

Compressor is A Sensor: A Universal Refrigerant Charge Fault Detection and Diagnostics Method Based on Pump Down Operation



Zhenning Li
Bo Shen

June 2022



ORNL IS MANAGED BY UT-BATTELLE LLC FOR THE US DEPARTMENT OF ENERGY

DOCUMENT AVAILABILITY

Reports produced after January 1, 1996, are generally available free via OSTI.GOV.

Website www.osti.gov

Reports produced before January 1, 1996, may be purchased by members of the public from the following source:

National Technical Information Service
5285 Port Royal Road
Springfield, VA 22161
Telephone 703-605-6000 (1-800-553-6847)
TDD 703-487-4639
Fax 703-605-6900
E-mail info@ntis.gov
Website <http://classic.ntis.gov/>

Reports are available to US Department of Energy (DOE) employees, DOE contractors, Energy Technology Data Exchange representatives, and International Nuclear Information System representatives from the following source:

Office of Scientific and Technical Information
PO Box 62
Oak Ridge, TN 37831
Telephone 865-576-8401
Fax 865-576-5728
E-mail reports@osti.gov
Website <https://www.osti.gov/>

This report was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

Buildings and Transportation Science Division

**A UNIVERSAL REFRIGERANT CHARGE FAULT DETECTION AND DIAGNOSTICS
METHOD BASED ON PUMP DOWN OPERATION**

Zhenning Li, Bo Shen

June 2022

Prepared by
OAK RIDGE NATIONAL LABORATORY
Oak Ridge, TN 37831
managed by
UT-BATTELLE LLC
for the
US DEPARTMENT OF ENERGY
under contract DE-AC05-00OR22725

CONTENTS

CONTENTS	iii
EXECUTIVE SUMMARY.....	4
1. BACKGROUND	4
2. CHARGE PREDICTION METHODOLOGY	5
3. EXPERIMENT VALIDATION OF NEW CHARGE PREDICTION METHOD.....	9
4. CONCLUSION.....	12
5. REFERENCE.....	12

EXECUTIVE SUMMARY

The primary goal of this report is to develop a universal charge fault detection method that requires only a few experimental data with high prediction accuracy. Currently, pump-down operations is typical practices by HVAC technicians when they need to open the refrigerant circuit to make a repair. In addition, compressors have a built-in low-pressure cut-off protection function, and the compressor performance maps are commonly available from manufacturers. The new charge fault detection and diagnostics method innovatively utilizes the typical pump down operation, the compressor's low-pressure cut-off protection, and the compressor performance map. It does not require any geometry information of heat exchangers, refrigerant lines, or charge buffers.

In the report, the novel charge prediction method is formulated via theoretical analysis, then it was verified using experiment tests conducted on a residential system by closing TXV in a reversible heat pump. The experiments were conducted at four different charge levels, i.e., 7 lbm, 8 lbm, 9 lbm, 9.5 lbm. At each charge level, pump-down operations were conducted four times at different ambient conditions under cooling mode operation and another four times at different ambient conditions for heating mode operation. The repeatability of the charge prediction method was validated.

Experiment validations with heat pump refrigerant leakage tests demonstrate that the deviation of the proposed charge prediction method compared with measurement is within 8%. This technology makes refrigerant charge amount available at the technician's fingertips and leads to shorter maintenance time and fewer site visits.

1. BACKGROUND

Operation reliability of the HVAC systems plays an essential role in ensuring energy efficiency and indoor thermal comfort. To operate and maintain heat pump systems efficiently, the energy efficiency should be maximized through optimal control and the reliability should be maintained by continual fault diagnosis technology. For the residential and commercial HVAC systems, faults occur inevitably after long term operation. The occurrence of a fault is usually related to the improper initial installation or the degradation of components during the operation. Faults in heat pump systems can be classified into hard and soft faults. Hard faults lead to system halt and can be easily detected and diagnosed. However, soft faults such as refrigerant leakage are difficult to detect and diagnose before the fault accumulates to severe consequences. According to [1], refrigerant charge fault is the most costly soft fault among all different types of heat pump faults and has become a significant hurdle of heat pump efficiency. [2] showed that refrigerant charge accounts for 63% of tune-up faults of air conditioners. The refrigerant charge fault mainly attributes to refrigerant leakage ([3]). [4] revealed that the cooling capacity of a heat pump with 75% refrigerant charge, i.e., low-charged system, degrades by 20% than the same system with nominal refrigerant charge. And the system with 75% charge yields 16% Seasonal Energy Efficiency Ratio (SEER) degradation than nominal charged system. [5] found a heat pump with 10%-16% over-charge results in up to 30% increase in annual electricity consumption. As a conclusion, low-charge and over-charge systems induce efficiency degradation. To avoid operating heat pumps off-design conditions, the systems should always be charged with the appropriate amount of refrigerant.

