meet the needs of both DOE and the EETTs. The specifications call for a 30-kW machine with >93% efficiency and a 15-year life, costing <\$7 per kW. The full set of specifications (Sect. 4.2) contain several operational conditions, limitations, and performance measures that present a medium or high degree of technical

challenge. Meeting the full set of specifications represents a very significant challenge, given current technology.

Priority has been assigned to certain characteristics of the electric machine based on guidance from DOE and the EETTs. For example, the cost and high-speed efficiency of the electric machine could be assigned priority. In this study, priority or emphasis will be placed on the analysis of IPM motor designs, in part because successful commercialization of this machine type has already been demonstrated successfully in the automotive industry.

# **3. ELECTRIC MACHINE TECHNOLOGY REVIEW**

There are several types and configurations of rotational electric machines to be considered in this study, each having specific strengths and weaknesses. It is anticipated that certain machine configurations will not be acceptable to the automotive industry because of their inability to meet specific requirements such as specific power at peak load, continuous power, volumetric power density, cost per kilowatt, efficiency, maximum weight, and lifetime. The estimation of programmatic risk relative to the commercialization of a given design is also of critical interest.

## **3.1 BRUSHLESS PM MACHINE**

Brushless PM machines are constructed with the electric winding on the stator and PMs on the rotor. There are several conventional PM machine configurations and other more novel concepts conceived in recent years to improve performance. The configuration of a PM machine and the relationship of the rotor to the stator determine the geometry and the shape of the rotating magnetic field. The shape of the back-emf is a fundamental characteristic. PM machines in which the magnetic flux travels in the radial direction are classified as radial-flux machines. They are cylindrical in shape, and the rotor is usually located inside the stator but can also be placed outside the stator. PM machines in which the magnetic flux travels in the rotor is usually located inside the stator but can also be placed outside the stator. PM machines. They can have multiple disk or pancake-shaped rotors and stators. The stator-rotor-stator configuration is typical. The shape of the back-emf of PM machines matches that of the driving currents and can be trapezoidal or sinusoidal. Although both kinds are brushless and synchronous, PM machines with trapezoidal back-emf are referred to as PM synchronous motors.

In general, PM machines have a higher efficiency as a result of the passive, PM-based field excitation. PM machines have the highest power density compared with other types of electric machines, which implies that they are lighter and occupy less space for a given power rating. The amount of magnet material that is required for a given power rating is a key cost consideration. The cost of magnet material is high compared with the cost of the other materials used in electric motors, and design attributes that minimize the required amount of magnet material are important considerations in motor selection. The stators of PM machines are generally fabricated in the same manner as induction machine stators; however, modifications are sometimes necessary, such as the design of a stator lamination to accommodate high flux density.

## **3.2 IPM MACHINE**

In contrast to surface-mounted PM machines, buried-magnet or IPM machines offer certain advantages, their suitability for high-speed operation being perhaps the most obvious. The fundamental difference is that in a surface-mounted rotor, the flux cannot be moved tangentially *within* the magnet to provide a rotor-to-stator phase advance, while in a buried-magnet rotor the flux *can* be moved tangentially above the magnets in the rotor iron so that a quite significant rotor-to-stator phase advance can result. The flux may be skewed to such a degree by the time it passes through the stator, areas of saturation may exist in pairs of adjacent teeth at each pole. In

favor of surface mounting, the presence of ferromagnetic material at the rotor surface increases the air gap inductance.

As a result of the rotor-to-stator phase shift, buried magnets add a reluctance component to the torque produced by the motor, which tends to improve the constant-power speed range. This avoids the power dropoff that is common in surface magnet PM machines operating at high speeds. IPM machines can provide torque under certain conditions with less I<sup>2</sup>R losses than other PM machines.

The saturation that may occur in the quadrature axis (q axis or interpolar axis, extending out radially from the interpolar space) of IPM machine stators is not all good. The saturation represents magnetic flux that is not used efficiently in producing torque. All forms of field weakening, regardless of the PM motor type, represent a loss in motor efficiency. However, the reluctance torque benefit in the IPM may be well worth this drawback.

IPMs facilitate the use of easily manufactured rectangular magnets or other convenient geometries. Yet another design consideration is that IPM machines with high-energy magnets can be designed to provide rapid acceleration because of their high torque/inertia ratio; this is why compact versions of IPMs are commonly used in servo systems.

Figure 3.1 shows conceptual depictions of IPM rotor configurations; Fig. 3.1 shows a version with straight or flat magnets, and Fig. 3.1b depicts magnets that have been split and oriented in a V-configuration. This second version can accomplish different objectives depending on the precise geometry. It might allow the use of slightly longer magnets within the same magnet arc. This would provide more magnetic flux for performance enhancement. A different configuration would place more rotor yoke iron between the magnets and the air gap and allow for different flux line paths in the yoke.



Fig 3.1. Two variations of an IPM machine rotor.

The SHV version of the IPM that will be considered in this study is more sophisticated than the depiction in Fig. 3.1 and is more accurately depicted in Fig. 3.2. Note that the machine has a high stator slot count and that the rotor magnets are positioned very close to the rotor-to-stator gap. This positioning and the air pockets at the ends of the magnets are necessary to reduce saturation that could otherwise be a serious path of flux leakage, as indicated in the sketch. The figure illustrates an issue with rotor mechanical integrity resulting from the fact that the magnets are held in place only by two narrow metal bridges located between the magnet air pocket and the air gap. This rotor mechanical integrity issue must be fully addressed to permit operation at the target high rotational speed (i.e., >10,000 rpm).



Fig. 3.2. View of the SHV IPM machine with key features.

To fully define and model an IPM machine suitable for the SHV, numerous parameters must be defined for each of several categories that include dimensions, windings control, thermal, and magnetics. Through modeling, the designer and analyst are able to identify which parameters are critical to machine performance and which have an effect on the machine performance that may not be intuitive. Inductance, maximum current, rated voltage, wire size, magnet size, and magnet arc are just a few examples of critical parameters that must be set consistent with the assigned values of other parameters. For more on critical machine parameters, see Sect. 4.3.

In IPM machines, the PMs are entirely encased in rotor cavities. This arrangement may lead one to conclude that the iron or laminated steel alloy provides good containment at high speeds. However, this is not necessarily the case. The magnets slice through the rotor in a sizable 2-dimensional plane that tends to result in a weaker rotor if corrective measures are not used. What rotor material is left provides limited structural integrity, since the material is a soft magnetic steel alloy or iron. High-speed rotor operation is still possible, but it must be designed for and verified using structural calculations (e.g., via an FEA). Rotor strengthening can be accomplished through the use of high-strength end rings, effective bonding in the magnet cavity, and/or the use of outer diameter (OD) rotor containment—either a high-strength metal can or a fiber-composite wrap. Most of these strengthening techniques increase the effective rotor-to-stator air gap and can adversely affect the machine performance.

### **3.3 SURFACE MOUNT PM MACHINE**

This section discusses the interior-rotor, surface-mount configuration of the PM machine and the exterior-rotor configuration of the same.

#### 3.3.1 Interior Rotor

The interior-rotor, surface-mount PM motor has as one of its most distinguishing characteristics a high torque/inertia ratio. The shaft torque increases proportionately with rotor length and with the square of the rotor diameter. The specific power and volumetric power density are also generally higher than in other non-PM machine types.

The stator of this machine is quite similar to that of an induction motor or synchronous motor. As with an induction motor, winding the stator is a difficult operation and is best performed using specialized, automated equipment. The stator yoke and rotor are generally made of laminations of magnetic steel, and the rotor laminations come from the hole pieces punched out of the stator laminations. Alternatively, the rotor yoke may be machined from a soft iron or low-carbon steel; however, eddy current losses will be higher than for a laminated rotor.

Figure 3.3 shows conceptually a number of different rotor designs that are used in surface-mount PM machines. Shown in Fig. 3.3a is a traditional rotor configuration where the surface magnets are curved both at the top and bottom. Four poles are shown, but several more poles can be added to the rotor and generally are added as the diameter of the rotor increases. Shown in Fig. 3.3b is the "bread loaf" design where the magnets are contoured on the top and flat on the bottom. The flat bottoms are more easily fabricated and bonded to the rotor yoke.

Shown in Fig. 3.3c is a substantial modification of (b) in which only half as many magnets are used. If the magnets have the same polarity, the design is called a consequence-pole rotor. The other two poles are nothing more than salient segments of the soft iron rotor yoke. Using only half the number of magnets reduces cost; however, the machine operates with a lower permeance coefficient. The double air gaps that the magnet flux must cross require a thicker magnet to avoid demagnetization. Additional poles may be added to the rotor design. If the two magnets in Fig. 3.3c were different poles, this configuration would represent a cross between a PM motor and a synchronous reluctance motor.<sup>1</sup>



Fig. 3.3. Examples of rotor and magnet configurations in surface-mounted PM machines.

The rotor configuration shown in Fig. 3.3d features a ring of magnet material bonded over the rotor yoke. The ring is magnetized after its placement on the rotor yoke. The mechanical integrity of the magnet is enhanced by the 1-piece ring construction.

The spoked, internal (but not buried) magnet configuration in Fig. 3.3e has the advantage of using bar magnets with no curved surfaces. Since the magnet surface area is considerably greater than the rotor surface area over which the magnet flux passes, flux concentration occurs.<sup>2</sup> This configuration is effective in getting improved performance from low-cost ferrite magnets.

The configuration in Fig. 3.3f shows curved surface magnets contained by a ring or shell. Although this design provides good magnet containment strength, the manufacturing cost of the magnets and rings may be somewhat higher. Effective and consistent containment requires a precise machined fit to tight tolerances.

The surface-mounted PM machine can be driven electrically by either trapezoidal or sinusoidal waveform. The position can be determined either by a sensor or by zero crossing, depending on the waveform. These electrical and control considerations can affect performance in terms of parameters such as torque density and torque pulsations.

As with the IPM machine, one of the most challenging design and manufacturing issues in producing an interior-rotor, surface-mount PM machine is magnet retention. Centrifugal forces

tend to limit the rotational speed of the machine. Failure to retain the magnets will almost certainly destroy both the rotor and the stator assemblies. Magnets are usually bonded to the rotor yoke in a process that is carefully controlled with regard to cleanliness, adhesive specifications, and curing.<sup>1</sup> Many designs use additional methods of containment, such as a tight-fitting steel shell over the rotor made of non-magnetic 300-series stainless steel or Inconel<sup>TM</sup> or wrapping of the rotor with an epoxy-impregnated, high-strength fiber.

### 3.3.2 Exterior Rotor

The HEV is a high-torque machine application at the low-speed range. Since torque increases with the square of machine diameter, the high torque requirement leads to diameter sizes that, in *internal* rotor machines, can present magnet containment design challenges during high-speed operation. However, the exterior-rotor, surface-mount PM motor offers unique advantages for medium- to-high speed applications. One of these is the outer shell construction of the rotor, which is well suited for containing and securing the surface magnets. Also, the high inertia of the rotor structure is very effective in reducing torque ripple. For these reasons, the external rotor machine continues to be of high interest for the SHV traction drive.

This is not to say that the exterior rotor machine does not have its disadvantages. The rotating outer shell may be helpful in some machine applications, but in the HEV, the rotating shell may pose a potential rotating hazard if it is not enclosed or covered with a shield. This is not a major disadvantage, especially in light of the modest machine length that would be required. It also is somewhat more difficult to provide a coolant flow path to the interior stator than to the exterior stator in the interior rotor machine.

## **3.4 INDUCTION MACHINE**

The induction motor has a long history of successful operation in industrial applications and has proved to be a rugged and reliable machine. Electric motor manufacturers have a great deal of knowledge and expertise in the design and fabrication of induction machines, which can be readily applied to a traction motor design. For the sizes of interest in the FreedomCAR project, the induction motor has been shown to have a lower efficiency and lower power or torque density than PM and reluctance motors (see Appendix B).

Although some promising cost-saving concepts have been investigated in recent years, there appears to be a dearth of new ideas for making substantial improvements to efficiency. Only small incremental improvements may be expected in the performance characteristics (i.e., efficiency, power density, etc.) of induction machines in the near future. Thus, high reliability and low technological risk will likely remain the primary advantages of this technology in the foreseeable future.

#### **3.5 SWITCHED RELUCTANCE MACHINE**

Reluctance machines are synchronous machines with certain unique features pertaining primarily to their doubly salient stator and rotor pole design. The machines are robust, use simple construction, and are suitable for high speeds. They include two types, switched and synchronous.

The *synchronous* reluctance motor is used in industry, where motors are required to operate in synchronism or where highly regulated speed control is required using a variable-frequency drive. The motors provide constant, unvarying (or highly controlled) speed from no load to full load with no slip.

The *switched* reluctance motor (SRM) is excited by current pulses applied to each phase. The current pulses are applied based on precise rotor position. The inductance profile is triangular, with maximum inductance when it is in an aligned position. When voltage is applied to the stator phase, the motor creates torque in the direction of increasing inductance.

Both synchronous and SRMs require a position sensor unless new, sensorless technology is employed. Position sensors are a source of increased cost and reduced reliability.

In reluctance machines, torque is produced by the tendency of the rotor to move to a position where the inductance of the excited stator winding is maximized (i.e., rotor tooth aligns with active stator phase to minimize reluctance). The rotor is typically constructed of soft magnetic iron shaped so as to maximize the variation of inductance with rotor position. Opposite poles form a phase and the phases are magnetically independent of one another. The machines tend to be noisy; a characteristic that has limited their applications in the past and has also limited their use currently in vehicles. Research has been on-going for years in an attempt to address the noise issue, but little has been accomplished in actual noise mitigation. Reluctance machines are relatively low-cost machines, and they generally do not contain PMs.

Novel electric machines are being developed that have attributes that are unique or that combine features of PM, induction, or reluctance machines. There are several novel electric machine concepts that are being investigated by government laboratories, universities, and industry.

# 4. IPM MACHINE DESIGN POTENTIAL

#### **4.1 DISCUSSION OF MACHINE DESIGN**

#### 4.1.1 Mechanical Design Issues

Electric motors are readily designed to provide specific torque and useful power; however, a crucial question for any motor design is its maximum speed capability. Estimates may be made using force balance equations and elastic equations for rotational systems axisymmetric about an axis. These techniques, which may be matched to estimate circumferential stress and radial interference requirements (radial stress), provide only a rough idea of the speed capabilities of a particular configuration. In each design, the magnets generate an equiangular load that adds bending stresses to the tensile stresses; consequently, a finite element code is needed to determine a more representative picture of the stresses and deformation of the components of the motor. ORNL has used ALGOR stress analysis to examine the mechanical capabilities of the IPM motors.

#### 4.1.1.1 Mechanical failure criteria

Since the rotor material is ductile, if failure is generated in the rotor, an excellent way to determine its maximum rotational speed is to adjust that speed so that the von Mises stress equals the rotor's yield strength. Yield strength is obtained from a uniaxial tensile test at the onset of plastic flow. Although one is tempted to use the ultimate strength, this is not wise because plastic flow allows the components to move, which may create imbalances that will lead to failure.

For ductile materials, experience has shown that the von Mises stress provides a dependable and non-conservative estimate of failure. This approach assumes that yield, which is the onset of plastic deformation, is caused by a critical shear stress on an octahedral plane. The normal to the octahedral planes have equal direction cosines with the three axes. The expression for octahedral shear stress is

$$\tau_{\rm oct} = \frac{1}{3} \sqrt{(\sigma_{\rm x} - \sigma_{\rm y})^2 + (\sigma_{\rm y} - \sigma_{\rm z})^2 + (\sigma_{\rm z} - \sigma_{\rm x})^2 + 6(\tau_{\rm xy}^2 + \tau_{\rm yz}^2 + \tau_{\rm zx}^2)}.$$
 (1)

where,

 $\sigma_i$  = stress in the direction indicated by the subscript

 $T_{ij}$  = shear stress on the plane perpendicular to the first subscript and in the direction indicated by the second subscript

In the uniaxial test, all components of stress except for  $\sigma_x$  are zero. The value of the critical octahedral shear stress may be obtained from the uniaxial test data by substituting  $\sigma_x = \sigma_{yield}$  in Eq. (1). The result is

$$\tau_{\rm oct} = \frac{\sqrt{2}}{3} \sigma_{\rm yield} \ . \tag{2}$$

When more complex loading occurs, for which terms in Eq. (1) are not zero, Eq. (1) may be set equal to Eq. (2). The result is that

$$\sigma_{\text{yield}} = \sqrt{\frac{(\sigma_{x} - \sigma_{y})^{2} + (\sigma_{y} - \sigma_{z})^{2} + (\sigma_{z} - \sigma_{x})^{2} + 6(\tau_{xy}^{2} + \tau_{yz}^{2} + \tau_{zx}^{2})}{2}},$$
(3)

where the term on the right of Eq. (3) is known as the von Mises stress or the effective stress.

Different failure modes may require different criteria to determine maximum operating speed. For example, if the failure mode is fracture of the magnets, which are brittle materials, the criteria for operation will necessitate a Weibull distribution of the magnet's transverse fracture strength. From this distribution, a maximum stress may be determined to achieve the required probability of fracture.<sup>3</sup>

#### 4.1.1.2 Mechanical operating speeds of IPM motors

The IPM machines are progressing through an evolution that significantly increases their speed capabilities. Three types of machines, two of which are already in the market, have been examined using the ALGOR finite element program. The two are the Toyota Prius THS motor (2003) and the Toyota Prius THS2 motor (2004). The third is being proposed by ORNL as a modification of the THS2 to deliver increased torque and power using the principles of the high-strength undiffused brushless (HSUB) motor.

The interior PMs move within cocoons of M19 steel during operation. To observe how they load the M19 with the finite element code, it is necessary to use gap elements, which come into play only when their initial dimension is reduced. Such a reduction indicates that the materials are trying to overlap. Although this is mathematically possible, it is realistically not permissible. To prevent this from happening, their stiffness normal to the surfaces is incorporated as part of the stiffness matrix. Since this is a non-linear calculation, the model in the configuration must be elastically stable when the first load increment is applied. This stability is provided by using a spring element so soft that it will not significantly impact the final solution. After each load increment, the gap elements are checked to see which ones have diminished; and one by one, those that have diminished are added to the stiffness matrix. The load along each active gap element is calculated. The load for inactive gap elements is zero.

In each IPM model, the load of the magnets and all of the material to the outer radius must be supported by the remaining spoke-like portions of the rotor. The significant mechanical contribution of the Toyota Prius THS motor is the use of two 1-mm-thick peripheral bridges of M19 silicon steel between the loaded region and the spokes to support each IPM. This magnet loading is shown in Fig. 4.1, in which it appears that the rotor interface between the magnet and the periphery bends, allowing the magnet load to be applied only at its outer edge. Because of symmetry, the total magnet load appears to be 240 lb. Figure 4.2 shows the onset of plastic deformation in the inner surface of the bridge near the spoke, indicating that the maximum operating speed is 5686 rpm.



Fig. 4.1. Magnet loading in the THS design.



Fig. 4.2. Onset of plastic deformation in the THS motor.

The impressive additional mechanical contribution of the THS2 motor is the addition of a ledge on the spoke side to carry a large part of the magnet load and relieve the load on the bridge. Figure 4.3 shows that the magnet load supported by the ledge on the spoke side of the cocoon is 102 lb. The result of this load redistribution is that the maximum operating speed prior to the onset of plastic deformation is increased by 10% to 6231 rpm. Figure 4.4 shows that the bridge is similar to that of the THS motor.



Fig. 4.3. Magnet load of the THS2 motor.



Fig. 4.4. Beginning of plastic deformation in the THS2 motor.

The third type of motor proposed by ORNL is the modified THS2 motor, which uses the ledge of the THS2 with the two magnets rotated into a radial orientation, adds an inner magnet to connect their inner corners, and employs a post or pile to provide additional support between each end of the inner magnet and the large region loaded by the magnets. Initial examination using the finite element approach indicated that the maximum operating speed prior to the onset of plastic deformation of the HSU configuration, using 1.2-mm bridges and 1.2-mm piles, is 9716 rpm. The magnet loading on the ledge is shown in Fig. 4.5, and the onset of plastic deformation at the inner pile is shown in Fig. 4.6.



Fig. 4.5. Magnet load on the ledge of the modified THS2.



Fig. 4.6. Onset of plastic deformation in the modified THS2.

#### 4.1.2 Thermal Design Issues

The full set of thermal requirements specified by the FreedomCAR program is listed in Table 4.1. The interpretation of these requirements is that a 10 L/min flow of coolant in the temperature range of -40 to +105 °C shall be sufficient to cool the machine under all operating conditions defined in the general specifications and during severe driving cycles.

| Thermal Requirement                                    | Specification |
|--|---------------|
| Coolant inlet temperature (°C)                         | -40 to 105    |
| Ambient (outside container) operating temperature (°C) | -40 to 105    |
| Flow rate of coolant (L/min)                           | 10            |
| Maximum coolant pressure drop (psi)                    | 2             |
| Maximum coolant inlet pressure (psi)                   | 20            |
| Storage temperature (°C)                               | -50 to +125   |

#### Table 4.1. Thermal requirements for the SHV motor

The machine design calls for a "dry" stator and rotor system and for the stator assembly to be encased in an aluminum housing with a built-in cooling jacket adjacent to the stator's outer surface.

#### **4.1.3 Electromagnetic Design Issues**

An electromagnetic design issue for the IPM is whether the selected design has a lower impedance than desirable. If the impedance is too low, the motor may deliver the required 30 kW mechanical power, but with higher-than-desirable current in the inverter. For instance, in terms of electrical power, the inverter may be supplying 50 kW inrush with 20 kW regenerative power in the motor.

#### **4.2 MACHINE SPECIFICATION**

The machine specifications have been under a rigorous and ongoing review by DOE and the EETT. During the last several months of this study, the specifications have been revised on multiple occasions. Changes during March 2004 included increasing the rotation speed (both base and maximum speed) specification, a motor life specification, and additional thermal specifications. Meeting the full set of specifications is a significant challenge that will require widening the present technology envelope.