The research on developing refrigerant charge fault detection methods have been paid great attention for last few decades. [6] and [7] found the superheat degree at the compressor suction and subcooling degree at the condenser outlet are both affected by the amount of refrigerant charge in the system. Thus, superheat degree and subcooling degree can be good predictors of refrigerant charge. Despite their method shows high reliability, the method requires many experimental data. Considering the operation of heat pump is continuously fluctuating due to the changes of ambient temperature and building load, the extraction of

steady-state operation data requires long data acquisition time. [8] predicted refrigerant leakage in a vapor compression system using Artificial Neural Network (ANN). In addition to a large amount of experimental data required to train their ANN model, their model is only applicable for the specific heat pump system because the trained model is system dependent. [9] developed a mathematical decoupling framework for charge fault detection of vapor compression systems. Their method was effective to detect the refrigerant undercharge and overcharge faults. However, their method cannot quantify the total refrigerant charge amount. That is, if their method detects a charge fault, a technician cannot know how much refrigerant should be charged to or released from the system. Later, [10] presented the virtual refrigerant charge sensor for the vapor compression systems. The subcooling and superheat temperatures were used as the input variables to estimate the refrigerant charge amount. However, this model was only suitable for the heat pumps with the fixed speed compressor. According to [11], the calculation accuracy of their model was not satisfying when applied for the variable speed heat pump systems. After that, [12] improved the model by adding the evaporator inlet quality and the discharge superheat temperature as two additional predictors. However, under the conditions of lower outdoor temperatures or higher fault intensities (such as 70% low-charge or 130% over-charge), the performance of their Fault Detection and Diagnostics (FDD) method has large deviation compared with the actual charge amount.

The objective of this report is to develop a universal charge identification approach. It is an accurate, fast, cost-effective refrigerant charge fault detection method which can be executed automatically during existing vapor compression system commissioning operations. The new charge FDD method will utilize pump-down operations in the field and well-known compressor information (compressor maps) to identify key parameters and characterize a system charge model on the fly. It does not require geometry details of any components such as heat exchanger internal volumes, length of pipelines, and internal volume of accumulator and receiver as the previous charge models need. It is universally applicable to a variety of vapor compression systems, i.e., packaged systems and split systems under various field conditions.

2. CHARGE PREDICTION METHODOLOGY

Currently, HVAC technicians are regularly performing refrigerant pump down operations when they need to open the refrigerant circuit to make a repairment. Figure 1 shows a typical residential heat pump system. There are two cut-off valves, one valve in the suction line and one valve in the liquid line. As the technician closes the liquid line valve and turns the air conditioning on, the compressor pushes all the refrigerant into the high-pressure side of the system. Usually, the compressor has low-pressure protection mechanism, e.g., 30 Psig low pressure limit for a typical R-410A system. When the suction pressure gets to this predetermined lower limit, the compressor will be turned off by the unit control. Most of the vapor compression systems using scroll compressors have been equipped with the low-pressure protection feature. Thus, the termination of the pump down will be executed automatically at a constant low suction pressure without extra cost. At the end of the pump down, the suction pressure is extremely low. And the refrigerant mass flow rate is very small, because the compressor mass flow rate is dictated by the compressor displacement volume and low suction pressure setting (vapor density). At the termination, the vapor compression system reaches near steady-state balance points. Automatic pump down operation can be conducted by systems equipped with one solenoid cut-off valve at the condenser exit. After the pump down operation, the refrigerant can be released back to low-pressure side by opening the valve. The novel charge fault detection method is realized by analyzing the data recorded by a controller which monitors the compressor and the pressures and temperatures at the suction and liquid line during the pump down operation.

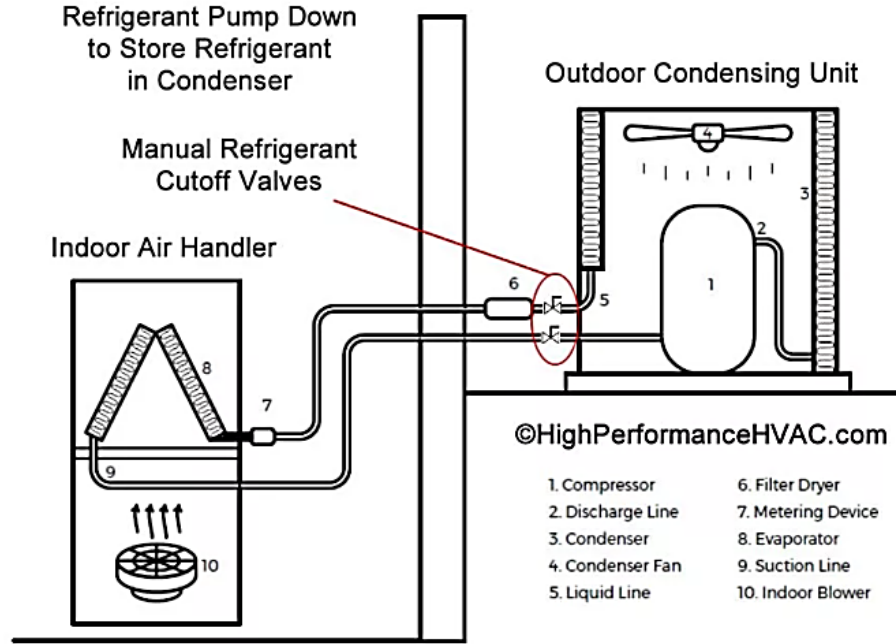


Figure 1: Schematic of Pump Down Operation of Heat Pump

There is an advantage of predicting charging using measured data from pump down operation instead of using data from steady state heat pump regular operation. During steady state operation, the amount of refrigerant in refrigerant buffer, i.e., receiver or accumulator, does not circulate in the system. Therefore, the refrigerant stored in the receiver or accumulator, does not affect the sensor measured information. In other words, the system operation information is identical when the receiver is filled with liquid refrigerant or completely empty, as long as the circulated refrigerant is of the same amount. Considering the pump down operation circulates all refrigerant into high-pressure side including the refrigerant in refrigerant buffer, one highlight of this charge prediction technology is its capability to predict the total refrigerant charge including refrigerant in accumulator and receiver. At the end of a pump down operation, the refrigerant status in the high-pressure side is schematized in Figure 2. The tube represents the total refrigerant flow path in the high-pressure side.

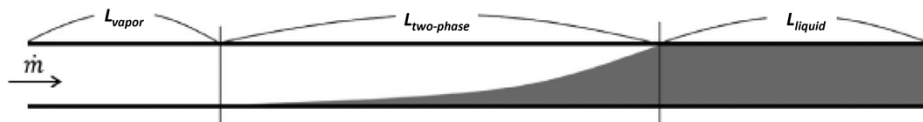


Figure 2: Refrigerant Distribution in High-pressure Side Flow Path

In the refrigerant flow path, the longer a section is occupied by a specific-phase of refrigerant, the greater amount of refrigerant under that phase is stored. The phase-specific refrigerant charge can be calculated as the product of refrigerant average density, the cross sectional area of the path and the length of the path occupied by the specific phase as shown in Equation (1).

$$m_{\text{phaseSpecific}} = (\rho_{\text{phaseSpecific}} A_{\text{crossSection}}) L_{\text{phaseSpecific}} \quad (1)$$

For a vapor compression system, the phase-specific average density and the cross-sectional area can be regarded as constants between multiple pump-down operations. Equation (2) is an abstract form of Equation

(1) and shows the linear relationship between the refrigerant charge and the length of the path occupied by different phases.

$$\begin{aligned} m_{twoPhase} &= k_1 L_{twoPhase} \\ m_{liquid} &= k_2 L_{liquid} \\ m_{vapor} &= k_3 L_{vapor} \end{aligned} \quad (2)$$

The summation of Equation (2) is the total refrigerant charge as shown in Equation (3).

$$m_{totalCharge} = m_{twoPhase} + m_{liquid} + m_{vapor} \quad (3)$$

Despite the pump down process is a dynamic process, at the end of the operation, the mass flow rate in the compressor changes very slowly and the system can be regarded to reach quasi steady state. And there is very small amount of refrigerant left in the low-pressure side after evacuating the refrigerant. Figure 3 shows the P-h diagram of the quasi-steady state at the last moment of pump down operation.