Table 4.2 lists most of the requirements from the revised specification and the estimated relative degree of technical challenge that is anticipated in meeting each requirement. To meet all of the requirements will present a significant technical challenge. The high-challenge requirements are related to power density in terms of mass and volume, the maximum estimated motor cost, and thermal considerations that relate to the power density.

Other requirements that are not listed, such as the minimum motor inductance, have a direct effect on the design of the motor and inverter and will be managed within the bounds of the primary requirements (in the table) and appropriate technical considerations or "engineering judgment." The battery operating voltage may need to be set at the high end of the range or increased further to reduce the current required for a given power rating and/or to ensure adequate current (i.e., for overcoming back-emf during high-speed operation). This may have vehicle maintenance safety implications that will have to be fully addressed before any final design selection process. Priority has been assigned to certain characteristics of the electric

machine based on guidance from DOE and the EETTs. For example, the cost and high-speed efficiency of the electric machine are considered high priorities.

| Requirement                                     | Motor        | Degree of<br>challenge |
|---|--------------|------------------------|
| Specific power @ peak load (kW/kg)              | >1.2         | High                   |
| Volumetric power density (kW/l)                 | >5           | High                   |
| Cost per kW (\$)                                | <7           | High                   |
| Efficiency, 10–100% speed, 20% rated torque (%) | >93          | Medium                 |
| Peak power (kW)                                 | 55           | Low                    |
| Continuous power (kW)                           | 30           | Low                    |
| Maximum speed (rpm)                             | 10,000       | Medium                 |
| Back-emf at maximum speed, line-to-line (V)     | <600         | Medium                 |
| Battery operating voltage (Vdc)                 | 325(200-450) | Low                    |
| Maximum current at motor, rms (A)               | 400          | Low                    |
| Torque ripple (%)                               | 5            | Low                    |
| Coolant inlet temperature $(^{\circ}C)^{a}$     | -40 to 105   | High                   |
| Flow rate of coolant ( <i>l</i> /min)           | 10           | High                   |
| Life (years)                                    | 15           | Medium                 |

#### Table 4.2. Requirements for the SHV motor

<sup>*a*</sup> For the full set of thermal requirements, see Sect. 4.1.2.

Note: To meet all requirements simultaneously present significant technical challenges. For instance, obtaining maximum power at minimum battery voltage results in exceeding the maximum current limit.

# **5. IPM MACHINE PARAMETRIC STUDY**

This section considers the design and modeling of (1) variations of an 8-pole, 6000-rpm IPM machine and (2) a high-speed version of the same machine capable of operation at >10 Krpm. The analyses described in this section entailed numerous, complex modeling runs (i.e., lumped parameter and FEA) where scripting subroutines were necessary for varying numerous parameters to arrive at designs with optimized performance. The results of the FEAs were used to improve the accuracy of the lumped parameter model results.

In addition to the machine types modeled in this section, additional machine configurations that include a 3-magnet layered, 8-pole rotor design and a type of surface-mounted, 12-pole rotor design are planned for inclusion in the final report.

# **5.1 SIZING THE IPM MACHINE**

The overall sizing of the machine is of great importance in terms of performance, structural integrity, cost, and weight. This study first considered the geometry of a commercially produced IPM machine with known performance to serve as a baseline for the lumped parameter model and FEA model to ensure that the results were consistent and fully understood.

Once the baseline case was well established and the lumped parameter model was adjusted using the results (e.g., saturation levels) of the FEA, the study was able to proceed to other machine sizes and geometries. As indicated in the following sections, the overall scaling of the rotor was necessarily a predominant consideration in meeting the target performance goals.

The modeling of a commercially produced IPM machine early in the study was limited to the maximum specification speed of the motor, 5700 rpm. The power produced by the machine, and many other parameters were consistent with the target performance goals. Therefore, the main design change needed was to make the machine capable of attaining speeds of >10,000 rpm.

## **5.2 STATOR WINDING DESIGN**

For the baseline IPM machine, the stator design was "as found" in the commercially produced motor that was disassembled and inspected. The stator ID was reduced for the high-speed IPM design, consistent with the scaling down of the rotor as described in Sect. 5.3. The other dimensions of the stator were adjusted in order to manage tooth flux saturation and to accommodate the required current in the slots based on the results of lumped parameter and FEA modeling. The lamination stack length was also varied independently based on modeling.

## **5.3 ROTOR DESIGN ISSUES**

The rotor is the most critical design challenge for developing an IPM machine that will meet performance targets. The design must consider centrifugal forces and mechanical stresses early on, since it would make little sense to model numerous design cases when few or no rotor designs would hold together mechanically.

The IPM "V-magnet" rotor baseline design is taken from a commercially produced motor and, based on the precise dimensions, the stresses were determined for the rotor at 5400 rpm. One of

the first steps in scaling the IPM machine down in size to one that would operate at >10 Krpm was to design the rotor so that it would experience the same stresses at 10 Krpm as the baseline design at 5400 rpm. The greatest stresses in the rotor are in the bridges (i.e., a pair of thin strips of metal retaining the magnets and a triangular steel segment in the rotor structure).

First, considering the forces:

centrifugal force = 
$$M * \omega^2 * r$$
, (4)

where M is the mass prone to fly off the rotor, r is the radius of its center of mass, and  $\omega$  is the rotor's angular velocity. An expression for the mass is

$$M = F^* r^{2*} L av{5}$$

where F is a factor accounting for the product of densities and cross-sectional fractions, and L is the length of the rotor.

Considering the shear stresses at the rotor bridges,

average shear stress = centrifugal force / (bridge \* L) = 
$$F * \omega^2 * r^3$$
/bridge . (6)

In scaling down the rotor assembly as described, one can assume that the speed changes by a factor,  $k_{w}$ , and the cross-sectional dimensions by a factor,  $k_r$ ; then

The ratio NewStress/Stress = 
$$k_w^2 * k_r^3 / k_r = (k_w * k_r)^2$$
. (7)

Hence, if  $k_r = 1/k_w$  then there will be no change in the magnitude of the stress. For instance, for  $k_w = 10,000/6,000 = 10/6$ , a new value of  $k_r = 6/10 = 0.6$  will maintain the same level of stress. For this reason, the rotor assembly was scaled down by 0.6.

Aside from geometry, the rotor parameters such as magnet strength, steel type, and amount of back iron were determined based on modeling. The stator and machine stack length were optimized in the high-speed (i.e. scaled-down) machine, independently based on lumped parameter and FEA modeling.

#### **5.3.1 PM Considerations**

The PM industry has improved both the properties and cost-value ratio of PMs in the last 20 years through the development of improved metallurgy and material sources/suppliers. This section will review the properties of various types of PMs, including a discussion of demagnetization considerations.

#### 5.3.1.1 PM strength and other key properties

The various types of PMs include the following:

- Alnico—a family of magnets made from aluminum, nickel, and cobalt characterized by excellent temperature stability, high residual induction, and enough energy for a number of industrial and commercial applications.
- Ceramic—a hard, low-cost ferrite made of barium and strontium ferrite with excellent stability. Ceramic magnets tend to be brittle, hard, and resistant to corrosion.
- Ferrites—a softer (non-sintered) version of the ceramic magnet. Lowest-cost magnets.
- Samarium cobalt (Sm<sub>2</sub>Co<sub>17</sub>)—a rare-earth magnet with outstanding magnetic properties including high BHmax, excellent thermal stability, and excellent corrosion resistance. Samarium cobalt is formulated as SmCo<sub>5</sub> (1:5 material) and Sm<sub>2</sub>Co<sub>17</sub> (2:17 material). This magnet is well suited for applications demanding high magnetic strength in a high-temperature environment.
- Neodymium iron boron (NdFeB)—an advanced, rare-earth magnet that is the most powerful commercialized PM available. The sintered form provides the highest magnetic properties, but the bonded version can be made in more shapes and sizes. The sintered neodymium magnet ranges in strength from a BHmax of 28-50 mega-gauss-Oersted (MGOe).

Bonded magnets are combinations of magnetic powders and either thermo-elastomers or thermoplastic resins. These blended materials can be injection molded or compressed. Compressionbonded magnets have greater magnetic output but can be shaped into only simple geometries.

Neodymium magnets offer the best value in performance and cost; however, designers should be aware that this type of magnet is temperature-sensitive and susceptible to oxidation if not properly coated. The magnet is high in Br, Hc, and BHmax. Table 5.1 compares key properties of selected neodymium magnets and the most powerful samarium cobalt magnets. Neodymium magnets clearly have a potential for greater magnetic strengths but do not have the high-temperature capability of the samarium cobalt magnets. Depending on the specified grade, neodymium magnets may have a working temperature of up to 200°C and samarium cobalt magnets a working temperature of up to 375°C.

| Grade                                | BHmax   | Remanence, Br | Coercive force, Hc | Working    |
|--------------------------------------|---------|---------------|--------------------|------------|
|                                      | (MGOe)  | (kG,Tesla)    | (kOe)              | temp. (°C) |
| Neodymium mag                        | nets    |               |                    |            |
| N33                                  | 31–33   | 11.5, 1.15    | >10.5              | 80         |
| N33M                                 | 31–33   | 11.5, 1.15    | >10.5              | 100        |
| N33H                                 | 31–34   | 11.5, 1.15    | >10.5              | 120        |
| N33SH                                | 31–34   | 11.5, 1.15    | >10.6              | 150        |
| N30UH                                | 28-31   | 11.0, 1.10    | >10.2              | 180        |
| N30EH                                | 28-31   | 11.0, 1.10    | >10.2              | 200        |
| N45                                  | 43–46   | 13.5, 1.35    | >11                | 80         |
| N48                                  | 46–49   | 14, 1.40      | >10.5              | 80         |
| N50                                  | 47–51   | 14.2, 1.42    | >10.5              | 80         |
| N45M                                 | 43–46   | 13.5, 1.35    | >11                | 100        |
| N44H                                 | 42–45   | 13.3, 1.33    | >12.6              | 120        |
| Samarium cobalt                      | magnets |               |                    |            |
| Sm <sub>2</sub> Co <sub>17</sub> 28A | 28      | 10.9, 1.09    | 10                 | 300        |
| Sm <sub>2</sub> Co <sub>17</sub> 28B | 28      | 10.9, 1.09    | 10                 | 300        |
| Sm <sub>2</sub> Co <sub>17</sub> 28H | 28      | 10.9, 1.09    | 10                 | 300        |
| Sm <sub>2</sub> Co <sub>17</sub> 30A | 30      | 11, 1.10      | 10.2               | 300        |
| Sm <sub>2</sub> Co <sub>17</sub> 30B | 30      | 11.2, 1.12    | 10.2               | 300        |
| Sm <sub>2</sub> Co <sub>17</sub> 32  | 31      | 11.5, 1.15    | 10                 | 300        |

 Table 5.1. Comparison of selected neodymium and highest-performance
 samarium cobalt magnets [MMC Magnetics]

Source: MMC Magnetics, www.mmcmagnetics.com, Happague, NY.<sup>4</sup>

Other properties of interest are shown in Table 5.2 for general applications for neodymium and samarium cobalt magnets. Neodymium has twice the bending strength of samarium cobalt and also significantly high resistivity. Note that the thermal expansion of neodymium is roughly a third of what it is for samarium cobalt. For comparison, cast iron has a thermal expansion of  $10.6-13.5 \times 10^{-6}$ /°C, which is at least three times that of neodymium; and aluminum alloys have an even higher coefficient of  $22-24.1 \times 10^{-6}$ /°C, or nearly seven times that of neodymium.

| Table 5.2. Physical | properties of | neodymium and | samarium c | obalt magnets |
|---------------------|---------------|---------------|------------|---------------|
|---------------------|---------------|---------------|------------|---------------|

| Property  | NdFeB | Sm <sub>2</sub> Co <sub>17</sub> |
|---|-------|----------------------------------|
| Specific gravity                                    | 7.4   | 8.2                              |
| Resistivity, μΩ-cm                                  | 150   | 86                               |
| Thermal expansion coefficient, 10 <sup>-6</sup> /°C | 3.4   | 9                                |
| Saturation <i>H</i> , kA/m                          | >2400 | >3200                            |
| Temperature coefficient of <i>Br</i> , %/°C         | -0.1  | -0.025                           |
| Bending strength, kg/mm <sup>2</sup>                | 24    | 12.3                             |
| Compressive strength, kg/mm <sup>2</sup>            | 80    | 30–90                            |
#### 5.3.1.2 Orientation of PM flux

The orientation of flux from the IPM design with V-configuration of the PMs is generally as indicated in Fig. 5.1. This orientation was verified in an IPM motor mass produced for the automobile industry. This configuration is useful for concentrating magnetic strength within a limited magnetic arc at the rotor pole. The use of this configuration in conjunction with high-strength magnets represents a unique design. The flux orientation was modeled in the FEA consistent with Fig. 5.1.



Fig. 5.1. Magnet field orientation as defined in the Flux2D model.

### 5.3.2 Laminates

Motor applications in general industry use low-carbon laminated steel for the rotor and stator. Such steel typically has electrical losses of ~6.6 watt per kg. High-efficiency motors are built with high-grade silicon steel, which typically reduces hysteresis and eddy current losses by half, to only ~3.3 watts per kg. Reducing the lamination thickness in rotor and stator steel also lowers eddy current losses. Improved insulation between laminations, when applied with enhanced quality control, further reduces these losses.

The IPM design calls for laminations both in the stator and in the rotor. Because of the complex shapes involved, it is expected that stamping the shapes out of thin steel and stacking them is the most cost-effective manufacturing approach. This cost-effective approach will also be advantageous in reducing eddy currents in both structures.

Currents will be induced in any conductor when it is rotated in a magnetic field. The induced currents are perpendicular to the flux and result in the generation of waste heat. The induced currents in a stator or rotor are called eddy currents. Hysteresis represents the power expended in a magnetic material as the flux density varies cyclically, and it may be thought of conceptually as the "magnetic friction" of a material.

The eddy current losses and hysteresis losses are often combined and referred to as core or iron losses. These losses are a function of the magnetic flux density, which, for the IPM designs considered in this study, are expected to be relatively high and comparable to those in field-

wound motors. This level of loss is due to the high-strength magnets and the magnet geometry in the rotor. The change in core losses as the motor load level changes is generally negligible.

The losses, in watts, for eddy current and hysteresis effects can be calculated using the following equations [Perrine]:

$$Loss_{h} = \frac{0.1445 \ \beta B_{r} \ H \ (freq) \ W}{density} \quad , \tag{8}$$

$$Loss_{e} = \frac{0.4818 \,\alpha \, B_{m}^{2} \, (Lam)^{2} \, (freq)^{2} \, W}{(\varepsilon) \, density} \quad , \tag{9}$$

where

 $\beta$  = hysteresis loss factor,

 $B_r$  = residual induction, kilogauss,

 $B_m = \max$ . magnetic induction, kilogauss,

H = coercive force, oersteds,

*Lam* = lamination thickness, inches,

Freq = excitation frequency of the motor,

 $\alpha$  = anomalous loss factor,

 $\varepsilon$  = electrical resistivity, microohm-cm, and

W = lamination weight, pound.

The hysteresis equation, Eq. (8), shows that hysteresis losses increase with the excitation frequency. The eddy current losses, Eq. (9), are proportional to the square of the excitation frequency and the square of lamination thickness. To minimize eddy current losses, this equation shows the high importance of relying on thin laminations for motors that operate at high excitation frequencies, such as the IPM design considered in this study.

The anomalous loss factor,  $\alpha$ , shown in Eq. (9) is used to account for differences between the observed eddy current losses and those calculated from electrodynamic theory. The disparity is generally due to magnetic domain wall effects. The anomalous loss factor increases as core loss decreases or lamination thickness decreases.

#### **Materials**

Laminations are generally made from low-carbon lamination steels, electrical steels, or silicon steels. Terminology is not always used consistently for what are, in reality, *two* major classes of materials. Most electrical steels are cold-rolled, non-alloyed, and low in carbon. These may be referred to as cold-rolled motor lamination (CRML) steel or simply as lamination steel. ASTM standard A726 describes CRML steels as follows.

CRML steels differ from common carbon steel in that

1. Manganese and phosphorous are added to increase electrical resistivity.

- 2. Mill processes are designed to enhance grain growth to reduce hysteresis.
- 3. Annealing is often used to reduce core loss and alter permeability.

The types of CRML steel include

- 1. Type 1—Beginning with material with controlled chemical composition, the lamination stock is either (1) shipped full hard and annealed after stamping or (2) annealed by the mill and shipped without any guarantee of magnetic properties.
- 2. Type 2—Optimal magnetic properties are attained by controlling the chemical composition, annealing the material, and then performing a critical reduction on a temper mill. The magnetic properties are not guaranteed.
- 3. Type 2S—This is the same as Type 2, with an additional guarantee of magnetic properties.

The other major class of laminate material is silicon steel or electrical steel. This type of lamination material is about twice as expensive as CRML material. Silicon steel laminations can be either grain-oriented or grain-non-oriented (GNO). The silicon promotes crystal orientation in grain-oriented silicon steel, which is used primarily in power transformers. However, of greater interest to the present study are GNO silicon steels, in which the silicon not only increases the volume resistivity of steel to reduce eddy currents but also affects the grain structure to reduce hysteresis. GNO silicon steels are used in motors, generators, and lighting ballasts.

Silicon steels contain from  $\sim 0.5\%$  to 3.25% silicon. As the amount of silicon is increased, the core losses are reduced by increased resistivity; however, the permeability of the steel is reduced in the presence of strong magnetic fields. At low and medium inductions, permeability improves with increasing silicon content.

Small amounts of manganese and aluminum may also be added to the steel primarily for metallurgical reasons; however, they are also helpful in affecting the grain structure and reducing hysteresis losses. Carbon, sulfur, and other elements are undesirable impurities that are kept low, especially in the high-grade steels. The carbon content can be lowered by annealing. The overall quality of magnetic steels for a given grade has improved over the years as a result of the improved control of impurities. As the impurities are reduced, hysteresis is reduced because of a decreased resistance to domain wall motion.

GNO silicon steels are available with a variety of surface coatings. These include an inorganic finish with natural oxides, inorganic insulation formed by a varnish applied to the surface of the material, inorganic insulation formed by a chemical treatment applied to the material, and inorganic/organic insulation applied to the surface of the material (http://www.acesita.com.br/eng/index.html). The material is available in coils, strips, and sheets.

Additional considerations of material properties, manufacturing, metallurgical properties, and classifications by ASTM and the American Iron and Steel Institute (AISI) are available in a handbook by R. C. Perrine.<sup>5</sup>

### **5.4 BASELINE IPM MACHINE**

Much of the preliminary work described in this interim report relates to verifying models, understanding model agreement/disagreement, baselining results relative to known machine performance specifications, and evaluating results at different machine speeds. This work is essential before evaluating other proposed machine designs for which performance data do not exist.

The IPM machine has been produced commercially since 2000 in a vehicle traction application for the Toyota Prius, a parallel hybrid vehicle. The motor design was modified in 2004 to provide higher torque at low speeds.

This section describes the analysis of a commercially produced IPM machine for which certain types of performance specification data are available. Specifically, published specifications exist for the Toyota Prius traction motor, although there is a lack of data relative to electrical current demand and/or efficiency. Cost estimates for this IPM design are provided in Sect. 7.2.

#### 5.4.1 Lumped Parameter Data Set for Baseline Case

The basic geometry of the IPM baseline case is shown in Fig. 5.2. Many key dimensions are defined in the figure as angular, linear, arc, or radial dimensions. The rotor, which is typically defined as the laminations and magnet for an IPM machine, for the purposes of this study and the modeling also includes the outer ring of the shaft (not shown in Fig. 5.2) because the steel ring of the shaft acts as additional iron in the rotor assembly and carries some of the magnetic flux. The detailed portion of Fig. 5.2 shows the three dimensions that define the tips of the stator teeth and the width of the slot openings. The bridge, as depicted at the ends of the magnets, is a critical dimension that is intentionally made small to encourage magnetic saturation to limit PM flux losses.

Tables 5.3 and 5.4 list and numerically define many of the key dimensions and other miscellaneous parameters for the baseline IPM machine. Most of the listed dimensions can be found in Fig. 5.2 or are self-explanatory. These parameters match those that were used in both the lumped parameter model and the Flux2D model (where required by the model). Many other parameters were required by both models; this is especially true for the lumped parameter model. Definitions for the full set of parameters used in the lumped parameter model, exceeding 300 in number, can be found in Appendix D.



Fig. 5.2. IPM machine sketch with critical dimensions.

| Selected dimensional parameter     | Abbrev. | Value  |
|------------------------------------|---------|--------|
| Stator outside radius, mm          | Rad3    | 134.62 |
| Radial distance to end of slot, mm | Rad2    | 116.5  |
| Rotor outside radius, mm           | Rad1    | 80.19  |
| Shaft radius (minus ring), mm      | RadSH   | 50.46  |
| Lamination stack length, mm        | Lstk    | 83.57  |
| Magnet width, mm                   | MagWid  | 38.48  |
| Magnet thickness, mm               | LM      | 5.31   |
| Bridge width, mm                   | Bridge  | 1.45   |

Table 5.4. Additional key parameters of the baseline IPM machine

| Key Design Parameters     | Abbrev. | Low Speed | High Speed |
|---------------------------|---------|-----------|------------|
| Angular speed, rpm        | RPM     | 1040      | 5400       |
| Sinusoidal Voltage, V     | Vs      | 600       | 885        |
| Line current set point, A | ISP     | 155       | 55         |
| Gamma, deg                | gamma   | 44        | 46.5       |
| Turns in stator coil      | TC      | 9         | 9          |
| Layers in stator slots    | Layers  | 1         | 1          |
| Magnet strength, Tesla    | BrT     | 1.12      | 1.12       |

#### 5.4.2 Lumped Parameter Results for Baseline Case

The results obtained from SPEEDCAD for the parameters defined in Sect. 5.4.1 are summarized in Table 5.5. The table indicates that the machine, when operated at 1040 rpm, had an efficiency of 95.7% and produced 322 Nm of torque of which 60% was due to reluctance. This low-speed

data does not fully account for magnetic saturation as will be further discussed below. Then the machine operated at 5400 rpm, it had an efficiency of 96.8% and produced 59.2 Nm of torque of which 37% was due to reluctance. That the model indicates a higher percentage of reluctance torque at low speeds than at high speeds has become a topic of debate since, in the opinion of some motor experts, it goes against classical theory of PM motors. However, the IPM machine with a V-shaped magnet at each pole is not a classic PM motor configuration.

| Selected Parameter         | Abbrev. | Low Speed | High Speed |
|----------------------------|---------|-----------|------------|
| Total machine torque, Nm   | Torque  | 322       | 59.19      |
| Reluctance torque, Nm      | RelTorq | 191.9     | 21.86      |
| Mechanical power, W        | Pmech   | 35069     | 33473      |
| Efficiency, %              | Eff     | 95.72     | 96.8       |
| Peak current in winding, A | IWpk    | 149.3     | 46.31      |
| RMS current in winding, A  | IWrms   | 96.64     | 32.16      |

Table 5.5. Selected key results of the baseline IPM machine at 1040 rpm and 5400 rpm

In addition to the two data sets described, numerous other simulation cases were made using the lumped parameter model to characterize machine performance over the entire specification speed range. These data are presented in the next series of plots. Furthermore, subsequent to the results presented above, FEA results showing significant magnetic saturation below 1200 rpm were factored into the SPEEDCAD model. Therefore, the low-speed data presented in plots and in Table 5.6 will contain certain results with improved accuracy compared to the above 1040 rpm data.

Figure 5.3 shows the power, efficiency, and torque for the machine over the full speed range. A torque of approximately 300 Nm is constant at low speeds up to only 1000 rpm before dropping gradually with speed. The efficiency is quite high above ~1500 rpm, even exceeding 97%; however, saturation adversely affects efficiency at low speeds. Power is constant beginning at 1000 rpm.

Figure 5.4 shows the line current (peak, average, and rms) considering only a single phase vs. speed for the IPM machine. The high current at low speeds results in significant levels of magnet saturation in the stator teeth. Figure 5.5 is a plot of the source voltage and current limit setpoint (ISP) for the machine vs. speed. The last plot, Fig. 5.6, shows the reluctance torque percentage of total torque vs. speed and heat flux vs. speed. These data and other related data are summarized in Table 5.6.



Fig. 5.3. Power, efficiency, and torque vs. machine speed for the full-size IPM.



Fig. 5.4. Stator current vs. machine speed for the full-size IPM.



Fig. 5.5. Source voltage and ISP vs. machine speed for the full-size IPM.



Fig. 5.6. Reluctance torque and heat flux vs. speed for the full-size IPM.

| Speed<br>(RPM) | Vs (V) | ISP (A) | Torque<br>(Nm) | Power<br>(kW) | Efficiency<br>(%) | Stator<br>current<br>(A rms) | Stator<br>current<br>(A peak) | Jrms<br>(A/mm <sup>2</sup> ) | Torque:<br>reluctance/total<br>(%) | Gamma<br>advance<br>(deg) | HeatFlux<br>(kW/m <sup>2</sup> ) |
|----------------|--------|---------|----------------|---------------|-------------------|------------------------------|-------------------------------|------------------------------|------------------------------------|---------------------------|----------------------------------|
| 520            | 600    | 283     | 298            | 16.2          | 71.4              | 200                          | 284.8                         | 23.5                         | 53.5                               | 33                        | 32.9                             |
| 1040           | 600    | 283     | 296.7          | 32.3          | 84.1              | 193.4                        | 283.2                         | 22.8                         | 52.6                               | 33                        | 31.1                             |
| 1100           | 600    | 233     | 281.5          | 32.4          | 88.4              | 160.8                        | 233.7                         | 18.9                         | 55.4                               | 33                        | 21.6                             |
| 1200           | 600    | 137     | 257.4          | 32.3          | 95.6              | 94.3                         | 137                           | 11.1                         | 55.9                               | 33                        | 7.6                              |
| 1300           | 650    | 114     | 239.9          | 32.7          | 96.8              | 78.8                         | 114.4                         | 9.3                          | 54.2                               | 33                        | 5.5                              |
| 1500           | 700    | 103     | 205.1          | 32.2          | 97.2              | 72.1                         | 103.7                         | 8.5                          | 51.9                               | 33                        | 4.8                              |
| 2000           | 885    | 86      | 155.8          | 32.6          | 97.7              | 59.7                         | 87                            | 7                            | 47.2                               | 33                        | 3.9                              |
| 3000           | 885    | 65      | 102.2          | 32.1          | 98                | 44.6                         | 65.2                          | 5.25                         | 40.1                               | 33                        | 3.4                              |
| 4000           | 885    | 55      | 78             | 32.7          | 97.7              | 36.4                         | 51.8                          | 4.3                          | 35.6                               | 33.6                      | 3.9                              |
| 5400           | 885    | 55      | 57.5           | 32.5          | 96.7              | 31.3                         | 45.8                          | 3.7                          | 34.7                               | 46.5                      | 5.7                              |

Table 5.6. SPEEDCAD characterization of a full-size IPM design for numerous key parameters over a speed range from 520 to 5400 rpm

### 5.4.3 FEA Modeling and Results for Baseline Case

The first goal of the FEA modeling task was to model the same IPM machine for which the lumped parameter model had produced results to determine how well the two models agree and to resolve differences. The resolving of differences can include different activities, including (1) making double checks and identifying errors, (2) assessing phenomena that the lumped parameter model either does not account for or does not thoroughly account for, and/or (3) taking the results of the FEA to fine-tune the lumped parameter model. This last activity generally amounts to telling the lumped parameter model how badly the permeability of the steel is being affected by saturation and helping the lumped parameter model account for other losses. Once this is accomplished, the lumped parameter model can be used with greater confidence to quickly evaluate other similar motor designs.

The first step in preparing the FEA is do develop the machine model to accurately reflect the proposed machine in terms of geometry, materials, magnet properties, and electrical current in the stator slots. Once the geometry is precisely defined, it is meshed as shown in Fig. 5.7 to permit the integration calculations of the elements. As indicated in the figure, the mesh is very fine at locations such as the rotor bridge and near the air gap where precision is necessary.



Fig. 5.7. Mesh of elements reflecting an emphasis on precision at critical machine areas.

After the problem is fully defined, the FEA is solved using either a static or dynamic solving process. Although parameters such as the total torque come out the same using either process, the dynamic model can be solved with an electrical circuit model to provide additional information regarding waveforms, back-emf, and torque fluctuations with time. The static model is less cumbersome to use and provides useful parameters such as flux density, permeability, flux maps of the geometry, and torque relative to the rotor position.

Modeling the same commercially produced IPM machine that SPEEDCAD modeled as described in Sect. 5.4.2, results were obtained showing the total torque the machine was capable of producing. Figure 5.8 shows the torque fluctuating over time based on a dynamic FEA and the

corresponding circuit-driven stator current waveform to give an additional sense of time. The fluctuation is due to reluctance torque and possibly also cogging torque. (The plotted torque values are negative merely because of the selected direction of rotation.) The model used a current-driven circuit with 313 A peak in each phase line and a 1040 rpm rotor speed to generate the fluctuating peak torque. The calculated average of the depicted waveform is 40.28 Nm. Since the torque is for one segment of the rotor, the total machine peak torque is eight times that amount or 322.2 Nm.



Fig. 5.8. Torque and stator current over time with baseline machine operating at 1040 rpm.

The model assumes that 313 A can be applied to the stator windings. This is not expected to be a major problem for the 1-turn coils in the stator; however, the inverter requirements must be assessed carefully.

Figure 5.9 shows the torque fluctuating over time based on a dynamic FEA and the corresponding current waveform. In this case, the rotor speed was increased to 5400 rpm. A peak current of 45 A in each phase line is required to generate the fluctuating peak torque that matches what was developed in the lumped parameter model. The calculated average of the depicted waveform is 7.9 Nm, and the average of the whole machine is 63.2 Nm peak. The model assumes that 45 A can be fed to the stator windings.

Once the developed torque was compared for the two types of machine models, the FEA model was used to explore other potential issues such as saturation in the rotor and stator steels. Figure 5.10 shows the flux density mapping of a portion of the machine geometry. In order to better highlight areas of severe saturation, the maximum flux density was set at 2 Tesla, which caused areas with flux density above 2 Tesla to be depicted as white. Although the flux density map changes as the rotor is turned, severe saturation was generally observed at or near the two bridge areas and at a corner of a stator tooth, as indicated in the figure. Of course, saturation at the bridges is highly desirable.

Flux density maps such as this will be generated for other candidate machines, and comparisons will be made to aid in determining when undesired or unacceptable saturation is occurring in stator teeth or in rotor or stator back iron.

In the evaluation of magnetic saturation, Fig. 5.11 was generated to assess the flux density in the stator across an arc-shaped path that cuts through five stator teeth and parts of two other teeth. At the top of the figure, the relatively large number of isoflux lines passing through stator slot #1 suggests that, in at least some portion of the tooth, the flux density is likely high. In the #1 stator tooth, the flux density plot shows a flux density peak that is flat-topped and is reaching flux densities of up to 1.8 Tesla. This value exceeds the saturation level of the steel, which, for this particular modeling run, was selected at a very high value of 1.7 Tesla. The right-hand plot in the figure shows that the relative permeability of the steel has dropped to near zero in slot #1 as a result of the saturation condition that exists. The figure makes it clear that saturation cannot be avoided even through the use of expensive lamination steel.



Fig. 5.9. Torque and stator current over time with baseline machine operating at 5400 rpm.



Fig. 5.10. Flux density color-coded map of rotor sector and portion of stator with a 2 Tesla ceiling.



Fig. 5.11. Flux density and relative permeability over a pre-defined path across stator teeth.

The PM flux loss across the bridge paths is significant in spite of saturation of the path; therefore, an FEA was used to generate an estimate of these losses. Figure 5.12 shows six paths that were defined in the FEA and the integration of flux over each path length. The bridge on the left seems to receive >36% of the flux produced by the adjacent magnet, and the bridge on the right, >40% of the flux produced by its adjacent magnet. These preliminary results are higher than expected and will be studied further in other machine configurations. It is essential to understand how the flux from the stator might affect the results obtained over the four short paths. Additional FEA runs are planned where the stator current is set to zero.



Fig. 5.12. Results of FEA analysis to determine the fraction of magnetic flux strength that is lost across the narrow bridge paths.

# 5.5 HIGH-SPEED IPM MACHINE

This section describes the lumped parameter modeling of an IPM machine similar to the baseline case except that it is scaled down to accommodate higher-speed operation. The rotor and shaft was scaled by 0.6 to maintain the same stresses at 10,000 rpm as the baseline machine experienced at 5700 rpm. The stator was scaled down to a lesser extent in order to manage tooth flux saturation and to accommodate the required current in the slots. The lamination stack length was also varied independently. Cost estimates for this IPM design are provided in Sect. 7.2.

### 5.5.1 Lumped Parameter Data Set for IPM

Tables 5.7 and 5.8 list and numerically define many of the key dimensions and other miscellaneous parameters for the high-speed IPM machine. The parameters match those that were used in both the lumped parameter model and the Flux2D model (where required by the model). Many other parameters not listed were required by both models, and this is especially true for the lumped parameter model. Definitions for the full set of parameters used in the lumped parameter model, exceeding 300 in number, can be found in Appendix D.

| Selected dimensional parameter     | Abbrev. | Value |
|------------------------------------|---------|-------|
| Stator outside radius, mm          | Rad3    | 102   |
| Radial distance to end of slot, mm | Rad2    | 84.85 |
| Rotor outside radius, mm           | Rad1    | 48    |
| Shaft radius (minus ring), mm      | RadSH   | 30    |
| Lamination stack length, mm        | Lstk    | 200   |
| Magnet width, mm                   | MagWid  | 23    |
| Magnet thickness, mm               | LM      | 4.02  |
| Bridge width, mm                   | Bridge  | 0.660 |
|                                    |         |       |

 Table 5.7. Selected key dimensions of the high-speed IPM machine

| Table 5.8.  | Additional key  | parameters | of the | high-speed | IPM 1 | machine  |
|-------------|-----------------|------------|--------|------------|-------|----------|
| 1 4010 0101 | riadicional neg | parameters | or the | mgn spece  |       | inacimic |

| Key design parameters  | Abbrev. | Low speed | High speed |
|------------------------|---------|-----------|------------|
| Angular speed, rpm     | RPM     | 2000      | 10,000     |
| Sinusoidal voltage, V  | Vs      | 200       |            |
| Current set point, A   | ISP     | 1710      |            |
| Gamma, deg             | gamma   | 32.7      |            |
| Turns in stator coil   | TC      | 1         | 1          |
| Layers in stator slots | Layers  | 1         | 1          |
| Magnet strength, Tesla | BrT     | 1.12      | 1.12       |

### 5.5.2 Lumped Parameter Results for IPM

The results obtained from SPEEDCAD for the parameters defined in Sect. 5.5.1 are summarized in Table 5.9. The table indicates that when operated at 2000 rpm, the machine had an efficiency of 88.9% and produced 254.8 Nm of torque, of which 50% was due to reluctance. When the machine operated at 10,000 rpm, it had an efficiency of 85.9% and produced 31.1 Nm of torque, of which 23.9% was due to reluctance. As with the baseline IPM design, the model indicates a higher percentage of reluctance torque at low speeds than at high speeds. The table suggests a worse efficiency than was the case over much of the speed range. As will be seen in the data plots and summary that follow, the machine efficiency is well above 93% for various intermediate machine speeds.

| Selected parameter         | Abbrev. | Low speed | High speed |
|----------------------------|---------|-----------|------------|
| Total machine torque, Nm   | Torque  | 254.8     | 31.1       |
| Reluctance torque, Nm      | RelTorq | 126.4     | 7.43       |
| Mechanical power, W        | Pmech   | 53355     | 32500      |
| Efficiency, %              | Eff     | 88.9      | 85.9       |
| Peak current in winding, A | IWpk    | 1735      | 231.2      |
| RMS current in winding, A  | IWrms   | 1196      | 141.1      |

| Tabla 5 0   | Selected | regults of | the | high_sneed | IDM | maching at | 2000 m | hne ma | 10K 1 | ·nm |
|-------------|----------|------------|-----|------------|-----|------------|--------|--------|-------|-----|
| 1 able 5.9. | Selected | results of | une | mgn-speeu  |     | machine at | 2000 r | pm and | 101/1 | .pm |

In addition to the two data sets described, numerous other simulation cases were made using the lumped parameter model to characterize machine performance over the expanded speed range of the high-speed IPM machine. These data are presented in the next series of plots and summarized in Table 5.10.

Figure 5.13 shows the power, efficiency, and rms current for the machine over the expanded speed range from 1,000 to 10,000 rpm. The efficiency is quite high above ~2000 rpm, even exceeding 96%; however, saturation adversely affects efficiency at low speeds where the current can be potentially very high (~1200 A during a 55-kW peak power surge). The available power level is constant beginning at just over 1000 rpm unless there is a peak power demand near the 2000 rpm base speed.



Fig. 5.13. Power, efficiency, and current vs. speed for high-speed IPM machine.

| Speed<br>(RPM) | Vs (V) | ISP (A) | Torque<br>(Nm) | Power<br>(kW) | Efficiency<br>(%) | Stator<br>current<br>(A rms) | Stator<br>current<br>(A peak) | Jrms<br>(A/mm <sup>2</sup> ) | Torque:<br>reluctance/total<br>(%) | Gamma<br>advance<br>(deg) | Heat flux<br>(kW/m <sup>2</sup> ) |
|----------------|--------|---------|----------------|---------------|-------------------|------------------------------|-------------------------------|------------------------------|------------------------------------|---------------------------|-----------------------------------|
| 1000           | 200    | 1710    | 261.7          | 27.4          | 81.1              | 1200.1                       | 1765                          | 24.3                         | 49.9                               | 32                        | 49.6                              |
| 2000           | 200    | 1710    | 266.2          | 55.7          | 89.6              | 1203.7                       | 1742.1                        | 24.3                         | 50.4                               | 32.7                      | 50.2                              |
| 2000           | 200    | 590     | 153.3          | 32.1          | 96.4              | 505                          | 599.3                         | 8.2                          | 46                                 | 32                        | 9.4                               |
| 3000           | 200    | 450     | 103.1          | 32.4          | 96.6              | 306                          | 461                           | 6.2                          | 39.1                               | 32                        | 9                                 |
| 4000           | 200    | 378     | 78.1           | 32.7          | 95.8              | 250.3                        | 282.3                         | 5.1                          | 34.3                               | 32                        | 11.1                              |
| 6000           | 200    | 310     | 51.7           | 32.5          | 93.2              | 185.2                        | 308.6                         | 3.7                          | 27.6                               | 32                        | 18.3                              |
| 8000           | 200    | 252     | 38.7           | 32.4          | 90.2              | 150.3                        | 228.8                         | 3                            | 24                                 | 33                        | 27.1                              |
| 10000          | 200    | 360     | 31.1           | 32.5          | 85.9              | 141.1                        | 231.2                         | 2.9                          | 23.9                               | 43                        | 41.3                              |

Table 5.10. SPEEDCAD characterization of a high-speed IPM design for key parameters over a speed range from 1000 to 10K rpm

Figure 5.14 shows the plot of torque, reluctance torque, and the ratio of the two vs. speed. Clearly, the machine is designed to deliver high reluctance torque at low speeds where the greatest torque demand exists.



Fig. 5.14. Torque, reluctance torque, and torque ratio for high-speed IPM machine.

Figure 5.15 shows plots of line current (rms and peak) and the heat flux vs. speed. Current can rise to very high values when the machine supplies short-duration 55 kW peak power at or near the 2000 rpm base speed. The heat flux drops below 20 kW/m<sup>2</sup>, but only in the limited intermediate speed range from 2000 ~6200 rpm. At low speeds, heat flux is high due to ohmic losses especially during a peak power surge, and heat flux increases with speed as a result of high-frequency iron losses.

Figure 5.16 is a plot of dc voltage and the line ISP vs. speed to show how the voltage was fixed while the ISP was varied from a very high value of 1710 A to a level as low as ~250 A near 8000 rpm.

Table 5.10 summarizes the data presented in Figs. 5.13–5.16 and other related data including the gamma advance (i.e., electrical advance) of the field relative to the rotor position.



Fig. 5.15. Line current and heat flux for high-speed IPM machine.



Fig. 5.16. Vdc and line ISP for high-speed IPM machine.

# 5.5.3 FEA Modeling and Results for High-Speed IPM

Will be provided in final report.

# 5.6 FIELD WEAKENING CONSIDERATIONS

Will be provided in final report.

# 6. ROTATING ELECTRIC MACHINES WITH SURFACE-MOUNTED MAGNETS

At the beginning of this study, the target design specifications were those shown in Table 6.1. A desired speed was not included in this specification; however, considering the capabilities of the Toyota Prius motor, it was decided to design the machines as described in this section to have a base speed of 1500 rpm, a constant power speed ratio (CPSR) of 4, and a base power of 30 kW. Such a machine would be capable of short 55-kW bursts. During peak power bursts, the inverter current is not to exceed 300 A rms. Between 1500 and 6000 rpm, there must be some type of field weakening.

| Requirement                                     | Inverter     | Motor        | Integrated<br>system |
|---|--------------|--------------|----------------------|
| Specific power @ peak load (kW/kg)              | >12          | >1.3         | >1.2                 |
| Volumetric power density (kW/l)                 | >12          | >5           | >3.4                 |
| Cost per kW                                     | <\$5         | <\$7         | <\$12                |
| Efficiency, 10–100% speed, 20% rated torque (%) | >97          | >93          | >90                  |
| Peak power (kW)                                 | 55           | 55           | 55                   |
| Continuous power (kW)                           | 30           | 30           | 30                   |
| Battery operating voltage (V <sub>dc</sub> )    | 325(200-450) | 325(200-450) | 325(200-450)         |
| Maximum current, rms (A)                        | 300          | 300          | 300                  |
| Torque ripple (%)                               | NA           | 5            | 5                    |
| Coolant inlet temperature                       | 105          | 105          | 105                  |

#### Table 6.1. Old target design specification for power electronics and electric machines

# 6.1. ROTOR MAGNET CONTAINMENT

As the base speed increases, magnet containment becomes a critical problem. For a machine with surface-mounted magnets operating as a brushless direct current motor (BDCM) with trapezoidal back-emf, there are four options:

- 1. Wrap the magnets with a suitable B-stage prepreg glass tape.
- 2. Encase the rotor in a non-magnetic can.
- 3. Use an "inside-outside configuration" in which the stator is inside the structure containing the magnets and rotor laminations. The centrifugal forces on the magnets are then restrained by this structure.
- 4. Use an axial gap configuration. In this arrangement, the stator and rotor are in the shape of a toroid. The armature current is in the radial direction and the magnets are charged in the axial direction. The air gap is in the axial direction and the centrifugal force on the magnets is in the radial direction. Thus a restraining ring can be used that does not impact the air gap volume.