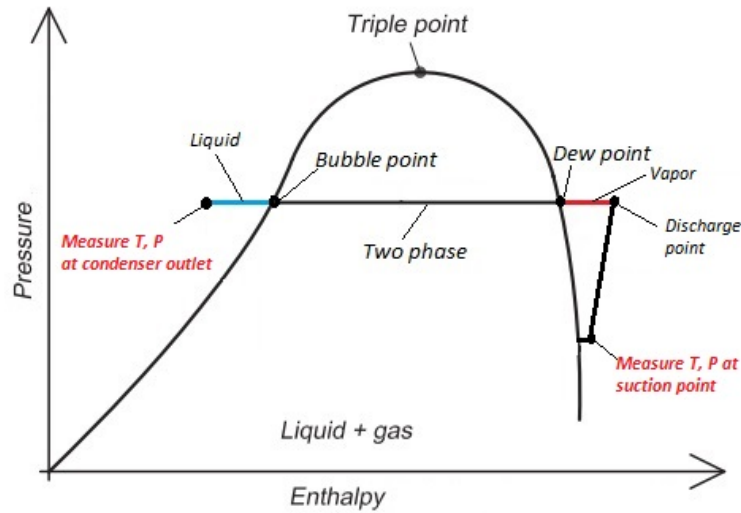


Figure 3: P-h diagram for the Quasi Steady State at the End of Pump-down

Based on the energy conservation, the capacity of each phase can be calculated by the enthalpy difference between the phase transition points, governed by the measured condensing pressure at the condenser exit. Equation (4) shows how to calculate the heat transfer rate. h_{fg} is the latent heat of refrigerant at the condensation pressure, i.e., discharge pressure. $h_{bubblepoint}$, $h_{dewpoint}$, $h_{dischargePoint}$ and $h_{condenserOutlet}$ are the enthalpy at bubble point, dew point, discharge point and condenser outlet, respectively.

$$\begin{aligned} \dot{Q}_{twoPhase} &= \dot{m} \times h_{fg} \\ \dot{Q}_{liquid} &= \dot{m} \times (h_{bubblePoint} - h_{condenserOutlet}) \\ \dot{Q}_{vapor} &= \dot{m} \times (h_{dischargePoint} - h_{dewPoint}) \end{aligned} \quad (4)$$

From the heat transfer point of view, the heat transfer rate between air and refrigerant can be expressed as Equation (5), where $U_{twoPhase}$, U_{liquid} , U_{vapor} are the total heat transfer coefficient per unit tube length for different phase sections, $LMTD_{twoPhase}$, $LMTD_{liquid}$, $LMTD_{vapor}$ are the logarithmic mean temperature difference between the outdoor air and refrigerant of different phase.

$$\begin{aligned}
Q_{twoPhase} &= U_{twoPhase} L_{twoPhase} LMTD_{twoPhase} \\
Q_{liquid} &= U_{liquid} L_{liquid} LMTD_{liquid} \\
Q_{vapor} &= U_{vapor} L_{vapor} LMTD_{vapor}
\end{aligned} \tag{5}$$

Since the heat transfer coefficient of the refrigerant is much larger than the heat transfer coefficient of air, the air heat transfer coefficient dominates $U_{twoPhase}$, U_{liquid} , U_{vapor} . The dominance of airside thermal resistance is true for forced convection when the fans are on. If the fans are closed during the pump down operation, the airside heat transfer coefficient for natural convection is even smaller than forced convection, and the airside thermal resistance is even more dominant. It is worthwhile to mention that, the variation of heat transfer coefficient of air is very small under different ambient temperature for forced convection [13] as well as for natural convection [14] in the typical application temperature range of the heat pump systems. Therefore, $U_{twoPhase}$, U_{liquid} , U_{vapor} can be regarded as constants which are not sensitive to the variation of ambient temperature. By equalizing Equation (4) and Equation (5) and rearrange the equations, the phase specific path length can be expressed in Equation (6).

$$\begin{aligned}
L_{twoPhase} &= \frac{\dot{m} \times h_{fg}}{U_{twoPhase} LMTD_{twoPhase}} \\
L_{liquid} &= \frac{\dot{m} \times (h_{bubblePoint} - h_{condenserOutlet})}{U_{liquid} LMTD_{liquid}} \\
L_{vapor} &= \frac{\dot{m} \times (h_{dischargePoint} - h_{dewPoint})}{U_{vapor} LMTD_{vapor}}
\end{aligned} \tag{6}$$

Plug Equation (6) into Equation (2), then sum up refrigerant charge in different phases as Equation (3), the total refrigerant charge is shown in Equation (7).

$$m_{totalCharge} = k_1 \times \frac{\dot{m} \times h_{fg}}{U_{twoPhase} LMTD_{twoPhase}} + k_2 \times \frac{\dot{m} \times (h_{bubblePoint} - h_{condenserOutlet})}{U_{liquid} LMTD_{liquid}} + k_3 \times \frac{\dot{m} \times (h_{dischargePoint} - h_{dewPoint})}{U_{vapor} LMTD_{vapor}} \tag{7}$$

The constants k_1 , k_2 , k_3 and constants $U_{twoPhase}$, U_{liquid} , U_{vapor} can be grouped as shown in Equation (8).

$$m_{totalCharge} = \left(\frac{k_1}{U_{twoPhase}}\right) \times \frac{\dot{m} \times h_{fg}}{LMTD_{twoPhase}} + \left(\frac{k_2}{U_{liquid}}\right) \times \frac{\dot{m} \times (h_{bubblePoint} - h_{condenserOutlet})}{LMTD_{liquid}} + \left(\frac{k_3}{U_{vapor}}\right) \times \frac{\dot{m} \times (h_{dischargePoint} - h_{dewPoint})}{LMTD_{vapor}} \tag{8}$$

By lumping the constants in Equation (8), Equation (9) shows the refrigerant charge calculation.

$$m_{totalCharge} = C_1 \times \frac{\dot{m} \times h_{fg}}{LMTD_{twoPhase}} + C_2 \times \frac{\dot{m} \times (h_{bubblePoint} - h_{condenserOutlet})}{LMTD_{liquid}} + C_3 \times \frac{\dot{m} \times (h_{dischargePoint} - h_{dewPoint})}{LMTD_{vapor}} \tag{9}$$

In Equation (9), for a specific heat pump system there are four constants C_1 , C_2 , C_3 and $m_{totalCharge}$. These four constants are not sensitive to the variation of the ambient condition. They are specific values for that vapor compression system. Therefore, the four constants can be obtained through a few pump-down operations at different ambient conditions. To be specific, since there are four unknowns, four equations are needed. That is, minimum four pump-down operations under different ambient temperature will be conducted to form four equations. After the four pump-down runs, the total refrigerant charge can be solved. The experiment information required to assign into Equation (9) is obtained by system controller at

the end of pump down operation when the system reaches quasi steady state. The constants of C_1 , C_2 , C_3 can be obtained on the day of the unit installation. Since they are not sensitive to the charge variation, they can be assumed being constants and treated as inputs to a controller of this specific heat pump unit. Later for continuous monitoring, the unit will only need to go through one pump down operation to calculate $m_{totalCharge}$ in Equation (9).

To obtain the average temperature of different phases and the refrigerant enthalpy values required in Equation (9), only the suction state point and the condenser outlet state point are necessary, because the pressure drop inside condenser and pipes are negligible due to very small refrigerant mass flow rate. For the compression process, the refrigerant mass flow rate and compressor power can be obtained using the compressor map from the manufacturer. The compressor discharge temperature can be decided by the energy balance. As a result, all state points in Figure 3 are available.

As stated in previous section, the novel charge FDD method can take advantage of the ‘low-pressure protection’ capability of the compressor to furtherly ease the data acquisition process. Low-pressure protection indicates that the controller will shut down the compressor at a predetermined low suction pressure limit. This can further ease the experiments by only measuring three variables, i.e., the suction temperature and condenser outlet temperature and pressure. And the pump down operation can be scheduled by the controller to automatically perform at different ambient conditions. Once the charge amount is predicted, the refrigerant charge fault can be diagnosed by comparing the name-plate charge amount suggested by the manufacturer with the measured charge amount.

3. EXPERIMENT VALIDATION OF NEW CHARGE PREDICTION METHOD

The charge prediction method was validated using experiment data obtained from laboratory refrigerant leakage test from two residential heat pump systems ([15]). The measured charge level in the leakage test is shown in Figure 4. Three points highlighted in red circles are sampled from the experiment data to solve the constants C_1 , C_2 , C_3 in Equation (9) for each of the test heat pump system. The goal is to test whether the fitted Equation (9) can predict other points in leakage tests.