Two control methods have been developed to drive a BDCM with surface-mounted magnets. The first method, conventional phase advance (CPA), was developed by UQM Technologies.<sup>6</sup> This method uses a conventional voltage source inverter to drive the motor. The second method is dual mode inverter control (DMIC), developed by ORNL.<sup>7</sup> A condensation of its basic operation is included in Appendix E. The success of either of these two methods is highly dependent upon the value of the machine inductance; the required values are summarized in Table 6.2.

| Mode    | L <sub>max</sub>   | L <sub>min</sub>   | Comments  |
|---------|--|--|---|
| DMIC    | $\pi \operatorname{sqrt}(91/1215) \operatorname{E}_{b}/\Omega_{b} I_{r}$ | $\pi \operatorname{sqrt}(1620) \operatorname{E}_{b}/\Omega_{b} \operatorname{I}_{rms}$ |   |
| CPA     | $36V_{dc}E_b//\pi 3\Omega_bP_r$  | $sqrt(2V_{dc}2/CPSR + 72E_b2/\pi 2-$   | $L_{\infty} = 8.485 \ E_b / \pi 2 \Omega_b I_{rms}$ |
|         |  | $24E_bV_{dc}/\pi CPSR)/\pi\Omega_bI_{rms}$   |   |
| Link    | $V_{dc} = 2E_b + 1.489\Omega_b LI_{rms} / \pi 2 + 2.5$                   | 236RI <sub>rms</sub>   | L <l<sub>max of the DMIC</l<sub>                    |
| Voltage |  |  |   |

Table 6.2. Limiting values of inductance for BDCM operation

A machine with surface-mounted magnets can also have a sinusoidal back-emf; this is referred to as a PM synchronous motor. Two options are available to control such a machine:

- 1. Design the motor with the inductance within the range shown in Table 6.2.
- 2. Design a structure as in the Honda motor<sup>3</sup> to contain the magnets. In the Honda motor, this structure also contributes reluctance torque.

Late in this study, the AEMD specifications of Sect. 4.3 were introduced. It was decided to continue as before but to emphasize the parameters that would limit the operation at the AEMD levels. Designs that showed promise would then be analyzed for mechanical and thermal limitations at a later date. Eleven configurations have been analyzed, using both software developed by the Power Electronics and Electric Machinery Research Center (PEEMRC) and T. J. E. Miller's SPEEDCAD software. Their parameters are shown in Table 6.3. All cases have three phases and an air gap of 60 mils to facilitate the use of prepreg glass tape wrap or metal cans for magnet containment. Case 9 has been designed to meet the AEMD specifications, excluding thermal and mechanical requirements that will be taken up in the next phase of this study. Case 11 is based on the latest Honda design. These cases are now discussed in the body of this chapter.

# **6.2 DESIGN CASES**

As seen in Table 6.3, there are four radial-gap, 18-pole design cases (1, 2, 3 and 4) with the rotor interior to the stator. The difference between these is in the turns per coil and the stack length. There are three 8-pole inside-rotor designs (5, 6, and 10). The difference between these is in the number of turns per coil. Case 7 is an axial gap design using the ORNL Bailey module, which employs two stators with the rotor between them. Case 8 is an "inside-outside" design where the stator is interior to the rotor. Case 9 is a fractional-slot winding, and case 11 is a Honda type design.

| Case | Rso* | Rro** | Rotor   | Mode | Slots/pole per | Poles | Turns/coil | Length |
|------|------|-------|---------|------|----------------|-------|------------|--------|
|      | (in) | (in)  |         |      | phase          |       |            | (in)   |
| 1    | 5    | 3     | inside  | BDCM | 1              | 18    | 8          | 1.969  |
| 2    | 5    | 3     | inside  | BDCM | 1              | 18    | 4          | 1.969  |
| 3    | 5    | 3     | inside  | BDCM | 1              | 18    | 4          | 3.938  |
| 4    | 5    | 3     | inside  | BDCM | 1              | 18    | 2          | 3.938  |
| 5    | 6.5  | 3     | inside  | BDCM | 1              | 8     | 8          | 3.938  |
| 6    | 6.5  | 3     | inside  | BDCM | 1              | 8     | 4          | 3.938  |
| 7    | 5.3  | 4     | Axial   | BDCM | 1              | 18    | 6          | 5      |
|      |      |       | gap     |      |                |       |            |        |
| 8    | 5    | 4     | outside | BDCM | 1              | 18    | 2          | 4      |
| 9    | 6.5  | 3     | inside  | PMSM | 0.5            | 10    | 8          | 1.969  |
| 10   | 6.5  | 3     | inside  | BDCM | 1              | 8     | 2          | 3.938  |
| 11   |      |       | Salient | PMSM |                |       |            |        |

 Table 6.3. Case parameters for cost study

\*Rso = outer radius of stator.

\*\* Rro = outer radius of rotor.

The discussions evaluating these designs will proceed as follows:

- 1. Cases 1, 2, 3, 4, 5, 6, and 10 are part of a cost study discussed in Sect. 7, where pole count and stack length are varied. Interesting design features are discussed in Sect. 6.2.2.
- 2. In the final report (due in September 2004), a mechanical study of the magnet containment capabilities of metallic cans and B-stage glass tape placed over the magnets will be presented.
- 3. Section 6.3 presents the design of a surface-mounted PM motor with an external rotor. A mechanical study of this "inside-out" rotor, case 8, will be presented in the final report.
- 4. The PEEMRC has developed an axial gap motor to be used with the DMIC. It has been driven to 6600 rpm with the dynamometer to ensure its mechanical integrity and is in the PEEMRC Test Cell 1 for measurement of torque, power, and efficiency as a function of speed. A similar motor designed for this study is discussed in Sect. 6.4. FEA and performance test results will be presented in the final report.
- 5. The PEEMRC is exploring a radial gap motor with self-supporting, surface-mounted magnets in the shape of an inverted wide "T". The magnets are separated by several millimeters of rotor, as in the Honda motor, giving rise to saliency. Its design will be discussed in Sect. 6.5.
- 6. Since inductance plays a critical role, a fractional-slot design is presented in Sect. 6.6.

### 6.2.2 Design Study of Cases 1, 2, 3, 4, 5, 6, and 10

The performance parameters of these cases are summarized in Table 6.4. The first four cases have 18 poles and the next three have 8 poles. Their stack lengths have a value of either 1.969 or 3.938 inches. The turns per coil of the 18-pole motors are varied as 8, 4, 4 and 2. The stack length of the 8-pole design remains at 3.938 inches, but the turns per coil vary as 8, 4, and 2. These values were chosen to illustrate how these parameters impact motor inductance.

| Parameters                                   | Numerical values |                      |           |            |                          |        |        |
|--|------------------|----------------------|-----------|------------|--------------------------|--------|--------|
|  |                  | 18                   | Pole      |            |                          | 8 Pole |        |
| Case   | #1               | #2                   | #3        | #4         | #5                       | #6     | #10    |
| Rated power, P <sub>r</sub> , W              | 30000            | 30000                | 30000     | 30000      | 30000                    | 30000  | 30000  |
| Torque, N-m                                  | 191              | 191                  | 191       | 191        | 191                      | 191    | 191    |
| Speed, rpm                                   | 1500             | 1500                 | 1500      | 1500       | 1500                     | 1500   | 1500   |
| Outer radius of stator, $R_{so}$ , in        | 5                | 5                    | 5         | 5          | 6.5                      | 6.5    | 6.5    |
| O radius of rotor, R <sub>ro</sub> , in.     | 3                | 3                    | 3         | 3          | 3                        | 3      | 3      |
| Inner radius of rotor, R <sub>ri</sub> , in. | 2.453            | 2.453                | 2.453     | 2.453      | 2.009                    | 2.009  | 2.009  |
| Stack length, L, in.                         | 1.969            | 1.969                | 3.938     | 3.938      | 3.938                    | 3.938  | 3.938  |
| Supply voltage, V <sub>dc</sub> , V          | 529.31           | 264.26               | 408.19    | 203.71     | 409.11                   | 204.47 | 102.23 |
| Number of magnets                            | 18               | 18                   | 18        | 18         | 8                        | 8      | 8      |
| $\Omega_{\rm b}$ , elect. rad/s              | 1413.72          | 1413.72              | 1413.72   | 1413.72    | 628.3                    | 628.3  | 628.3  |
| T <sub>c</sub> , turns/coil                  | 8                | 4                    | 4         | 2          | 8                        | 4      | 2      |
| T <sub>s</sub> , turns/slot                  | 16               | 8                    | 8         | 4          | 16                       | 8      | 4      |
| Line-to-neutral back-emf at                  |                  |                      |           |            |                          |        |        |
| base speed, E <sub>b</sub>                   | 147.06           | 73.53                | 147.06    | 73.38      | 138.52                   | 69.26  | 34.63  |
| $I_{peak} = P_r / (2E_b), A$                 | 102              | 204                  | 102       | 204.42     | 108.29                   | 216.58 | 433.15 |
| I <sub>rms</sub> = sqrt(2/3)Ipeak            | 83.28            | 166.56               | 83.28     | 166.90     | 88.42                    | 176.83 | 353.67 |
| Phase inductance, L, uH                      | 1270             | 316                  | 624       | 156        | 1560                     | 390    | 97     |
| Phase resistance, R, ohms                    | 0.0673           | 0.0168               | 0.0249    | 0.006      | 0.0153                   | 0.0038 | 0.0009 |
| Wire gage                                    | 16               | 16                   | 16        | 16         | 16                       | 16     | 16     |
| Wires per turn                               | 6                | 12                   | 12        | 25         | 27                       | 55     | 111    |
| Wire area, mm2                               | 1.308            | 1.308                | 1.308     | 1.308      | 1.308                    | 1.308  | 1.308  |
| Copper area in slot, mm2                     | 133              | 133                  | 133       | 133        | 583                      | 583    | 583    |
| Current Density, A/mm2                       | 13.00            | 13.00                | 6.50      | 6.25       | 3.07                     | 3.01   | 2.98   |
| L <sub>DMICmin</sub> , uH                    | 97               | 24                   | 97        | 24         | 195                      | 49     | 12     |
| L <sub>DMICno cont. cu</sub> r, uH           | 839              | 210                  | 839       | 209        | 1674                     | 419    | 105    |
| L <sub>DMICmax</sub> , uH                    | 1074             | 268                  | 1074      | 267        | 2144                     | 536    | 134    |
| The following inductances use                | Lawler's         | V <sub>dc</sub> . Th | ey are be | est when I | _ <l<sub>DMICmax</l<sub> |        |        |
| L <sub>CPAmin</sub> , uH                     | 568              | 142                  | 684       | 170        | 1315                     | 329    | 82     |
| L <sub>CPAinf</sub> ., uH                    | 1074             | 268                  | 1074      | 267        | 2144                     | 536    | 134    |
| L <sub>CPAmax</sub> , uH                     | 2131             | 532                  | 1643      | 409        | 3491                     | 872    | 218    |

 Table 6.4. Comparison of high- and low-inductance motors

Cases 1 and 2 were initially designed for geometrically similar motors having widely different inductances, 1270 uH and 316 uH, respectively, to compare how well they would respond to CPA control and to DMIC. From Table 6.4, we find that even though the inductances differ by a factor of 4, they are both sufficiently large that CPA is more efficient than DMIC. CPA is capable of operation at infinite CPSR if resistances are neglected. The current density, however, is quite high at 13 A/mm<sup>2</sup>. Hendershot<sup>1</sup> recommends that the range be between 4 and 10 A/mm<sup>2</sup>,

with the lower number for totally enclosed motors and the upper number for forced-air-cooled motors. The Case 1 and 2 motors would have to be liquid cooled.

Since the inductance is proportional to the square of the number of turns per coil and the length of the coil, the stack length of Cases 3 and 4 was increased so that the number of turns could be reduced. The cost of the material associated with the additional length was \$160, making the low-inductance motor more expensive. The current density was reduced to a more acceptable value of 6.5 A/mm<sup>2</sup> in Case 4; and, in both cases, the motor inductance is slightly below the minimum required for using CPA, indicating that the DMIC control is superior. The efficiency calculation confirms DMIC superiority by 2 percentage points for Cases 3 and 4. The reason is that the DMIC rms current is 60% of that drawn by CPA.

Cases 5, 6, and 10 employed a larger diameter to make more room for the stator wires so that the current density could be reduced while a wide range of inductances is explored. The current density is reduced to 3 A/mm<sup>2</sup>, and the inductances range from about 100 to 400 to 1600 uH as the turns per coil range from 2 to 4 to 8, respectively. In all three cases CPA will work, but the rms current for DMIC control is 70% of the current drawn by CPA.

# 6.2.3 PM Rotors with Magnet Encasement

The magnets of high-speed PM motors must be encased to ensure that they do not separate from the rotor and that they do not shift, which could cause imbalance problems. Examples of materials used for encasement are aluminum, 304 stainless steel, Inconel 718, wound fiberglass tape pre-impregnated with phenolic resin, wound fiberglass composites, and wound carbon fiber composite material. The metals and carbon fiber composite are conductors, a fact that must be considered if they are used. Prepreg fiberglass tape is a relatively low-cost insulator and may be applied and oven-cured. The problem with all the encasements is that they occupy space in the gap between the magnets and the stator teeth, limiting the amount of encasement that may be used.

An interesting feature of a metal can is that it is a conductor and as such can generate torque like a squirrel cage induction motor until synchronous operation is achieved. For synchronous operation, the non-magnetic properties of the aluminum allow the rotor to behave like a conventional surface-mounted PM motor.

The final report will include a finite element mechanical analysis showing the speeds at which plastic deformation or other failure mechanisms initiate.

# 6.3 THE OUTER ROTOR MOTOR

Figure 6.1 shows the input of Case 8, which was analyzed using SPEEDCAD software. Its dimensions are shown in Table 6.3. This motor operates in BDCM mode, and its circuit parameters at a base speed of 1500 rpm are

Rated power,  $P_r = 30 \text{ kW}$ , Number of poles, p=18, Back-emf per phase,  $E_b=101.8$  V, Rms phase current,  $I_b = 155$  A, Inductance per phase,  $L = 219 \mu$ H, and Resistance per phase,  $R=15 m\Omega$ .

Total

| RadSH    | 5.000   | (x,y)=(-5.610,-3.096) |
|----------|---------|-----------------------|
| Rad1     | 4.060   |                       |
| Gap      | 0.060   |                       |
| LM       | 0.236   |                       |
| BetaM    | 180.000 |                       |
| dGap     | 0.000   |                       |
| Poles    | 18      |                       |
| Nmbp     | 1       |                       |
| Rad3     | 0.375   |                       |
| Slots    | 54      |                       |
| S-Slot   | Square  |                       |
| SD       | 1.750   |                       |
| TWS      | 0.200   |                       |
| SO       | 0.080   |                       |
| TGD      | 0.040   |                       |
| SOAng    | 20.000  |                       |
| Lstk     | 4.000   |                       |
| RotType  | ExtRad  |                       |
| Config   | Normal  |                       |
| RotorAng | 0.000   |                       |
| U        |         |                       |
|          |         |                       |
|          |         |                       |
|          |         |                       |
|          |         |                       |
|          |         |                       |
|          |         |                       |
|          |         |                       |

Fig. 6.1. Configuration of the outer rotor PM motor.

At 30,000 W and 1500 rpm, the efficiency is 93%. The active component weights are shown in Table 6.5, and losses are summarized in Table 6.6.

| Material              | Weight, lb |
|-----------------------|------------|
| Rotor and stator—Iron | 26.68      |
| Magnets—NeFeB         | 3.05       |
| Wire—Cu               | 5.69       |

35.42

| Table 6 5   | Component | waights of | the Coce | 9 outor | noton motor |
|-------------|-----------|------------|----------|---------|-------------|
| 1 able 0.5. | Component | weights of | the Case | o outer | rotor motor |

| Туре   | Loss at 1500 rpm, W | Loss at 6000 rpm, W |
|--------|---------------------|---------------------|
| Cu     | 732                 | 124                 |
| Fe     | 929                 | 12272               |
| Magnet | 599                 | 9566                |
| Total  | 2160                | 21962               |

Table 6.6 Outside rotor motor losses at 30 kW useful power

In the SPEEDCAD software, 10-mil laminations are used and the magnets are not segmented; consequently, the losses at 6,000 rpm are quite high. This emphasizes the need for a small volume of iron, segmented magnets, and a laminate that has low losses at high electrical frequencies.<sup>8</sup>

# 6.4. THE AXIAL-GAP MOTOR

Dimensions of the axial-gap motor are shown in Table 6.3, and Fig. 6.2. shows the components of ORNL's axial gap PM motor, which is similar to but heavier than the motor of Case 7 discussed in this section. The two stators are wired in series. There is a 40-mil air gap between each stator and the magnet. Each stator is 2.4 in. thick, and the magnets are 0.1 in. thick (the magnets in ORNL's motor are 0.2 in. thick). Since the motor is designed to operate as a BDCM, there are 54 slots. Each double-layer coil has three turns, placing six turns in each slot. The motor parameters for a base speed of 1500 rpm are

Rated power,  $P_r = 30$  kW, Number of poles, p=18, Back-emf per phase,  $E_b=80$  V, Inductance per phase, L = 434 µH, and Resistance per phase, R=17.4 mΩ.

The motor is designed for operation at 6000 rpm to achieve a CPSR of 4. Since it operates in the BDCM mode, two phases are on at any one time. Thus the total back-emf at base speed is 160 V, while at 6000 rpm the total back-emf is 640 V (320 V/stator). The active material weights are shown in Table 6.7.

ORNL's 30-kW axial-gap PM motor was mechanically designed using elastic equations that were symmetric about an axis to determine the required interference at the titanium ring/magnet interface and at the magnet/hub interface. The design analysis did not evaluate the effect of bending, which occurs because of the 18 equiangular loads from the magnets. The titanium ring solved the differential expansion problem that had allowed the magnets to slip on the hub when the temperature increased during operation. Furthermore, the higher strength of the titanium ring allowed the motor rating to be increased to 30 kW, its original design goal. Although the motor and fan have remained intact while they were driven by the dynamometer at 6600 rpm for a half hour, an FEA will provide a clearer picture of the stresses during operation. A mechanical analysis of this design will be included in the final report, along with performance test results.



Fig. 6.2. Elements of ORNL's axial-gap PM motor.

 Table 6.7. Component weights of the Case 7 axial-gap PM motor

| Material                                 | Weight, lb |
|--|------------|
| Stators (2) 0.005-in. silicon steel tape | 31.1       |
| Magnets—NeFeB                            | 1.07       |
| Wire—Cu                                  | 16.46      |
| Rotor—Al hub with Ti support ring        | 2.13       |
| Total                                    | 50.76      |

### 6.5 SALIENT POLE PM MOTOR

In FY 2000, ORNL conceived the idea of a PM motor with self-supporting magnets, which would slide into a slot at the surface of the rotor and which would depend upon the strength of the magnet to support itself and the strength of the rotor material to hold it in place. The magnet shape would be in the shape of a fat inverted "T," and a ledge or tab machined into the rotor material would grip the inside of the T's overhang.

Two obvious possibilities exist for such a motor configuration. Originally, the thought was to place the magnets as close together as possible so that the magnets would appear as conventional radial-gap surface-mounted magnets, with a magnet fraction slightly larger than normal because of the presence of the support tab. Recently, however, Honda has used this approach, with increased separation of the magnets to make use of reluctance torque, which ORNL had not considered. The separation was optimized to maintain sufficient reluctance torque while using less magnet material. Greater magnet separation also lightens the load on the tabs and correspondingly lightens the reaction load on the magnets, which increases the possible rotor speed.

Figure 6.3 shows the configuration initially being examined. The web between the magnets in this configuration is 4 mm. The magnets are 7 mm thick. For this configuration, the outer radius of the rotor is 3.1 in. and the inner radius is 2.2 in.



Fig. 6.3. Rotor with self-supporting magnets.

Gap elements are placed between the magnet and the rotor so that the variation of the load distribution from the magnets on the rotor may be examined. The load is along the gap element, which is drawn normal to the two surfaces it is separating. Gap elements are chosen so that they do not enter the calculation unless the gap is reduced from its initial value during the solution. The solution is iterative; consequently, the magnet must be supported by a weak spring in the finite element model so that during the initial calculation, it may determine which gap element first began to decrease. The stiffness of that gap, which is the modulus of the surrounding material, is then included in subsequent calculations.

Figure 6.4 shows the compressive loads in pounds at each of the nodes along the magnet/rotor interface. The largest load is –164 lb. It also shows the load on the weak spring, which is about 0.1 lb, which will have little effect on the solution. Figure 6.5 shows the von-Mises stress between the magnet and rotor, as well as the stress caused in the rotor by the magnet load. Figure 6.6 confirms that the radial stresses between the rotor and magnet are compressive and that the radial stresses in the rotor near the inner corner of the magnet are tensile because of bending of the tab. Plastic deformation in the silicon steel occurs at 9237 rpm. This number will rise as the web increases and the magnet material decreases. Figure 6.7 shows the radial displacement of the magnet and the M-19 silicon steel tab at maximum speed, revealing that intrusion into the gap is small, even at this high speed.



Fig. 6.4. Self-supporting load along the magnet/rotor interface.



Fig. 6.5. Von Mises stresses induced by rotor bending and magnet loading.



Fig. 6.6. Radial stresses confirming compression at magnet/rotor interface and rotor bending at base of tab.



Fig. 6.7. Radial displacement of the self-supporting magnet.

#### 6.6 FRACTIONAL-SLOT WINDING

A fractional-slot motor is shown as it appears in the SPEEDCAD software in Fig. 6.8. At a base speed of 2000 rpm, the circuit parameters are

Rated power,  $P_r = 30 \text{ kW}$ , Number of poles, p = 10, Back-emf per phase,  $E_b = 48.5 \text{ V}$ , RMS phase current,  $I_b = 30000/(3*48.45) = 206$  A, Inductance per phase,  $L = 234 \mu$ H, and Resistance per phase,  $R = 5.25 m\Omega$ .

Iterating between Eqs. (5) and (17) of Appendix E leads to a minimum inductance value of 185.3  $\mu$ H for constant lead-angle control. Since the circuit parameter is 234 uH, the motor can be controlled in the PMSM mode.

The motor meets the efficiency specifications at 2000 rpm because its efficiency at 20% torque is 94.6%; however, at 20% torque and 10,000 rpm, the efficiency is 82.7 %. The problem is increased core loss, and the loss in the magnets as shown in Table 6.8.