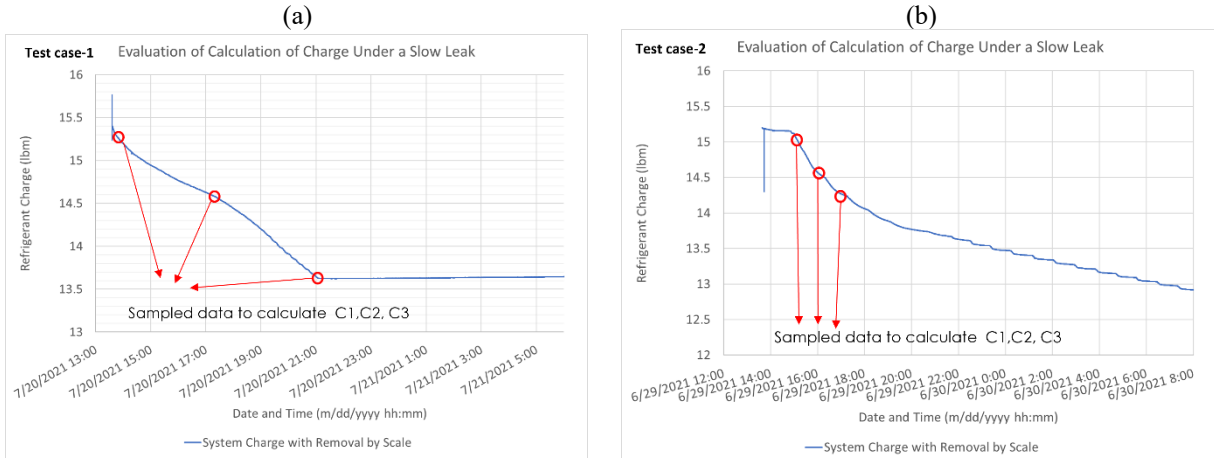


Figure 4: Sampling data to solve the constants for theoretical charge prediction equation (a) Test case-1; (b) Test case-2.

Table 1 shows the solved constants in Equation (9) using the sampled data from Figure 4.

Table 1: Solved constants in charge prediction equation using experiment data

Test Number	C_1	C_2	C_3
Test case-1	3.84	10.37	28.89
Test case-2	6.19	1.68	12.50

Figure 5 shows the prediction of other charge levels using the established charge prediction equation for different test cases. The discrepancy between measured charge and predicted charge is within 8% and 5%, respectively with two different test cases.

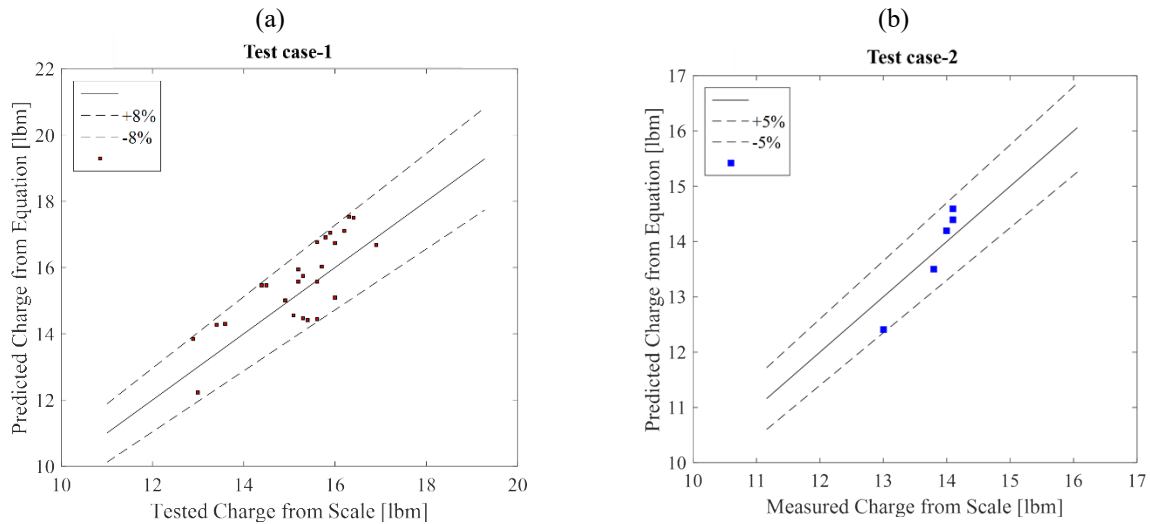


Figure 5: Preliminary Validation of Charge Prediction Method (a) Test case-1; (b) Test case-2.