Fig. 6.8. A fractional-slot motor.

Table 6.8. Losses of the fractional-slot motor at 20% torque

| Speed, rpm | P <sub>Cu</sub> , W | P <sub>core</sub> , W | P <sub>mag</sub> , W | P <sub>total</sub> , W |
|------------|---------------------|-----------------------|----------------------|------------------------|
| 2000       | 32                  | 152                   | 154                  | 338                    |
| 10,000     | 44                  | 2400                  | 3874                 | 6318                   |

In the PEEMRC data, the laminations are 10 mil thick, and the magnets are not segmented. Assuming a 50% core loss reduction from employing 5-mil laminations and a 50% magnet loss

reduction from employing segmented magnets, an estimate of the power loss and efficiency at 10,000 rpm for 30 kW useful power is

$$\begin{split} P_{loss} &= 1200 + 1937 + 44 = 3181 \ W \\ E_{motor} &= 30000/(30000 {+} 3181) \ x \ 100 = 90.4\% \ . \end{split}$$

These values emphasize the need to have a low-loss lamination material and segmented magnets.

# 7. COST ANALYSIS

With few exceptions, most motor cost estimates currently available are at the aggregate level, providing no detailed mass and cost distribution of motor constituent elements.<sup>9</sup> It is important that cost analysis be performed at the motor component level when several competing alternative motor designs need to be evaluated based on both performance and cost.

## 7.1 METHODOLOGY AND ASSUMPTIONS

The focus of this cost analysis is to examine the relative cost-effectiveness of alternative motor designs. Other major electric drive components, such as the controller and gear drive, have not been included in this analysis. A spreadsheet-based cost modeling framework was developed for electric motor cost estimation that would allow an examination of performance vs. cost trade-offs among the competing alternative designs. This framework is designed so that it also allows adjustments, at the component level, for changes in material prices, substitutions, or design changes to further refine the estimate and to test the sensitivity of overall motor cost to changes in component costs. Although the initial focus of the cost estimation is at the major component level, additional design details such as different magnet shape and strength will be incorporated as design progresses.

The cost estimation in this study assumes a bottom-up approach in a large-scale motor manufacturing facility. The cost structure for a motor manufacturing facility was developed based on conversations held with a few brushless PM machine manufacturers. Each motor is broken down into *seven* main constituent elements that include magnets, rotor lamination, rotor shaft, stator lamination, copper windings, housings, and cooling. Housings mainly include rotor end caps, motor frame, and frame end caps. Motor component sizing information obtained from SPEEDCAD runs is used as essential input for the cost estimation.

It is assumed that the production of these components takes place under realistic, favorable economic conditions with volumes high enough to justify a significant level of automation and full realization of raw-material volume discounts. Raw materials for various motor components are purchased from suppliers, and they are assembled in a motor manufacturing facility. Laminations are usually sold as a set for both rotors and stators, and cost in this case is mostly dictated by the stator size, number of slots and magnets. Although lamination dies made of carbide materials are expensive, in the range of  $\sim$  \$200K, a long die life of about 70 million parts results in this cost being a relatively small fraction of the overall lamination cost. Rotor shaft material is assumed to be cold drawn steel. The motor frame and end caps are manufactured from extruded aluminum and die-cast aluminum, respectively. The cost of motor cooling has not been determined explicitly, but it is estimated to be 10% of the total manufacturing cost. Labor and overhead are assumed to take into account the cost of machining operations necessary for the motor housing and end caps. Thus, the manufacturing cost of the complete motor is determined by adding the individual element costs plus the labor and overhead, which includes the cost of assembly and testing and is estimated to represent ~25% of the total motor component material costs. Finally, the OEM cost is estimated by adding the profit margin of 10% for a large-scale production volume to the manufacturing cost.

## 7.2 COST ESTIMATES FOR THE IPM MACHINE

Table 7.1 shows the mass and cost of distribution of two alternative motor designs under consideration in this phase of this study. The relatively small size of the high-speed IPM motor design, compared with the 2004 Prius design cost, results in a low manufacturing cost, < \$340. The motor cost in terms of \$/kW is estimated to be 8.1 and 7.4 for the 2004 Prius and the high-speed IPM designs, respectively. These costs are considerably higher than the desired < \$2.2/kW AEMD motor specification. The gear drive cost was not included in the analysis because program targets did not require inclusion.

| Motor components   | Priu      | ıs 04     | High-Speed IPM |           |
|--------------------|-----------|-----------|----------------|-----------|
|                    | Mass (lb) | Cost (\$) | Mass (lb)      | Cost (\$) |
| Magnets            | 2.2       | 71        | 2.4            | 77        |
| Rotor lamination   | 11.7      | 16        | 11.8           | 13        |
| Rotor shaft        | 25.5      | 46        | 12.1           | 22        |
| Stator lamination  | 39.4      | 52        | 68.6           | 73        |
| Copper windings    | 13.2      | 44        | 11.8           | 38        |
| Housing            | 16.7      | 38        | 8.1            | 21        |
| Cooling            | n/a       | 33        | n/a            | 30        |
| Labor and overhead | n/a       | 67        | n/a            | 61        |
|                    |           |           |                |           |
| Mfg. cost          | n/a       | 367       | n/a            | 334       |
|                    |           |           |                |           |
| Profit margin      | n/a       | 37        | n/a            | 33        |
|                    |           |           |                |           |
| OEM price          |           | 404       |                | 368       |

Table 7.1. Motor mass and cost distribution of two alternative IPM designs

Material types for various motor components are assumed to be similar for both machine designs; but most component weights for the high-speed IPM design, except magnets and stator lamination, are either the same or less. The result is a lower manufacturing cost for the high-speed IPM machine than for the 2004 Prius design. As expected, the cost of magnets dominates the overall motor material cost distribution. In both cases, sintered magnets at a price of about \$32/lb were specified, which is the most expensive class of magnets used in electric motors today. It is estimated that the cost of sintered neodymium magnets is 30–70% higher than for the most commonly used compression-molded neodymium magnets. The magnet material prices are varying widely in the market today, creating increased uncertainty for estimating motor cost.
#### 7.3 PERFORMANCE VS. COST TRADE-OFFS FOR THE SURFACE-MOUNTED INNER ROTOR MACHINE

ORNL's Radial-Gap Motor Design Tool is an internal model of radial-gap PM motors, which was used to determine the dimensions, winding configurations, and weight of materials needed for the active components of the radial-gap PM motors with surface-mounted magnets discussed in Sect. 6. The component weights for each machine type are shown in Table 7.2. As in Sect. 6, the (four) 18-pole machines and (three) 8-pole machines are listed in the table.

|                                  | 18-pole |       |       |       | 8-pole |       |       |
|----------------------------------|---------|-------|-------|-------|--------|-------|-------|
| Material weight \ case           | #1      | #2    | #3    | #4    | #5     | #6    | #10   |
| Magnet mass, Ib                  | 2.15    | 2.15  | 4.30  | 4.29  | 4.45   | 4.45  | 4.45  |
| Rotor laminates, lb              | 2.79    | 2.79  | 5.58  | 5.57  | 12.38  | 12.38 | 12.38 |
| 1.5-india steel shaft, lb.       | 2.93    | 2.93  | 3.90  | 3.90  | 3.90   | 3.90  | 3.90  |
| Two 0.5-inthick steel            |         |       |       |       |        |       |       |
| connecting disks, lb             | 4.76    | 4.76  | 4.76  | 4.76  | 3.03   | 3.03  | 3.03  |
| Stator laminates, Ib             | 14.90   | 14.90 | 29.80 | 29.74 | 66.30  | 66.30 | 66.30 |
| Copper, Ib                       | 13.90   | 13.90 | 20.55 | 21.38 | 64.17  | 65.36 | 65.96 |
| 0.5-inthick AI cylinder housing, |         |       |       |       |        |       |       |
| lb                               | 4.90    | 4.90  | 8.14  | 8.14  | 10.47  | 10.47 | 10.47 |
| Two 0.5-in Al end disks, lb      | 7.68    | 7.68  | 7.68  | 7.68  | 13.10  | 13.10 | 13.10 |

| Table 7.2. Weight | t comparison of P | A motors with | n surface-mounted | magnets |
|-------------------|-------------------|---------------|-------------------|---------|
|-------------------|-------------------|---------------|-------------------|---------|

The costs of components, labor, and profit for each machine type are shown in Table 7.3. Material cost in \$/lb is referenced in the second column of Table 7.3. The cost in \$/laminate for M19 silicon steel laminates for the stator and rotor is listed in the row under the case numbers. Costs of the shaft; the two disks it penetrates, which support the rotor flux return cylinder; and the 0.5-in.-thick aluminum housing cylinder and end disks are added to obtain a complete motor cost estimate. The processing and overhead costs are considered to be 25% of the material cost. Cooling costs are estimated to be 10% of the sum of the material cost, plus processing and overhead cost. These costs are added to the 10% profit margin to obtain the OEM cost for the motor alone. Inverter costs are not included.

|                                   |           | 18-pole            |          |          |                    | 8-pole   |                 |          |
|-----------------------------------|-----------|--------------------|----------|----------|--------------------|----------|-----------------|----------|
| Material\ case                    | cost/unit | #1                 | #2       | #3       | #4                 | #5       | #6              | #10      |
| Cost per laminate, \$/laminate    |           | 0.41               | 0.41     | 0.41     | 0.41               | 0.63     | 0.63            | 0.63     |
| Magnet material, \$               | \$14.50   | \$31.18            | \$31.18  | \$62.35  | \$62.21            | \$64.53  | \$64.53         | \$64.53  |
| 0.0185-in. M19 rotor lamins., \$  |           | \$6.68             | \$6.68   | \$13.35  | \$13.35            | \$20.47  | \$20.47         | \$20.47  |
| Rotor shaft, \$                   | \$1.80    | \$5.27             | \$5.27   | \$7.01   | \$7.01             | \$7.01   | \$7.01          | \$7.01   |
| Rotor support disks, \$           | \$0.50    | \$2.38             | \$2.38   | \$2.38   | \$2.38             | \$1.52   | \$1.52          | \$1.52   |
| 0.0185-in. M19 stator lamins., \$ |           | \$35.65            | \$35.65  | \$71.30  | \$71.30            | \$109.61 | \$109.61        | \$109.61 |
| Copper wire, \$                   | \$3.07    | \$42.60            | \$42.60  | \$62.99  | \$65.53            | \$196.68 | \$200.33        | \$202.17 |
| Cylindrical aluminum frame, \$    | \$2.50    | \$12.24            | \$12.24  | \$20.36  | \$20.36            | \$26.18  | \$26.18         | \$26.18  |
| Aluminum end caps, \$             | \$3.00    | \$23.03            | \$23.03  | \$23.03  | \$23.03            | \$39.29  | \$39.29         | \$39.29  |
| Labor and overhead                | 25%       | \$30.76            | \$30.76  | \$65.60  | \$66.20            | \$116.32 | ¢117 23         | \$117.60 |
|                                   | 10%       | \$39.70<br>\$10.88 | \$10.88  | \$32.85  | \$00.29<br>\$33.15 | \$58 16  | \$58.62         | \$58.85  |
| Cooling                           | 10 /0     | φ19.00             | \$19.00  | ψυ2.00   | φ00.10             | φ30.10   | φ <u></u> 00.02 | φ30.03   |
| Mfg. cost                         |           | \$218.67           | \$218.67 | \$361.32 | \$364.62           | \$639.76 | \$644.78        | \$647.31 |
| Profit margin                     | 10%       | \$21.87            | \$21.87  | \$36.13  | \$36.46            | \$63.98  | \$64.48         | \$64.73  |
| OEM price                         |           | \$240.54           | \$240.54 | \$397.45 | \$401.08           | \$703.74 | \$709.26        | \$712.04 |

Table 7.3. Cost comparison of PM motors with surface-mounted magnets

The question about the cost of electric motors with increased inductance made this study especially interesting. Work with DMIC had shown that, when CPA is used, a high inductance is necessary to control the current at its rated value during high-speed operation. Before the study, the statement was often heard that inductance is expensive. The reason is that in several cases, the system inductance was increased by adding inductors in each of the three motor phases, which is cumbersome and inefficient. Since DMIC incurred the added cost of six additional thyristors, making it inherently more expensive than a conventional 3-phase voltage source inverter, consideration was given to offsetting this expense by designing a smaller low-inductance electric motor that used a smaller inverter with lower-rated devices. However, it was later determined that there is significant additional cost to designing a low-inductance motor, precluding any offsetting cost benefit.

# 8. SUMMARY

This interim report provides background and summary information that describes parametric studies conducted over recent years, and testing programs that demonstrate both the potential capabilities and technical limitations of

- brushless PM machines (axial gap and radial gap),
- the IPM machine,
- surface-mount PM machines (interior or exterior rotor),
- induction machines, and
- switched reluctance machines.

This section described the general findings and accomplishment of the study as of June 2004.

#### IPM Machine Modeling

This study relied on numerous, complex modeling executions (i.e., lumped parameter and FEA) where scripting subroutines were necessary for varying numerous parameters to arrive at machine designs that exhibit optimized performance. The results of the FEAs were used to improve the accuracy of the lumped parameter model results. The modeling effort first required that both the models and the modeling approach be verified by modeling a machine with known performance characteristics. The only IPM machine filling this requirement was the traction motor in the Toyota Prius. After considerable effort and many SPEEDCAD and Flux2D runs, the analysts were able use FEA model results effectively in "fine-tuning" the lumped parameter model. Specifically, the impact of magnetic saturation required adjusting the lumped parameter code because it was not able to accurately simulate saturation as an FEA code can.

It is interesting to note that for the baseline IPM machine (i.e. 2004 Prius), the efficiency is above 95% for all speeds except speeds below  $\sim$ 1200 rpm, where efficiency ranges from 71% at 520 rpm to 88% at 1100 rpm. The analysts believe that meeting program machine target goals in the overall project will likewise be dependent on machine speed.

The next effort in the study was to take the adjusted lumped parameter model and model a highspeed (i.e. reduced-size) IPM machine that would be able to operate at the target design specification speed (i.e., >10 Krpm). Scaling the IPM machine down in size to one that would operate at high speed required a rotor that would experience the same stresses at 10 Krpm as the baseline design at 5400 rpm. The rotor was scaled by 0.6 and the stator and stack length were adjusted based on other considerations, including multiple modeling runs with a scripting subroutine. The analysts were generally pleased by the resulting machine design, which is predicted to produce the required torque and power to meet performance target goals. Plots of torque, power, current, and efficiency based on the lumped parameter model showed reasonable results and relationships, which will receive further analysis and verification as the study continues.

The optimized, high-speed IPM machine has efficiencies similar to those of the baseline case. However, in the extended, high-speed range, efficiency dropped to 90% at 8 Krpm and 86% at 10 Krpm. This is considered acceptable, especially at this stage of development. The modeled source voltage was maintained at a much lower level (200 V) than for the baseline case (600–885 V). Consequently, the current level was much higher (150–505 Arms) over much of the speed range and far higher (~1200 Arms) at speeds ranging from 1–2 Krpm. The data make a strong case for increasing the source voltage, and plans for future study include doing so. FEA performance modeling of the high-speed IPM machine is planned to ensure that magnetic saturation levels are reasonable and to verify that there is good agreement with the lumped parameter model.

The study will continue, using the modeling tools to analyze other selected alternative machines of high interest, including (1) IPM machines whose rotors contain layered magnets and (2) 12-pole PM machines featuring surface magnets with mechanical locking tabs for magnet retention. The study also plans to explore the use of relatively weak injected magnets in selected machine configurations.

#### IPM Design Issues

As rotor speed increases, mechanical balance at all possible load and cooling conditions becomes more critical. In addition, magnetic losses in the rotor become more important due to the higher frequencies and thus high-quality steel and laminated construction becomes imperative. In high-speed PM machines, rotor magnet retention and rotor structural integrity are critical and must be adequately addressed. In the IPM design, the greatest mechanical stresses in the rotor are in the bridge areas (i.e., a pair of thin strips of metal retaining both the magnets and a triangular steel segment above the magnets called the polar cap). Increasing the width of the bridge reduces the mechanical stress but it increases the amount of magnetic energy leaking through it (up to 25% of the magnetic potential may be lost.) A low magnetic saturation limit in the bridge's material will effectively limit the impact of this magnetic flux leakage path. Mechanical requirements for the bridge are discussed in Sect. 4.1.2.2. Alternative ways to hold the magnets and polar cap in place may have to be considered.

The OEM's electric motor goal is for a limited-duration 55 kW peak power output at the base speed of 2000 rpm and 30-kW continuous-power up to a speed of at least 10,000 rpm. These output goals must be attained with a dc link voltage of 200 Vdc and a 400 A<sub>rms</sub> current limit. In addition, there are formidable goals for efficiency and power density. The conflicting design impact of certain target goals makes questionable whether all the goals can indeed be satisfied simultaneously. For instance, parametric modeling results show that the 200 Vdc link requirement makes it difficult or infeasible to design a motor able to achieve 55 kW with less than 400 A<sub>rms</sub> and to deliver 30 kW at 10,000 rpm. To achieve high rotor speeds with a low voltage constraint requires low back emf generation in the rotor at high speeds. To accomplish this within a high power density goal, flux weakening and or a reduction in the number of turns in the stator poles is needed. This results in higher current densities and losses, and a reduction in the efficiency of the motor, and greater demands on the inverter.

In high-power-density IPM machines, it is unavoidable that both the rotor and stator operate at or near saturated conditions in many regions specifically during peak power operation, which creates electromagnetic design issues that this study is presently addressing. The high current at low speeds results in significant levels of magnetic saturation in the stator teeth and the rotor bridge is designed to operate at saturated conditions to prevent flux leakage. The study will continue to make use of FEA modeling to analyze IPM machines, particularly conditions prevailing at the stator teeth and the rotor bridge. FEA results, to date, are discussed in Sect. 5.4.3.

## Non-IPM Designs

Because the FreedomCAR program retains a strong interest in alternative machine designs, lumped parameter modeling of the following PM machines was performed:

- four 18-pole, radial gap (with cost study)
- three 8-pole, radial gap (with cost study)
- one outer-rotor
- one fractional-slot winding
- one Honda-type (T-shaped PMs with tabs for retention)
- axial gap—analysis begun (to continue)

These machines were designed to have a base speed of 1500 rpm, a CPSR of 4 and a base power of 30 kW to reflect performance targets in effect earlier in the study, when much of the work took place. The machines would be capable of short 55-kW bursts. During peak power bursts, the inverter current would be limited to 300 Arms. Between 1500 and 6000 rpm, some type of field weakening would be used.

Although a study with fully integrated lumped parameter modeling/FEA was not performed for these machines as it was for the IPM, modeling has produced results for most of the listed machine types. The Honda-type machine with T-shaped PMs was also analyzed using FEA to determine stresses in the PMs. Analyses will continue for assessing PM-retention rotor wraps and machine performance in general.

## Cost Study

Material types for the full-size and high-speed IPM machine components were assumed to be similar in both cases, but most component weights of the high-speed IPM design, with the exception of magnets and stator lamination, are either the same or less because the stack length is considerably greater (i.e., 200 mm vs. 83.6 mm). The large-plant, high-production manufacturing cost for the high-speed IPM machine is \$368, compared with \$404 for the baseline machine.

As expected, the cost of magnets dominates the overall motor material cost distribution. In both IPM cases, sintered magnets at a price of about \$32/lb were specified, which is the most expensive class of magnets used in electric motors. The magnet material prices vary widely in the market today, resulting in increased uncertainty for estimating motor cost.

Costs estimates also were generated for the surface-mounted, inner rotor machine. Attractive pricing resulted for the four 18-pole machines, ranging from \$240 to \$401.

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# APPENDIX A: SUMMARY OF PRIOR CRADA STUDY

The purpose of the parametric machine study CRADA was to evaluate the various high-potential machine technologies that can be applied to electric hybrid vehicles and machine tool applications. This appendix describes both the scope of the study and the results of motor testing performed at the end of the study.

The axial-gap PM machine demonstrated efficiencies 5–7% higher compared to the SRM during testing. The axial-gap PM machine has a peak efficiency of about 97% when operated with sinusoidal pulse width modulation (PWM) at higher torque levels. The axial-gap PM machine had efficiencies of  $\geq$  95% over a wide speed range with three electrical drive conditions: standard PWM, modified PWM, and sinusoidal PWM. The efficiency of the SRM ranged from about 86–90%. The acoustic noise emitted by the SRM was greater than 90 db for all speeds. The acoustic noise levels must be reduced in order to potentially be used in a traction motor application.

## A.1 CRADA STUDY SCOPE

The study focused on a number of different machines that were designed, optimized, and simulated to operate in either a motor or generator mode. Extensive design and analysis was conducted on the inverter electronics necessary to drive and control the machines. Loss and efficiency calculations, performance ratings, and weight and cost analyses were performed for each machine and for the inverters. The study also examined the cooling, packaging, and sensor issues associated with each machine system.

The 10 tasks that made up the parametric electric machine study CRADA are as follows.

- 1. **Design analysis**—This task consisted of the parametric study and evaluation of different inverter topologies, control schemes, and machine types. Through the use of computer analyses, machine and inverter performances were simulated so that valid comparisons could be drawn. The analysts examined and modeled both hard- and soft-switching inverter topologies.
- 2. **Drive system simulation**—In this task, the analysts studied various machine technologies by analytically placing each machine into a HEV platform. Series and parallel hybrid electric drive line architectures were simulated over the same drive schedule. The task compared the hybrid drive trains with a conventional drive train. The analysts compared various parameters, including performance, efficiency, fuel economy, and cost. Operating characteristics were derived for each of the technologies.
- 3. **Machine design**—This task pertained to the design of an axial-gap PM machine and SRM. The axial-gap PM machine was designed with two wound stators and one rotor with magnets mounted on each side of the rotor iron. The stator phases were connected in series to ensure an identical current flow in each.
- 4. **Manufacturing study**—The manufacturing study focused on several important design, manufacturing, assembly, and operation issues pertaining to the axial air gap motor. These issues are (a) axial force determination and impact during and after assembly due

to the magnets; (b) air gap tolerance determination and impact; (c) balance requirements and approaches that would be effective for the relatively large rotor diameter used in this type of motor; (d) PM retention methods, primarily for significant production operations where tolerances, in-place magnetization, and bonding methods are considered; (e) stator winding; (f) assembly techniques applying primarily to the prototype; and (g) multiple rotor or stator configurations for increased horsepower designs.