We conducted experiments for four different charge levels, two different operation modes of heat pump, and eight different outdoor temperatures. Table 2 shows the test matrix.

Table 2: Experiment Test Matrix to Validate the Reproducibility of the Charge Migration Prediction

Reproducibility Test Matrix				
Charge Level [lb]	7 lb	8 lb	9 lb	9.5 lb
Outdoor T [F]	71 (Cooling)	71 (Cooling)	71 (Cooling)	71 (Cooling)
	75 (Cooling)	75 (Cooling)	75 (Cooling)	75 (Cooling)
	82 (Cooling)	82 (Cooling)	82 (Cooling)	82 (Cooling)
	95 (Cooling)	95 (Cooling)	95 (Cooling)	95 (Cooling)
	71 (Heating)	71 (Heating)	71 (Heating)	71 (Heating)
	67 (Heating)	67 (Heating)	67 (Heating)	67 (Heating)
	55 (Heating)	55 (Heating)	55 (Heating)	55 (Heating)
	45 (Heating)	45 (Heating)	45 (Heating)	45 (Heating)

Figure 6 shows the refrigerant mass flow rate measurement. Two data reduction method was used. One uses the compressor map to predict refrigerant mass flow rate during pump-down. The other uses the suction density and displacement volume. The refrigerant mass flow rate using the above two data reduction methods is very close.

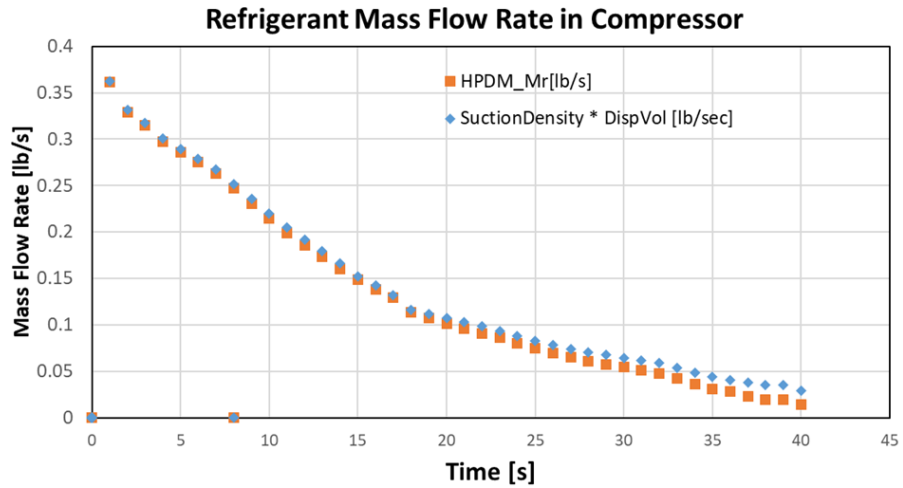


Figure 6: Refrigerant mass flow rate through the compressor for pump down under cooling mode, Toutdoor=71F, 7 lb system charge

Table 3 shows the charge migrated from the low-pressure side to the high-pressure side during pump-down using different data reduction methods.

Table 3: Low-side charge calculation using different data reduction methods

Output	
Pumpdown Duration [s]	40
Displacement Vol [ft^3/sec]	0.100613
Toutdoor [F]	
TC_AirRETURN_AVG	73.6618537
TC_AirSupply_MHX_Avg	70.551
T_OD_Fan_MHX_Avg	74.7730488
LowSide_Charge_CompressorMap [lb]	5.29
LowSide_Charge_DisVolDensity [lb]	5.62

The repeatability of the pump-down charge migration is important. Figure 7 shows the low-pressure side charge migration obtained from pump-down at different outdoor temperatures.

Charge migration through compressor [s]

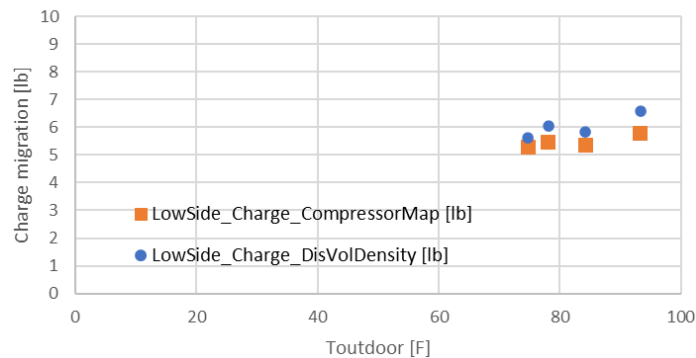


Figure 7: Repeatability test of low side charge migration at different outdoor temperatures.