- 5. Electronics design—This design and development process was for a 45-kW inverter to drive the trapezoidal motor. It involved the construction and testing of a "test bed" inverter to demonstrate snubbing and packaging concepts and then the next-generation "universal" inverter. The snubbing circuit used in both protected the insulated gate bipolar transistors (IGBTs) from voltage stress and reduced switching losses. The inverter system was quite elaborate and beyond state-of-the-art at that time, including an encoder for speed and position feedback and a digital signal processor (DSP) controller to process commands and synthesize signals for the inverter drive bus.
- 6. **Machine hardware construction**—This task planned the construction of axial-gap and switched-reluctance motors (SRMs) based on concepts developed in the manufacturing study (Task 4 above).
- 7. Electronic hardware construction—The DSP inverter control system was built upon a PC computer system with interfaces to the inverter and motor. The motor controller was designed to control the axial-gap motor and a variety of other types of motors using current sensors and an absolute position encoder. A 16-bit I/O bus fed a data acquisition system.

## 8. Testing of axial-gap PM motor and an SRM

- a. Axial-gap PM motor testing—Motor testing was conducted at the CRADA partner facility in August of 1994. Performance was measured based on electrical, thermal, and mechanical characteristics. The primary electrical indices used were voltage, current, power, and efficiency. Tests included no-load, motor characteristics, system characterizations at 25 and 60°C coolant temperatures, mechanical, and thermal. Test results and conclusions are provided in Sect. A.3.1.
- b. SRM testing—An SRM and inverter system test was performed at the CRADA partner facility in January 1995. The general scope of the test and the types of data indices collected are the same as for the axial-gap PM motor. Test results and conclusions are provided in Sect. A.3.2.
- 9. Noise study—This study was to investigate the high-noise problem that is encountered in SRMs. The study successfully determined that commutation-related noise frequencies were prevalent at various motor speeds and that commutation-related noise suppression measures must be developed such as optimizing air-gap length and number of poles. Manufacturing tolerance (i.e., uneven machining or punching) in diametrically opposite poles can create uneven magnetic pull in the radial direction.
- 10. **Final analysis**—Based on the results of the design simulation and machine tests, and the results and recommendations for technology/test improvements were developed and documented.

Drive system specifications were established at the start of the project and the requirements applied to all motor designs included in the Task 1 parametric electric machine study. These designs include the following:

- Radial air gap PM machines
- Axial-gap PM machines
- Induction machines (radial and axial)
- SRMs
- Switched reluctance

## A.2 SUMMARY OF RESULTS OF THE PARAMETRIC STUDY

Parametric studies consist of analytical models that can be extremely useful in conducting machine/system analyses quickly and without the cost, inevitable delays, and logistical problems that tend to plague testing of actual hardware. Researchers who have been involved with hardware-based, experimental testing of new technologies are well acquainted with the problems that frequently arise. The parametric studies summarized in this section obtained results without the peripheral issues and complications of data acquisition inadequacies, calibration issues, bearing overheating, magnet demagnetization, magnet mounting, etc. that are evident in Sect. A.3. It is true that hardware-related problems must be discovered, and that is why tests of hardware are conducted. However, the logic and wisdom of first pursuing parametric studies for machine selection cannot be disputed.

The motor performance for three stator diameters and the efficiencies at selected low and high rotational speeds were determined. For each motor type, 7-in, 11-in, and 15-in stator diameters were considered, and typically a range of poles.

The motor efficiency derivations were determined by measuring the power consumption of the motor and determining the segregated motor losses. If the segregated losses are totaled, efficiency = 1-(total losses)/(total power to motor).

The types of motor losses include the following (listed from largest loss to smallest loss in the case of a radial PM motor representative of this study):

- Stator resistive (I<sup>2</sup>R) loss
- Rotor iron and magnet loss
- Stator eddy current
- Stator hysteresis
- Friction
- Windage

## A.3 SUMMARY OF THE RESULTS OF MOTOR TESTING

## A.3.1 Axial-Air-Gap PM Machine, Inverter, and Universal Controller Testing

A complete axial air gap PM motor and inverter system test was conducted to evaluate the entire system performance under motoring and regenerating modes. The efficiency of the combined system including motor and inverter reached 90% at full speed and half torque. The specification

called for 81% efficiency at the design point, and the system performed well beyond expectations based on simulation.

The motor data obtained in this test are considered inaccurate and should be used carefully. The error is due to the power meter's lack of bandwidth and the inability of the instruments to distinguish between the inverter's and the motor's contribution to power loss. The overall system performance measurements are considered accurate. More-reliable motor measurements could have been obtained if a power meter with higher sampling frequency, more memory storage, and faster computation speed had been available.

Table A.1 lists motor efficiency for various motor speed and torque levels for three electrical drive conditions: (1) standard PWM operation, (2) modified PWM operation, and (3) sinusoidal PWM operation. Table A.2 lists motor efficiency and torque for various motor speeds for the same three electrical drive conditions. Sinusoidal operation at high torque levels produced the highest efficiency measurements.

|                          | Motor speed (RPM) | Peak motor torque<br>(ft-lb) | Motor efficiency (%) |
|--------------------------|-------------------|------------------------------|----------------------|
| Standard PWM operation   | 2800              | 91.2                         | 94.4                 |
| 1                        | 2100              | 99.8                         | 93.6                 |
|                          | 1400              | 99.9                         | 91.1                 |
|                          | 700               | 99.9                         | 88.3                 |
| Modified PWM operation   | 2800              | 55.0                         | 92.1                 |
| •                        | 2100              | 100.8                        | 94.4                 |
|                          | 1400              | 100.2                        | 93.4                 |
|                          | 700               | 99.7                         | 88.8                 |
| Sinusoidal PWM operation | 2800              | 89.0                         | 96.2                 |
| 1                        | 2100              | 90.8                         | 95.5                 |
|                          | 1400              | 88.8                         | 93.0                 |
|                          | 700               | 95.2                         | 89.8                 |

#### Table A.1. Efficiency as a function of motor torque

|                          | Motor speed (RPM) | Peak motor efficiency<br>(%) | Motor torque (ft-lb) |
|--------------------------|-------------------|------------------------------|----------------------|
| Standard PWM operation   | 2800              | 96.5                         | 30.4                 |
| -                        | 2100              | 96.5                         | 29.7                 |
|                          | 1400              | 96.3                         | 10.2                 |
|                          | 700               | 96.1                         | 20.6                 |
| Modified PWM operation   | 2800              | 96.7                         | 30.0                 |
| 1                        | 2100              | 96.8                         | 30.1                 |
|                          | 1400              | 97.1                         | 20.5                 |
|                          | 700               | 94.4                         | 30.2                 |
| Sinusoidal PWM operation | 2800              | 97.4                         | 50.3                 |
| -                        | 2100              | 97.6                         | 30.1                 |
|                          | 1400              | 99.4                         | 10.2                 |
|                          | 700               | 96.1                         | 20.4                 |

#### Table A.2. Efficiency as a function of motor speed

#### System Efficiency Comparison between Different Control Methods

The comparison is limited to system efficiency only because of the accuracy of the instrumentation.

*Efficiency as a function of load torque*—The modified PWM method improved the efficiency by 3% at 100 ft-lb torque and more than 10% at torque below 30 ft-lb. At 10 ft-lb torque, the efficiency difference widened to 15%.

*Efficiency as a function of speed*—The modified PWM method was the overall winner because it produced the highest efficiency for a broader range of speeds and torques. The sinusoidal PWM method had lower efficiency at lower speeds compared with the standard PWM method. However, its efficiency numbers surpass those of the standard PWM method at high speeds. The sinusoidal PWM method has the same efficiency as the standard PWM method at half speed. When the speed is higher, the sinusoidal PWM method becomes more efficient.

## A.3.2 Switched Reluctance Machine

A complete SRM and inverter system test was conducted at the CRADA partner's facility to evaluate the system performance parameters, including electrical, thermal, and mechanical characteristics. Emphasis was placed on collecting electrical characteristics (voltage, current, power, and efficiency) for use in future design improvements of the SRM and power inverter.

The SRM constructed for the test was designed using the PC-SRD software (SPEEDCAD), developed by Glasgow University.

## Setup

The test setup for the motor and inverter included a dc dynamometer load, a dc power supply, a control unit, and a data acquisition system. System, inverter, and motor efficiency calculations

are based on three power measurements that were made at the dc input, inverter output, and motor output.

The load was a dc motor-based dynamometer that had a separated field weakening control for different speed settings. The source was a bidirectional dc power supply that provided power to the inverter during motoring and took the energy back to the utility line during the regenerative mode.

The motor controller included an HCTL-1100 motion control computer, a motion control board, and an inverter to establish the dc bus voltage, current limit, dynamometer speed, and field weakening. The motion control board monitors an encoder signal and compares it with the register information in the computer to determine the output PWM signals for the inverter. The inverter was a conventional two-switch, two-diode-per-phase, IGBT-based inverter.

The data acquisition system was a computer-controlled unit that retrieved data from a general purpose interface bus (GPIB). All instruments were equipped with a GPIB bus and were triggered simultaneously.

## Stator Winding Temperature Tests

Four temperature sensors were attached to the stator windings while the motor was tested at four different speeds (700, 1400, 2100, 2800 rpm) and four different torque settings (25, 50, 75, and 100 ft-lb). The motor was cooled by a chiller adjusted to 23°C. At each load condition, the temperature among the windings varied by only 20°C. From the measured stator winding temperature, the temperature inside the motor rotor was expected to be greater than 90°C. The high temperature from the bearing was not detected by the stator windings. <u>Efficiency Tests</u>

The inverter output power measurement needed four channels. As a result of constraints of the data acquisition system, only three channels were used to project the total inverter output power. The accuracy was unknown, but the results tended to favor the motor and gave it a higher than expected efficiency measurement at low speeds. The numbers look more reasonable at high speeds.

The measurement of the system efficiency seemed to be accurate and consistent to the team analysts. Typically, a low-speed, low-torque condition gave lower efficiency and vice versa. The overall system efficiency was significantly lower than that obtained from the PM machine drive, which had 90% maximum system efficiency. The efficiency value was also lower than that projected by the PC-SRD software.

Motor efficiency for the SRM at 2800 rpm ranged from approximately 76% for low torque to about 88% at high torque. For low speed (700 rpm), the efficiency ranged from approximately 86% at low torque to 90% at high torque. Table A.3 lists the motor efficiency for the SRM.

| Target motor<br>speed (rpm) | Actual motor<br>speed (rpm) | Motor torque<br>(ft-lb) | Motor power<br>(watts) | Motor efficiency<br>(%) |
|-----------------------------|-----------------------------|-------------------------|------------------------|-------------------------|
| 700                         | 730                         | 25.5                    | 4,320                  | 86.1                    |
|                             | 760                         | 49.9                    | 8,040                  | 88.6                    |
|                             | 785                         | 75.7                    | 12,480                 | 90.0                    |
|                             | 815                         | 102.4                   | 17,520                 | 89.6                    |
| 1400                        | 1430                        | 25.2                    | 5,117                  | 80.6                    |
|                             | 1460                        | 51.6                    | 10,698                 | 88.0                    |
|                             | 1485                        | 75.1                    | 15,836                 | 88.3                    |
|                             | 1510                        | 100.4                   | 21,528                 | 88.5                    |
| 2100                        | 2130                        | 24.2                    | 7,320                  | 78.4                    |
|                             | 2155                        | 50.0                    | 15,300                 | 84.9                    |
|                             | 2190                        | 75.0                    | 23,323                 | 86.8                    |
|                             | 2220                        | 100.0                   | 31,524                 | 87.8                    |
| 2800                        | 2830                        | 25.7                    | 10,328                 | 76.3                    |
|                             | 2860                        | 49.7                    | 20,184                 | 85.1                    |
|                             | 2890                        | 74.7                    | 30,655                 | 86.8                    |
|                             | 2920                        | 99.0                    | 41,049                 | 87.3                    |

Table A.3. SRM efficiency test results

#### Measurement Results at Regenerative Mode

Only two regenerative mode measurement points were taken (700 rpm at 25 ft-lb and 50 ft-lb). The phase A voltage waveform indicates IGBT chopping during PWM operation, compared with the motoring mode where only one IGBT operated during operation. The current ripple shows the same order of magnitude for both the motoring and regenerative modes.

The dc link current oscillated at a frequency close to the utility supply possibly due to noise pickup.

## Mechanical Vibration and Noise Measurement Results

The mechanical vibration was tested at three target speeds (700, 1400, and 2100 rpm) by placing vibration pickups at the front and back bearings. The frequency spectrum for the mechanical vibrations is a function of the component specifications and the electrical commutation frequency. The commutation frequency is equal to the product of the motor's speed and the number of rotor poles divided by 60.

Power measured at the second, third, and fourth harmonics is about the same as the fundamental frequency, indicating that the four stator torque pulses are reasonably balanced.

Acoustic noise was picked up that related to the commutation frequencies. The lower-frequency acoustic noises (below 200 Hz) were suppressed by the mounting bed. The measurement results indicated that the overall acoustic noise level was greater than 90 db for all speeds. The noise frequencies were commutation-related and clustered below 3.5 kHz. The noise of the PWM switching frequency (3 to 4.5 kHz) did not stand out in most cases, except at 700-rpm, 25 ft-lb load. Therefore, SRM acoustic noise reduction should focus on commutation related noises.

# APPENDIX B: SUMMARY OF THE AEMD TEAM 1 STUDY

AEMD Team 1 engineers considered several machine configurations for the AEMD machine design. These included sinewave PM machines, induction machines, and switched reluctance motors (SRMs). Machine designs were developed according to AEMD specifications and guidelines provided by the EETTs. For each configuration, the best machine design of the favored topology was selected and documented.

The research and development (R&D) emphasis was different for each machine type, depending on where the technical challenges were or what needed to improve to make each a stronger contender. The effort was directed toward the evaluation of low-cost technology for the induction machine, design for large CPSR for the PM machine, and investigation of various drive topologies for the SRM.

As part of the AEMD project, Team 1 has developed a parallel induction machine that was tested in part at ORNL. The machine performed well and, because of its mature and well-understood technology, represents a low risk. For the size of interest, the induction machine has a lower efficiency and power density when compared to the PM machine. Only small improvements are expected to the performance characteristics of the induction machine in the future; thus, the PM machine appears to be better suited for traction drive applications. AEMD Team 1 also developed a series PM machine with an outer rotor configuration. The motor testing demonstrated a fairly wide speed range with efficiencies  $\geq$  93%. The outer-rotor PM machine is well suited for medium and high-speed applications. The outer-rotor design may pose a potential rotating hazard if not properly shielded. The IPM machine has higher power density when compared to the outer rotor machine. This appendix summarizes the activities and results for each of the motor projects.

## **B.1 TOP-TIER TARGETS AND COMPARISON OF MACHINE TYPES**

The overall goal of the AEMD task was to develop traction motors for potential HEV applications. These targets are listed in Table B.1 for a series machine.

| Parameter                                    | Target                          |
|--|---------------------------------|
| Cost   | \$450                           |
| Peak power                                   | 53 kW                           |
| Continuous power                             | 30 kW                           |
| Battery nominal operating voltage            | 200–450 V @ 400A <sub>rms</sub> |
|  | max                             |
| Motor fundamental electric frequency (max)   | 1000 Hz                         |
| Efficiency (10–100% speed, 20% rated torque) | 93%                             |
| Electric motor/speed reducer mass            | 35 kg                           |
| Electric motor/speed volume                  | 11 liters                       |

#### Table B.1. Targets for the AEMD program

As summarized in this appendix, a CRADA member facility evaluated a conventional induction machine, a low-cost induction machine, an outer-rotor PM machine, and a SRM. The estimated

performance comparison of the machines, summarized in Table B.2, shows that the PM machine exhibited superior efficiency at the rated speed point and at both full-rated torque and 20% torque. However, the high-speed, part-load efficiency of the PM machine was lower than for the other machines. The table indicates that the PM machine has a significant advantage in packaging, as reflected in the measures of stack length and mass. All the machines were designed to meet packaging requirements for the program. The ac rms phase current necessary to meet the rated motoring point was similar among the designs, with the PM machine requiring the least current. The induction machine represents the lowest risk because the technology is very well understood. Both the induction and SRM machines can potentially be constructed from low-cost and easily manufactured components.

| Parameter                      | Induction | <b>Outer-rotor PM</b> | SRM  |
|--------------------------------|-----------|-----------------------|------|
| Efficiency @ rated power and   | 85.7      | 94.4                  | 82.3 |
| 1600 rpm, %                    |           |                       |      |
| Efficiency @ 20% rated power   | 87.6      | 95.7                  | 79.4 |
| and 1600 rpm, %                |           |                       |      |
| Stack length, mm               | 71        | 45                    | 80   |
| Active material mass, kg       | 18.6      | 12.8                  | 18.7 |
| Max rms phase current@ rated   | 185       | 155                   | 205  |
| torque/speed, A <sub>rms</sub> |           |                       |      |
| Relative risk                  | Low       | High                  | High |
| Machine cost                   | Low       | High                  | Low  |

Table B.2. Comparison of selected performance parameters for AEMD Team 1 machines

## **B.2 PARALLEL INDUCTION MACHINE**

A conventional machine for parallel hybrid vehicles was designed and tested by AEMD Team 1. In addition, a means was sought to give this very mature technology an additional competitive edge in cost, especially in light of less-than-favorable packaging requirements. Therefore, it was decided that certain low-cost design and manufacturing changes would be explored to see what effect, if any, they might have on performance. This effort produced a low-cost design that was similarly tested. Although both designs include a power generation capability, the emphasis in this project summary will be on the motoring capability, since only motoring is of interest in the present series HEV study.

## **B.2.1** Conventional Design

Since the induction machine was being designed for a potential parallel hybrid vehicle application, the geometry was driven by packaging constraints. It was not unexpected that the geometry constraints were related to machine cost. The packaging requirements dictated a large inner diameter, large ratio of machine OD to inner diameter, and short stack length. These geometry constraints led to a machine design having a high pole number. With stamped laminations in the rotor, the same constraints led to high material scrap during rotor manufacturing; this problem is addressed in the low-cost design (see Sect. B.2.2). The machine design also contained some compromises in the interest of the regenerative mode performance, which was an AEMD requirement. The conventional machine design was completed using common 26-gage, M-36 silicon steel. A design optimization parametric study was completed showing the trade-offs in performance as a function of geometry. This study used a AEMD Team 1 proprietary design program that implements a Monte Carlo design synthesis routine, where machine parameters are varied over a range of interest and machine performance parameters are calculated and tabulated. The AEMD requirements indicate that the efficiency at 20% load, from 10–100% speed, should be 93%. The Team 1 modeling study showed that this was not attainable at the load points selected, given the machine packaging constraints. Using a similar approach, parameters such as mass, electrical generation, and inertia were evaluated.

The design process continued until it arrived at the design geometry summarized in Table B.3.

| Stator             |       |
|--------------------|-------|
| Outer diameter, mm | 360   |
| Inner diameter, mm | 318.6 |
| Stack length, mm   | 71    |
| Stator slots       | 96    |
| Stator winding     |       |
| Turns per coil     | 5     |
| Parallel paths     | 4     |
| Strands            | 4     |
| AWG                | 18.5  |
| Rotor              |       |
| Inner diameter, mm | 285   |
| Outer diameter, mm | 317   |
| Stack length, mm   | 71    |
| Slots              | 144   |

Table B.3. Design geometry of the conventional induction machine

Testing the machine in the motoring mode at 267 Vdc, the machine showed good full-load efficiency characteristics,  $\sim$ 90% or above, over a broad speed range from 2500–5500 rpm. While still in the motoring mode, the efficiency testing at 20% load torque resulted in a >90% efficiency from 3000–6000 rpm; however, this fell short of the AEMD performance goal.

## **B.2.2 Low-Cost Design**

Team 1 took mature and well-understood induction machine technology and explored the adaptation of certain low-cost manufacturing processes such as the use of a powdered iron rotor with a segmented stator. Team 1 also reduced the rotor slot combination and controlled the form factor to facilitate the powder metal press operation. Although the performance analysis ultimately favored the conventional design, certain low-cost techniques, such as the use of segmented or slinky laminations, showed promise with little degradation in performance. Less promising in the near term was the powdered iron rotor, which exhibited a lower material saturation level than laminated electrical steels.

The design study relied on the Team 1 Proprietary Induction Machine Design Program. Key design variables were varied over predetermined ranges to identify trends and design limitations.

The low-cost design made use of 26-gage, M36 silicon steel for the stator, with modifications to the loss characteristics to account for additional iron losses due to low-cost manufacturing processes such as a slinky- or helically-wound stators or segmented stators with numerous welds.

The rotor design called for the use of 45-P sintered powdered iron rotor material. The material exhibits resistivity that is 30 times higher than in silicon steel, but it is not laminated as is silicon steel. The 45-P material has a lower saturation flux density and has generally lower permeability than silicon steel.

The design process continued until it arrived at the design geometry summarized in Table B.4. The parameters for the conventional design are repeated in Column 3 from the previous table for comparison purposes. Note that the low-cost design required a greater stack length than the conventional design.

| Stator             | Low cost | Conventional |
|--------------------|----------|--------------|
| Outer diameter, mm | 360      | same         |
| Inner diameter, mm | 317.4    | 318.6        |
| Stack length, mm   | 78       | 71           |
| Stator slots       | 96       | same         |
| Stator winding     |          |              |
| Turns per coil     | 9        | 5            |
| Parallel paths     | 8        | 4            |
| Strands            | 3        | 4            |
| AWG                | 20       | 18.5         |
| Rotor              |          |              |
| Inner diameter, mm | 285      | same         |
| Outer diameter, mm | 315.9    | 317          |
| Stack length, mm   | 78       | 71           |
| Slots              | 112      | 144          |

Table B.4. Design geometry of the low-cost induction machine

The low-cost machine performance relative to the specifications must be weighed against the ac current requirements in both the motoring and generating modes.

The machine peak torque vs. speed profile at 267 Vdc shows that the performance goals were met over the entire range of speeds specified. If higher current was permitted, the machine would be able to provide additional torque over most of the speed range. A maximum rms phase current of  $\sim$ 190 A was required to provide 180 Nm of shaft torque.

The machine efficiency vs. speed profile at peak torque at 267 Vdc shows that the machine efficiency was ~90% from 2500–6000 rpm. Under the same conditions, but at 20% torque, the target efficiency of 93% could not be met given the geometry and fundamental frequency constraints. The efficiency of the low-cost machine was still quite respectable at >90% from ~2700–6000 rpm and was almost as high as for the conventional induction motor.

Both the conventional design and the low-cost design were able to meet torque and speed requirements. However, the low-cost design required a 10% larger stack size, while opportunities exist for applying low-cost fabrication techniques such as laminated rotors to the conventional

design. There was also a slight efficiency loss (1%) in the low-cost design at 20% rated load. Therefore, it was concluded that the conventional machine was the most attractive design option.

## **B.3 OUTER ROTOR PM MACHINE**

The Team 1 proof-of-concept testing focused on a series, outer-rotor, PM machine that featured coaxial shaft output. The testing of this machine was both rigorous and comprehensive. Overall, the project is designed to proceed through four discrete stages: (1) initial testing of the proof-of-concept machine, (2) design changes, (3) hybrid GAP analysis, and (4) risk assessment. Each of these is discussed below.

The original machine design is designated the proof-of-concept machine because it demonstrates a design concept developed during the modeling phase. The subsequent modified design is considered to be the "deliverable" design, and a future third design will encompass certain other changes such as a single-shaft output. These three designs are summarized in Table B.5.

| Subassembly       | POC                | Deliverable          | Future                        |
|-------------------|--------------------|----------------------|-------------------------------|
| Laminations       | 26 gage, M36       | 29 gage, M15         | 29 gage, M15                  |
| Winding           | 3 coils/phase      | 6 coils/phase        | 6 coils/phase                 |
| Magnets           | 18 segment arcs    | 30 segment arcs      | Tile magnets                  |
| Rotor material    | Solid steel        | Solid/laminated      | Solid/laminated               |
| Housings          | Slip fit stator to | Shrink fit stator to | Eliminate 1 of 3 housings and |
|                   | housing            | housing              | simplify design               |
| Gearing on output | Dual output        | Dual output          | Single output                 |
|                   | Double reduction   | Double reduction     | Single reduction              |
|                   | 10:1 ratio         | 8.5:1 ratio          | 3:1 ratio                     |
| Shafts and hubs   | -                  | -                    | Eliminate 3 shafts            |
| Bearings          | -                  | -                    | Eliminate several bearings    |

#### Table B.5. Summary of design changes for the AEMD Team 1 outer-rotor PM machine

The testing activities and design changes are summarized as follows:

- Initial test results—The back-emf and core loss correlated well with model predictions. Efficiency was higher than predicted because of an error in the loss prediction calculation. Torque data were obtained from motor operation at several different speeds. Test results showed that the machine speed apparently is limited by the material selection for the motor. The rotor experienced rapid heating starting at ~7000 rpm, and rotor demagnetization occurred as a result of excessive heating at 9000 rpm.
- 2. Design changes—Changes were necessitated by the need to improve performance and update cost estimates. Changes to improve performance included laminating the rotor to reduce rotor core losses, using a salient pole winding to reduce rotor harmonics, increasing the number of magnet segments to reduce magnet losses, changing the lamination steel to 29-gage M-15 to reduce stator core loss, reducing the gear ratio to 8.5:1 to minimize friction and windage losses and oil drag losses, and shrink-fitting the stator to the housing to reduce the thermal resistance.

- 3. Gap analysis—This analysis compared the ambitious target goals of the FreedomCAR program with actual or predicted performance of the proof-of-concept, deliverable, and future machine designs. The future machine design is predicted to have some areas of deviation from the performance and physical target specifications. These deviations are primarily in the areas of current (slight deviation of +15A), frequency (+200 Hz), vehicle speed above 77 mph, efficiency at >50% speed, mass (slight deviation of <4 kg), and cost (\$70). The EETT had agreed to increase drive frequency prior to this analysis. Targets are predicted to be fully met for torque at the driveshaft and machine volume.</p>
- 4. Risk assessment—Each of the changes needed to produce the future design was considered relative to program risk. In all, 15 changes affecting 7 subassemblies were predicted, and the risk was deemed "low" for each change with one exception. The exception is a high risk for replacing segmented and bonded magnets with as-pressed bar magnets while adopting a new high-speed assembly process.

The configuration of the deliverable series electric machine that was tested included a single reduction gear assembly. Torque vs. speed mapping of the machine was performed with dc link voltages of 325 and 200 Vdc. The machine was tested from 500 rpm to 12,000 rpm in intervals of 500 rpm with torque loads of 100%, 80%, 60%, 40%, and 20% and of 10% rated torque.

The deliverable series machine met the continuous and peak mechanical power goals from 3,000–12,000 rpm with the minimal dc link voltage, 200 Vdc. The machine met the peak torque requirement of 596 Nm from approximately 500–2500 rpm during the tests with a dc link voltage of 325 Vdc. The machine-demonstrated efficiencies of  $\geq$  93% from 2997–6003 rpm with mechanical loads  $\geq$  30 kW and from 3500–6001 rpm with mechanical power levels  $\geq$  55 kW with the minimal dc link voltage. The machine had slightly higher efficiencies when operated with the dc link voltage of 325 Vdc when compared to 200 Vdc. At mechanical power levels  $\geq$  55 kW, the machine demonstrated efficiencies of  $\geq$  93% from 3511–7507 rpm and  $\geq$  90% from 2496–9528 rpm with a dc link voltage of 325 Vdc.

## **B.4 SWITCHED RELUCTANCE MOTOR**

Team 1 considered a concentrated-winding SRM appropriate for a potential parallel hybrid vehicle application since it is predicted to have high performance over a wide speed range. A number of full-pitched configurations were also considered, including machines based on a unipolar, 120° conduction configuration and SRMs using a conventional inverter topology of 120° conduction and 180° conduction. Full-pitched machines are unique in that they generate torque from changing mutual inductance instead of from changing the self-inductance characteristic of the conventional concentrated coil machines. The full-pitch winding was used to reduce copper loss below base speed (given that more of the copper is utilized at any given time), but this approach led to high self-inductance, which tends to be exhibited by these machines.

The advantages of low-cost materials and simplicity of construction for which SRMs are known must be weighed against certain inherent drawbacks. One of these is machine size; however, this drawback was driven partly by the need for low-speed generation requirements that does not apply to the present study on a series application motor. The risk of continuing to pursue this technology is high also because of the following:

- 1. Machine efficiency significantly below the target at 20% load, over the speed range
- 2. Questions regarding the selection/packaging of the position sensor
- 3. The need to mitigate acoustic noise and transmitted vibration
- 4. The complexity of integrating the machine with an appropriate drive topology

# APPENDIX C: SUMMARY OF THE AEMD TEAM 2 AXIAL-GAP MOTOR STUDY

A multi-party team recommend an axial-gap traction motor system in support of AEMD's development program for a future series hybrid vehicle (SHV) configuration. Several iron-filled and ironless axial-gap PM BDCM and controller combinations were analyzed. Most combinations for this study were eliminated because of incompatibilities or a determination that the technology did not warrant extensive evaluation. This study summary presents the results from analyzing the leading motor/controller candidates.

The axial-gap machine developed by AEMD team 2 experienced thermal problems when operated continuously. The cooling strategies for this machine must be significantly improved. This motor has a very limited constant power operating speed range which greatly limits its potential use as a traction drive motor. The machine demonstrated about a 6–8 kW constant power capability.

## C.1. IRON-FILLED AND IRONLESS AXIAL-GAP MACHINE DESIGNS

This section provides a brief discussion of the potential advantages of adding iron to the stators of axial gap machine designs.

## C.1.2. PMBLDC, Axial-Gap, Ironless Motors

The ironless axial-gap PM brushless dc (PMBLDC) machine is able to maintain efficiency on a wider speed range than iron-filled motors because it does not have ac flux return losses. This configuration can also be designed to have a flatter plateau on the torque-speed curve. The ironless motors exhibit zero cogging torque. In general, axial-gap motors have the advantage that there is a potential for designing them with a higher active volume than a radial PM BDCM. This motor configuration also has the advantage of offering a more robust method of magnet retention without impacting performance significantly. Unlike the radial gap PM machine, the axial-gap machine's magnets may be retained by an outer radial lip that does not interfere with the magnetic air gap. However, because there is no flux-carrying member between the magnets, more magnet material is required than in the iron-filled counterparts, penalizing this design for material cost. In addition, because this motor contains no iron in the stator, it has an inductance too low to be compatible with CPA techniques. And because the wire is not shielded by iron, a high-strand-count stranded wire must be used in order to reduce eddy-current losses, impacting material cost.

## C.1.3. PMBLDC, Axial-Gap, Iron-Filled Motors

The most significant benefit of adding iron to the stator of the axial flux machine is that such designs require significantly less magnet material. In addition, introducing iron to the axial-gap PM machine increases inductance, thereby allowing CPA techniques to be employed. The iron-filled motor also has the flexibility of being configured as a stator-rotor-stator design, facilitating cooling of the stator and hence improving power density. However, these benefits do not come without some cost. The addition of iron brings with it significant cogging and ac flux return

losses, causing a slight reduction in efficiency. Even with these concerns, the system may offer the greatest potential for meeting the performance goals with improved cooling.

#### C.1.4. Iron-Filled vs. Ironless Axial-Gap Motors

The preferred method for addition of iron was determined to be through the use of iron-filled epoxy (IFE). It allows a very specific and controlled percentage of iron fill to be added to the motor. For purposes of comparison, an ironless motor design with similar power and speed characteristics was compared with a 15-kW 75% IFE motor design. Some of the most important variables are shown in Table C.1.

|                                    | 0% Fill | 75% Fill | Change | % Ironless |
|------------------------------------|---------|----------|--------|------------|
| Parameters                         |         |          | 0      |            |
| Performance                        |         |          |        |            |
| Output power, kW                   | 15      | 15       | 0      | 100.0%     |
| Rated speed, rpm                   | 3600    | 3600     | 0      | 100.0%     |
| Efficiency at rated torque, %      | 96.3    | 92.3     | -4     | 95.8%      |
| Efficiency at 20% rated torque, %  | 97.4    | 97.7     | 0.3    | 100.3%     |
| Dimensions                         |         |          |        |            |
| Outer motor diam (est.), mm        | 291.8   | 210.3    | -81.5  | 72.1%      |
| Outer motor vol (est.), Liter      | 4.319   | 2.621    | -1.698 | 60.7%      |
| Weights                            |         |          |        |            |
| Magnets, kg                        | 2.146   | 1.041    | -1.105 | 48.5%      |
| Copper in coils, kg                | 2.257   | 0.985    | -1.272 | 43.6%      |
| Iron in the stator, kg             | 0       | 0.668    | 0.668  |            |
| Flux return, kg                    | 2.481   | 2.824    | 0.343  | 113.8%     |
| Motor (est.), kg                   | 9.294   | 7.448    | -1.846 | 80.1%      |
| Losses (at rated torque)           |         |          |        |            |
| Copper, watts                      | 517.70  | 980      | 462.3  | 189.3%     |
| Core loss in IFE, watts            | 0       | 157      | 157    |            |
| Eddy currents loss in coils, watts | 28.98   | 48       | 19.02  | 165.6%     |
| Eddy currents loss in PM, watts    | 0       | 55       | 55     |            |
| Mechanical, watts                  | 28.3    | 28.3     | 0      | 0.0%       |
| Total losses, watts                | 575.01  | 1268.4   | 693.39 | 220.6%     |

Table C.1. Ironless motor comparison with 75% iron-filled motor

The IFE motor design is decidedly advantageous in the areas of copper and magnet material mass, motor diameter, and total motor volume. At partial power (up to about 25% rated power at 100% rated speed), the IFE motor is also competitive from an efficiency standpoint. In areas above 25% rated power, the ironless motor has a substantial advantage over the IFE machine. Higher currents were designed into this machine because the higher copper density and lower thermal resistance associated with the use of magnet wire, as opposed to Litz wire, allowed much higher thermal dissipation capabilities in the IFE machine. The impact of additional iron on the machine appears to be an approximately 50% reduction in the machine cost with a 4% drop in efficiency at 100% rated load at 100% rated speed. It is anticipated that the motor could be designed to achieve 93% efficiency over a very broad speed range by reducing the phase current with a slight increase in magnet material. Further analysis is required at the vehicle system level to determine the overall impact on vehicle system efficiency, based on anticipated real-world operating points derived from typical driving cycles. If the motor is run for significant periods of

time at partial load, the impact of this efficiency differential may be less significant than the associated cost benefits.

## C.2. MACHINE SYSTEMS FOR COMPARATIVE ANALYSIS

This section describes a baseline radial-gap machine design and five axial-gap machine configurations that were compared in the AEMD Team 2 study.

## C.2.1. System 1 (Baseline): PMBLDC Radial Gap CPA Motor System

For comparison, a representative PM, radial gap design motor was selected, primarily because it is the only technology currently used in production HEVs such as the Toyota Prius. Specifically, the Model EV53 motor from UQM Technologies, Inc., was selected because it is also commercially available and detailed information about the motor is readily available.

## C.2.2. System 2: Ironless PMBLDC Axial-Gap DMIC Motor System Loss and Cost Analysis

The ironless (DMIC) motor design is intended for use with a conventional variable-frequency inverter using CPA. In addition to the conventional inverter, a DMIC add-on is included to block the extremely high diode currents that the ironless motor would see above the base speed. Without the DMIC addition, this particular motor would be usable over a very small (no more that 2:1) CPSR. In this design, the motor's base speed is equal to the peak motor speed divided by the CPSR, as in any CPA design. The addition of DMIC allows the motor to be sized thermally for the rated power rather than for the elevated current levels typically experienced in a CPA control scheme. This motor has a substantially higher peak torque capability than a similar iron-filled machine. The DMIC motor design has slightly higher peak efficiency, with the entire peak efficiency plateau occurring within the motor's normal operating range. Of all the axial flux motors modeled, the ironless DMIC motor is the most expensive solution. The cost is primarily due to the higher magnet mass required because of the lower winding turn count and low base speed required in this approach. The advantage of this approach is that a CPSR much greater than 5:1 could be achieved (potentially 10:1 or greater with proper design) because of the current-blocking capabilities of the DMIC and the low-speed-related losses in the ironless motor design.

## C.2.3. System 3: Ironless PMBLDC Axial-Gap H-Bridge Motor System Loss and Cost Analysis

The ironless PMBLDC H-bridge motor was designed to be used with an inverter using oversized current switches. In this system, a CPSR capability is approximated by designing the motor to have a base speed equal to the system's max speed with a continuous rated torque capable of providing 30 kW at a speed equal to the peak speed divided by the CPSR. This motor has a substantially higher torque capability at the peak speed, but most of the plateau defining the peak efficiency falls outside the normal operating torque/speed range. Of the ironless motors studied, the H-bridge concept resulted in the lowest motor cost. At a system level, this cost is offset by

the cost of the higher switch ratings required for the high continuous current required at low speed.

# C.2.4. Systems 4 and 5: Iron-Filled PMBLDC Axial-Gap DMIC/CPA Motor System Loss and Cost Analysis

The iron-filled DMIC motor is very similar to the ironless DMIC motor, except that it can also be operated using a variable-frequency inverter using CPA without DMIC and still achieve a significant CPSR. This is a distinct cost advantage at the system level because of the simple inverter architecture that can be used. The addition of iron affects the DMIC motor in much the same way that it affected the iron-filled H-bridge motor. The general behavior is very similar to that of the ironless machine, with the peak efficiency plateau roughly 3% lower than the ironless version of the motor.

The iron-filled DMIC motor cost is approximately 33% above the cost of the iron-filled H-bridge motor. At a system level, this difference changes significantly as a result of the capability to use a standard variable-frequency inverter. This approach will likely lead to a motor that will be only slightly over the AEMD specification for mass and volume. Overall, this motor is a likely candidate for future work, although a fully dense iron-filled motor would possibly be a more appealing approach. Because of the capabilities of the DMIC, it is likely that this motor would look substantially different depending on whether the system uses CPA with DMIC, or CPA without DMIC. In the case of the DMIC-based approach, a partial iron fill would be used to reduce mass, volume, and cost; but a fully dense iron fill would not be used to reduce the spin-related losses that will ultimately limit the CPSR of the DMIC approach. On the other hand, a strictly CPA approach with a variable-frequency inverter would likely result in a fully dense iron-filled motor to reduce the diode currents above base speed.

## C.2.5. System 6: Iron-Filled PMBLDC Axial-Gap H-Bridge Motor System Loss and Cost Analysis

The iron-filled H-bridge motor was scaled from the ironless design using FEA results from earlier 75% iron-filled epoxy FEA. Functionally, the motor is nearly identical to the ironless H-bridge motor. The primary performance difference between the ironless and iron-filled motors is the peak efficiency of the machine. The behavior of the efficiency map is very similar to that in the ironless machine, but the peak efficiency plateau is approximately 3% lower. This results in a substantially higher thermal dissipation requirement. Shielding of the wire by the iron allows the use of very low strand count magnet wire (or solid magnet wire, in the case of fully dense iron fill), which greatly increases the thermal conductivity in the radial direction. This higher thermal conductivity allows the motor to operate at the lower efficiency point and can substantially shrink the motor diameter as well. From a motor cost standpoint, this is the least expensive solution studied. As with the earlier ironless H-bridge motor, however, the switch ratings of the inverter must be increased above those of a CPA inverter by the base rating times the CPSR required.

## C.2.6. Rotor/Stator/Rotor vs. Stator/Rotor/Stator Construction of Axial-Gap Motors

One area that warrants further research is the configuration of rotor and stator relative to each other in the machine. For ironless machines, the only configuration that is reasonable for single-slice, power-dense, axial-gap motors is a single stator between two rotors (rotor-stator-rotor, or RSR). In single-slice iron-filled axial-gap machines, however, it is possible to configure the motor with two stators with a rotor between them or two rotors with a stator between them. Both machines have similar losses associated with them, but this tradeoff offers several other items for consideration:

- The stator-rotor-stator (SRS) configuration offers simple cooling passage architectures (passages do not have to be integrated into the stator platter) because one face of each stator is exposed to the housing directly. This offers the advantages of a higher power density and lower machine temperature.
- SRS motors can be designed with a higher active volume using conventional magnet wire windings because no offset of the magnet face to accommodate the inner edge turns is required on the rotor.
- The SRS design affords a lighter rotor design for high-speed operation because of the elimination of the need to accommodate the inner edge turns with a rotor offset.
- Based on previous motor designs, it is anticipated that the SRS configuration would most likely result in higher axial loading of the bearings in cases where the rotor is slightly off-center, or skewed, relative to the stators. Further research is required to quantify the impact of this loading on the machine design.

## **C.3. SYSTEM COMPARISON**

A Pugh analysis was used in comparing the machine designs. This analysis qualitatively rates machine characteristics as better (+), worse (-), or the same (0) as the baseline. Table C.2 lists the comparison results from the Pugh analysis. In this case, superior (S) was added as another comparative measure, and it can even apply to the base case if the base case ranks with the best of all designs in the comparison. Based on the summary in the table, the most appealing non-induction motor option appears to be the IGBT inverter system using CPA with the Y-connected machine and some level of iron fill (system four). The primary driver for this selection is the low cost associated with both the inverter and motor.