4. CONCLUSION

The performance of the heat pump system varies greatly depending on the refrigerant charge amount. Improving the refrigerant charge fault detection and diagnostics method of vapor compression systems have the potential for increasing energy efficiency and reducing service cost. The primary goal of this report is to develop a universal charge fault detection method which requires only a few experimental data with high prediction accuracy.

The proposed charge prediction method is based on running through refrigerant pumping down cycles. With inputting the compressor model number, the fault diagnosis module knows the exact compressor power and mass flow rate map at measured suction and discharge pressure. When pumping down, a valve at the liquid line would close to stop the refrigerant flow, and the refrigerant is pumped by the compressor from the evaporator side to the condenser side. By monitoring the real time suction/discharge pressures and temperatures, the refrigerant mass at the evaporating and condensing sides can be accurately calculated.

As a result, the system charge has been predicted and compared to the nameplate to indicate a charge fault. Preliminary experiment validation shows the charge prediction accuracy is within 8%. The quasi-steady-state system model to simulate the pumping down process successfully can capture the transients of system during pump-down operation and demonstrates the efficacy of the new charge prediction method.

5. REFERENCE

1. Hong, S.B., J.W. Yoo, and M.S. Kim, *A theoretical refrigerant charge prediction equation for air source heat pump system based on sensor information*. International Journal of Refrigeration, 2019. 104: p. 335-343.
2. Rossi, T.M., *Unitary air conditioner field performance*. Proceedings of International Refrigeration and Air Conditioning Conference 2004. Paper 666.
3. Madani, H. and E. Roccatello, *A comprehensive study on the important faults in heat pump system during the warranty period*. International journal of refrigeration, 2014. 48: p. 19-25.
4. Kim, W. and J.E. Braun, *Evaluation of the impacts of refrigerant charge on air conditioner and heat pump performance*. International journal of refrigeration, 2012. 35(7): p. 1805-1814.
5. Domanski, P.A., H. Henderson, and W.V. Payne, *Effect of heat pump commissioning faults on energy use in a slab-on-grade residential house*. Applied Thermal Engineering, 2015. 90: p. 352-361.
6. Grace, I., D. Datta, and S. Tassou, *Sensitivity of refrigeration system performance to charge levels and parameters for on-line leak detection*. Applied Thermal Engineering, 2005. 25(4): p. 557-566.
7. Kocyigit, N., H. Bulgurcu, and C.-X. Lin, *Fault diagnosis of a vapor compression refrigeration system with hermetic reciprocating compressor based on ph diagram*. International journal of refrigeration, 2014. 45: p. 44-54.
8. Tassou, S. and I. Grace, *Fault diagnosis and refrigerant leak detection in vapour compression refrigeration systems*. International Journal of Refrigeration, 2005. 28(5): p. 680-688.
9. Li, H. and J.E. Braun, *A methodology for diagnosing multiple simultaneous faults in vapor-compression air conditioners*. HVAC&R Research, 2007. 13(2): p. 369-395.
10. Li, H. and J.E. Braun, *Development, evaluation, and demonstration of a virtual refrigerant charge sensor*. HVAC&R Research, 2009. 15(1): p. 117-136.
11. Kim, W. and J.E. Braun, *Performance evaluation of a virtual refrigerant charge sensor*. International journal of refrigeration, 2013. 36(3): p. 1130-1141.
12. Kim, W. and J.E. Braun, *Extension of a virtual refrigerant charge sensor*. International Journal of Refrigeration, 2015. 55: p. 224-235.
13. Wang, C.-C., et al., *Heat transfer and friction correlation for compact louvered fin-and-tube heat exchangers*. International journal of heat and mass transfer, 1999. 42(11): p. 1945-1956.
14. Churchill, S.W. and H.H. Chu, *Correlating equations for laminar and turbulent free convection from a vertical plate*. International journal of heat and mass transfer, 1975. 18(11): p. 1323-1329.
15. Butler, B., et al., *Refrigeration leak detection*, US Patent number: 11131471. 2021, Emerson Climate Technologies, Inc.