The second most appealing option, based on the Pugh tradeoff and cost analysis, is the DMICbased system (the fifth system in the table). Although cost analysis of currently available silicon devices appeared to indicate that the sixth system would be less costly because of a lower motor cost, research indicates that the silicon-controlled rectifier devices of the fourth system could be substantially less costly than system five's substantially larger current switches. With proper design, system five also offers an opportunity to substantially improve the CPSR over the baseline system as well as systems three, four, and six.

| System                                     | 1 (Baseline)               | 2                                       | 3                                       | 4  | 5  | 6  |
|--|----------------------------|---|---|--|--|--|
| Motor<br>description                       | PMBLDC<br>radial gap       | PMBLDC<br>axial-gap<br>RSR,<br>ironless | PMBLDC<br>axial-gap<br>RSR,<br>ironless | PMBLDC<br>axial-gap<br>RSR or<br>SRS, iron<br>filled | PMBLDC<br>axial-gap<br>RSR or<br>SRS, iron<br>filled | PMBLDC<br>axial-gap<br>RSR or<br>SRS, iron<br>filled |
| Winding configuration                      | 3-phase<br>Y-<br>connected | 3-phase<br>Y-<br>connected              | 3-phase H-<br>bridge                    | 3-phase<br>Y-<br>connected                           | 3-phase<br>Y-<br>connected                           | 3-phase H-<br>bridge                                 |
| Switch type                                | IGBT                       | IGBT                                    | MOSFET                                  | IGBT   | IGBT   | MOSFET   |
| Inverter add-<br>ons                       | СРА                        | DMIC                                    | Current<br>weakened                     | СРА  | DMIC   | Current<br>weakened                                  |
| Gear reduction                             | Yes                        | Yes                                     | Yes                                     | Yes  | Yes  | Yes  |
| Peak power<br>ratio                        | 1.66                       | +                                       | +                                       | S  | +  | S  |
| Peak power                                 | 53 kW                      | +                                       | +                                       | S  | +  | +  |
| Peak torque                                | 240 Nm                     | +                                       | +                                       | S  | +  | +  |
| Continuous<br>torque                       | 150 Nm                     | S                                       | S                                       | S  | S  | +  |
| System weight                              | 53.1 kg                    | S                                       | +                                       | +  | +  | +  |
| System volume                              | S                          | -                                       | +                                       | +  | +  | +  |
| CPSR                                       | 3.7:1                      | +                                       | S                                       | S  | +  | S  |
| System efficiency                          | 90/94                      | +/-                                     | +/S                                     | S/S  | S/-  | +/-  |
| Motor torque<br>ripple                     | Low                        | +                                       | +                                       | -  | -  | -  |
| System fault tolerance                     | Fair                       | +                                       | +                                       | S  | +  | +  |
| System cost in<br>volumes of<br>250 k/year | S                          | -                                       | -                                       | S  | -  | -  |
| System<br>development                      | S                          | -                                       | S                                       | -  | -  | -  |
| System<br>material cost                    | S                          | -                                       | -                                       | S  | -  | -  |
| System mfg<br>cost                         | S                          | S                                       | +                                       | S  | -  | -  |

Table C.2. Pugh analysis results for the baseline and axial gap motor designs

MOSFET = metal oxide semiconductor field effect transistor

#### C.4. SUGGESTIONS FOR CONTINUING MOTOR TECHNOLOGY RESEARCH

The suggested motor architecture for future development is the axial-gap PM BDCM. This was based on the expectation that, properly implemented, this configuration offers a superior solution to other high-technology motor designs under development from a standpoint of weight, volume, and efficiency. It is further believed that with certain improvements, this technology can also be made cost-competitive with these other options. The primary finding related to this motor type was that in order to meet cost objectives using PMBLDC technology, it is necessary to use some level of iron fill in the motor to reduce magnet cost. The amount and procedure for the added

iron was not finalized during this study and will require further development. The amount could vary from a 30% by volume IFE to a fully dense iron stator structure. The amount of iron added and the procedure for accomplishing the effort will require new model development and substantial manufacturing process research.

Another significant factor related to PMBLDC machines is that the cooling strategies related to this motor must be significantly improved. If fully dense iron stator construction is used, it is worthwhile to study the SRS construction discussed earlier. Using this approach would afford a simple method of adding external cooling passages for each of the stators. This solution would not be useful if the approach chosen were fractional iron fill through use of IFE. Another potential approach would be use of an oil spray cooling technique similar to that used in some large generator and motor applications. Use of such a system would help reduce magnet and coil temperature significantly, which would in turn reduce the required magnet materials and greatly improve the power density of the machine. This type of system would also allow the use of a number of different bearing options as a result of the capability to oil-lubricate bearings and eliminate the need for a sealed bearing. Seal drag and windage loss in the bearing set due to the high viscosity grease used are significant contributors to motor efficiency losses. A change to this type of cooling/lubricant system would greatly improve losses in this area.

One of the primary limitations in the use of this motor type was determined to be the lack of an inherent constant power operation capability. This study revealed no technologies that would significantly enhance this feature without modification to the inverter, control technique, or fundamental motor architecture. An area not covered by this study that has been identified for potential future study is the effect of changes to the motor that would perform either field weakening by mechanical means or variable winding geometry that can be changed during use.

# APPENDIX D: PARAMETER DEFINITIONS FOR SPEEDCAD MODEL

This appendix illustrates, lists, and defines parameters used in the SPEEDCAD model. Figure D.1 illustrates many of the physical parameters used in the model. The figure makes use of an IPM rotor and stator configuration with the shaft center point on the left-hand side.



Fig. D.1. Physical parameters used in the SPEEDCAD model (IPM machine).

The summary tables in this appendix segregate the full set of parameter types/definitions by the following categories:

Table D.1 – Dimensions Table D.2 – Magnet data Table D.3 – Control data Table D.4 – Winding data TBD Table D.5 – Magnet circuit design TBD Table D.6 – Steady state thermal model TBD

The parameter names above are listed in alphabetical order. The tables are intended to provide a quick and concise definition of a large number of parameters. More complete definitions of parameters can be found in the Motorsoft *User's Manual*.<sup>10</sup>

| Variable<br>name | Description   | Default<br>units |
|------------------|---|------------------|
| AmagSlot         | ptReal Area of one magnet slot in IPM lamination                        | mm^2             |
| BetaM            | ptReal Magnet pole arc [mDeg]   | mDeg             |
| Bridge           | ptReal IPM bridge   | mm               |
| BSlit            | ptReal Lam. width at inner end of rotor slits                           | mm               |
| DHub             | ptReal Rotor hub width, measured along the d-axis                       | mm               |
| Embed            | ptList Embedded magnet type   |                  |
| Gap              | ptReal Airgap length  | mm               |
| hq               | ptReal Radial depth of pole-piece; q-axis cross-flux goes through it    | mm               |
| IPMHq            | ptReal Depth of pole cap, measured along d-axis                         | mm               |
| LM               | ptReal Thickness of magnet in the direction of magnetization            | mm               |
| LM_min           | ptReal Smallest length through one magnet in direction of magnetization | mm               |
| Lrotor           | ptReal Effective rotor length   | mm               |
| LShaft           | ptReal Shaft length   | mm               |
| Lstk             | ptReal Stack length   | mm               |
| Lweb             | ptReal Radial length of web in IPM Embed type 4                         | mm               |
| MagWid           | ptReal Magnet width in spoke-type rotor                                 | mm               |
| MEdge            | ptReal Magnet edge  | mm               |
| MOH              | ptReal Magnet overhang at each end of the rotor                         | mm               |
| MslotWid         | ptReal Magnet slot width in IPM rotor                                   | mm               |
| Nmbp             | ptInteger Number of magnet blocks per pole                              |                  |
| Poles            | ptInteger Number of poles   |                  |
| Rad1             | ptReal Rotor radius   | mm               |
| Rad2             | ptReal Radius to stator slot bottom                                     | mm               |
| Rad3             | ptReal Stator outer radius  | mm               |
| RadSH            | ptReal Shaft radius   | mm               |
| RotorOD          | ptReal Rotor OD   | mm               |
| RotType          | ptList Rotor type   |                  |
| RYoke            | ptReal Radial thickness of the rotor yoke                               | mm               |
| SD               | ptReal Slot depth (NB. from slot bottom to stator bore)                 | mm               |
| Skew             | ptReal Stator skew [slot pitches]                                       |                  |
| Slits            | ptList Rotor has slits or not   |                  |
| Slots            | ptInteger Number of stator slots  |                  |
| SO               | ptReal Slot opening   | mm               |
| SOAng            | ptReal Undercut angle of stator tooth tip (slot opening)                | mDeg             |
| S-Slot           | ptList Slot shape (round or square bottom, or Pll. slot)                |                  |
| StatorOD         | ptReal Stator lamination OD   | mm               |
| Stf              | ptReal Lamination stacking factor                                       |                  |
| SYoke            | ptReal Radial thickness of the stator voke                              | mm               |
| TGD              | ptReal Radial depth of stator tooth tip (slot opening depth)            | mm               |
| TSlit            | ptReal Lam. width at outer end of rotor slits                           | mm               |
| TWS              | ptReal Stator tooth width   | mm               |
| Web              | ptReal IPM web  | mm               |
| wMag             | ptReal Width of magnet  | mm               |
| WSlit            | ptReal Width of rotor slits   | mm               |

| Table D.1. | SPEEDCAD | parameters relating to machine dimensions          |
|------------|----------|--|
|            |          | pur uniteres i enuering to indennite uniterestoris |

| Variable<br>name | Description                           | Default<br>Units |
|------------------|---------------------------------------|------------------|
| Br               | ptReal Magnet remanence at 20°C       | Т                |
| CBr              | ptReal Temperature coefficient of Br  | %/DegC           |
| СНс              | ptReal Temperature coefficient of HcJ | %/DegC           |
| DMag             | ptReal Density of magnet material     | kg/m3            |
| Нс               | ptReal Intrinsic coercivity           | kA/m             |
| MuRec            | ptReal Recoil permeability            |                  |

## Table D.2. SPEEDCAD parameters relating to the magnets

## Table D.3. SPEEDCAD parameters relating to control data

| Variable<br>name | Description   | Default<br>Units |
|------------------|---|------------------|
| da0              | ptBoolean da() equations (sinewound three-phase wye only)                   |                  |
| Drive            | ptList Sine/square wave or AC volt drive                                    |                  |
| DuCy             | ptReal Voltage-PWM duty cycle [0-1]   |                  |
| EMFCalc          | ptList Method of EMF calculation  |                  |
| fChop            | ptReal Voltage-PWM chopping frequency [kHz]                                 | kHz              |
| fChopAct         | ptReal Chopping frequency calculated from actual No. of chops               | kHz              |
| FixfChop         | ptList Is a fixed chopping frequency used (Yes/No)                          |                  |
| Freq1            | ptReal Fundamental frequency  | Hz               |
| gamma            | ptReal The phase angle between Iph1 and the q-axis (Eq1) [deg]              | deg              |
| HB%              | ptReal Width of hysteresis band as a percentage of ISP                      |                  |
| HBA_act          | ptReal Actual value of hysteresis band adjustment (HBA) used in calculation |                  |
| HBtype           | ptList Constant or variable hysteresis band width (sine-wave)               |                  |
| ISLA_Act         | ptReal Value of integration step length (ISLA) used to form solution        |                  |
| ISP              | ptReal Current regulator set-point current                                  | А                |
| ISP_Act          | ptReal Value of set point current (ISP) used to form solution               | А                |
| RPM              | ptReal Speed [rpm]  | rpm              |
| Rq               | ptReal On-state resistance of one transistor {ohms}                         | ohm              |
| Sw_Ctl           | ptList Voltage PWM/current hysteresis control                               |                  |
| t_q              | ptReal Transistor switching time [us]                                       | us               |
| Tol_Act          | ptReal Value of tolerance (Tol) used to form solution                       |                  |
| Vd               | ptReal Forward voltage drop of one diode                                    | V                |
| Vq               | ptReal Forward voltage drop in one transistor                               | V                |
| Vs               | ptReal dc supply voltage to the controller                                  | V                |
| X_EMF            | ptReal Adjustment factor for back EMF                                       |                  |
| XBgap            | ptReal Old emf adjustment factor. From v.6 set=1 and use X_EMF instead      |                  |
| XL               | ptReal Adjustment factor for inductance                                     |                  |

## APPENDIX E: FIELD-WEAKENING TECHNIQUES FOR SURFACE-MOUNTED PM MOTORS

An important attribute of traction drives is that they provide a wide constant power speed ratio (CPSR). In this discussion, CPSR is defined as the ratio of the highest speed at which rated power can be developed, to the lowest speed at which rated power can be developed while operating within the motor's rated current. The lowest rotor rpm at which rated power can be developed is referred to as base speed,  $N_b$ . Relative rotor speed, denoted as n, is the ratio of the rotor rpm, N, to the base speed.

PM motors lack a dedicated field winding; consequently, operation in a constant power mode above base speed must be achieved through appropriate control of the inverter that supplies the armature winding. The control achieved is not "field weakening" per se, but the effect is functionally similar to reducing the current in the field winding of classical doubly fed machines, such as the wound rotor synchronous motor.

The armature winding of PM motors with surface-mounted magnets can be distributed so as to achieve a sinusoidal back-emf or concentrated to achieve a trapezoidal back-emf. Machines with sinusoidal back-emf are commonly referred to as PM synchronous motors (PMSMs), while those with trapezoidal back-emf are called brushless dc motors (BDCMs). The field weakening of these two classes is discussed separately. The discussion is condensed from several references [A–Z]. For both the sinusoidal and trapezoidal back-emf wave shapes, the primary factor limiting the ability of the motor to operate over a wide CPSR is the armature winding inductance. Explicit formulas are given for each machine type to show the limitation that inductance places on CPSR.

The analysis neglects second-order effects such as speed-sensitive losses, which include friction, windage, hysteresis, eddy currents, and skin effect in winding resistance. These speed-sensitive losses will limit the CPSR of any practical motor to a finite value.

The sinusoidal back-emf PMSM is considered first.

#### Impact of Inductance on the CPSR of the PMSM

Figure E.1 shows a schematic of the three-phase PMSM driven by a common variable-speed inverter. The figure also defines the various parameters. The air-gap flux is established by the PM field, and there is no field winding. Thus this machine is singly fed. The line-to-neutral back-emf of the PMSM is sinusoidal, and the motor runs on sinusoidal phase currents. The magnitude of the emf is linear in motor speed; and the voltage constant,  $K_{\nu}$ , with units of rms volts per electrical radian per second, is fixed. Thus the rms value of the back-emf at any speed is given by

$$E = K_{\nu}\Omega$$
  
=  $\frac{\Omega}{\Omega_{b}}K_{\nu}\Omega_{b}$ , (1)  
=  $nE_{b}$ 

where  $E_b$  is the rms magnitude of the line-to-neutral back-emf at base speed and *n* is relative speed. Similarly, the motor reactance can be expressed as

$$X = \Omega L$$
  
=  $\frac{\Omega}{\Omega_b} \Omega_b L$ ,  
=  $nX_b$  (2)

where  $X_{h}$  is the reactance at base speed.



- p = number of poles
- N =actual rotor speed in rpm
- $N_b$  = base speed in rpm

$$n = \text{relative speed} = \frac{N}{N_h}$$

 $\Omega_b$  = base speed in electrical radians/sec

$$= \frac{p}{2} \cdot \frac{2\pi N_b}{60}$$

 $\Omega$  = actual rotor speed in electrical radians/sec

λ7

= 
$$n\Omega_b$$

- $E_b$  = rms magnitude of the phase-to-neutral emf at base speed
- $I_r$  = rated rms motor current
- $P_r$  = rated output power =  $3E_bI_r$
- $L_s$  = self inductance per phase
- $L_o$  = leakage inductance per phase
- M = mutual inductance
- L = equivalent inductance per phase =  $L_o + L_s + M$
- R = winding resistance per phase
- $v_{an}$  = applied phase A to neutral voltage
- $e_{an}$  = phase A to neutral back-emf
- $e_{ab}$  = phase A to phase B back-emf

#### Fig. E.1. Common variable-speed inverter topology and PMSM motor model.

A simplified, per phase, fundamental frequency phasor model of the motor and inverter is shown in Fig. E.2. In the figure,  $\overline{V}$  is the line-to-neutral fundamental frequency voltage phasor applied by the inverter to the motor. The angle of the applied voltage phasor,  $\delta$ , is called the inverter lead angle.  $\overline{E}$  is the back-emf voltage phasor, line-to-neutral, and  $\overline{I}$  is the motor current phasor.



Fig. E.2. AC circuit used in power flow discussion.

Up to base speed, the magnitude of the applied voltage, V, and the lead angle,  $\delta$ , can be adjusted, allowing the motor current phasor to be put in phase with the back-emf. This maximizes the torque produced per ampere. Voltage magnitude V and lead angle  $\delta$ , required to support any relative speed below base speed,  $n \leq 1$ , and rms current, I, are found from

$$\overline{V} = nE_b + I\left(R + jnX_b\right)$$

$$= \sqrt{\left(nE_b + IR\right)^2 + \left(nIX_b\right)^2} e^{j\tan^{-1}\left[\frac{nIX_b}{nE_b + IR}\right]}.$$
(3)

Neglecting the winding resistance, Eq. (3) becomes

$$\overline{V} = nE_b + jnIX_b$$

$$= \sqrt{\left(nE_b\right)^2 + \left(nIX_b\right)^2} e^{j\tan^{-1}\left[\frac{nIX_b}{nE_b}\right]}.$$
(4)

The rms magnitude of  $\overline{V}$  increases with speed and is limited by the available dc supply voltage and the type of modulation used to control the inverter switches. The maximum magnitude is obtained at base speed where n = 1 and at rated rms motor current for which  $I = I_r$ , then

$$V_{\max} = \sqrt{(E_b)^2 + (I_r X_b)^2} = \sqrt{(E_b)^2 + (I_r \Omega_b L)^2} .$$
(5)

Similarly, the lead angle  $\delta$  at base speed and rated current is given by

$$\delta = \tan^{-1} \left( \frac{I_r X_b}{E_b} \right) \,. \tag{6}$$

The power developed at base speed and rated current is the rated power of the motor, and since the current is in phase with the back-emf, we have

$$P_r = 3E_b I_r \tag{7}$$

The dc supply voltage necessary to support operation at base speed and rated current depends on the modulation level allowed in the inverter. If the inverter control scheme is sinusoidal PWM without linear modulation, then the required dc supply voltage is

$$V_{dc} = 2\sqrt{2}V_{\text{max}} , \qquad (8)$$

However, if over-modulation is allowed, a smaller dc supply voltage can be used to obtain the same fundamental frequency voltage,

$$V_{dc} = \frac{\pi V_{\text{max}}}{\sqrt{2}} \,. \tag{9}$$

Let us restrict our attention to operation above base speed such that n > 1 and  $V = V_{max}$ . Neglecting the armature resistance, the phasor current of the motor is

$$\overline{I} = \frac{V_{\max}}{nX_b} \sin \delta + j \left[ \frac{E_b}{X_b} - \frac{V_{\max}}{nX_b} \cos \delta \right],$$
(10)

which has rms magnitude

$$I = \frac{\sqrt{V_{\max}^2 - n2V_{\max}E_b \cos \delta + n^2 E_b^2}}{nX_b} .$$
(11)

The total power injected into the motor by the inverter is

$$\overline{P}_{in} = 3\operatorname{Re}(\overline{V}\ \overline{I}^*) = \frac{3V_{\max}E_b}{X_b}\sin\delta, \qquad (12)$$

while the total power converted by the motor is

$$\overline{P_m} = 3\operatorname{Re}(\overline{EI}^*) = \frac{3V_{\max}E_b}{X_b}\sin\delta \quad .$$
(13)

Since we have neglected the winding resistance,  $P_{in}$  equals  $P_m$  and the common value is

$$P_m = P_{in} = \frac{3V_{\max}E_b}{X_b}\sin\delta.$$
(14)

This expression shows that it is easy to control the motor to deliver rated power above base speed. All that is necessary is that the inverter lead angle,  $\delta$ , be held fixed at that value that causes  $P_m$  in Eq. (14) to be equal to the rated value  $P_r$  given in Eq. (7), that is

$$\delta = \sin^{-1} \left( \frac{X_b P_r}{3V_{\max} E_b} \right)$$

$$= \cos^{-1} \left( \frac{E_b}{V_{\max}} \right)$$
(15)

While constant lead angle control allows the PMSM to operate at constant power above base speed, it is not a certainty that doing so results in operating within the rated current. The critical factor is the motor inductance, as shown below.

Equation (11) gives the rms motor current, I, when operating at any speed above base speed. Using lead angle  $\delta$  from Eq. (15) so that rated power is produced, we require that the rms current in Eq. (11) be no greater than the rated value  $I_r$ , that is

$$I = \frac{\sqrt{V_{\max}^{2} - n2V_{\max}E_{b}\cos\delta + n^{2}E_{b}^{2}}}{nX_{b}} \leq I_{r}$$

$$= \frac{\sqrt{V_{\max}^{2} - n(n-2)E_{b}^{2}}}{nX_{b}} \leq I_{r}$$

$$= \frac{\sqrt{V_{\max}^{2} - n(n-2)E_{b}^{2}}}{n\Omega_{b}L} \leq I_{r}$$
(16)

Evaluating the inequality in Eq. (16) at relative speed n equal to the CPSR yields a minimum requirement on the motor inductance,

$$L_{\min} = \frac{\sqrt{V_{\max}^2 + CPSR(CPSR - 2)E_b^2}}{CPSR \ \Omega_b I_r}.$$
(17)

Since  $V_{\text{max}}$  as given by Eq. (5) depends on L, Eq. (17) has to be applied iteratively to get an exact inductance boundary for fixed values of *CPSR*,  $E_b$ ,  $I_r$ , and  $\Omega_b$ . For example beginning with  $V_{\text{max}} = E_b$ , Eq. (17) is processed to get a value of L. That value of L is used in Eq. (5) to get a corresponding value of  $V_{\text{max}}$ , and the process is then repeated. Typically, the value of L converges within a few iterations.

Note that Eq. (17) implies that an infinite CPSR can be achieved provided the motor inductance is greater than

$$L_{\infty} = \frac{E_b}{\Omega_b I_r} \quad . \tag{18}$$

While Eqs. (17) and (18) place lower bounds on the motor inductance to achieve either a finite or an infinite CPSR, there is also an upper bound that can be found by recognizing in Eq. (14) that the lead angle cannot exceed 90°. This results in a maximum inductance

$$L_{\max} = \frac{3V_{\max}E_b}{P_r\Omega_b} = \frac{V_{\max}}{\Omega_b I_r} \quad . \tag{19}$$

As an example of the use of these formulas, consider a PMSM with the following parameters

$$V_{dc} = 190 \text{ V} \Rightarrow V_{max} = 85.53 \text{ V} \text{ (assumes over-modulation)}$$
$$E_{b} = \frac{74.2}{\sqrt{2}} \text{ Vrms, } I_{r} = 203 \text{ Arms}$$
$$\Omega_{b} = 1634 \text{ elec. rad/sec}$$
$$CPSR = 9$$
(20)

For this example, the limiting inductance values are

$$L_{\min} = 142\,\mu H$$

$$L_{\infty} = 158\,\mu H$$

$$L_{\max} = 258\,\mu H$$
(21)

The CPSR performance of a PMSM with a finite CPSR is shown conceptually in Fig. E.3.


Fig. E.3. Constant power performance of the PMSM driven by sinusoidal PWM.

The key parameter in determining the CPSR capability of the sinusoidal back-emf PMSM is the motor inductance. This is also true for the trapezoidal back-emf BDCM.

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