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W. H. Roach and D. R. Smith

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# ESTIMATES OF MAXIMUM SUBCRITICAL DIMENSIONS OF SINGLE FISSILE METAL UNITS

W. H. Roach and D. R. Smith Los Alamos Scientific Laboratory Los Alamos, New Mexico 87544

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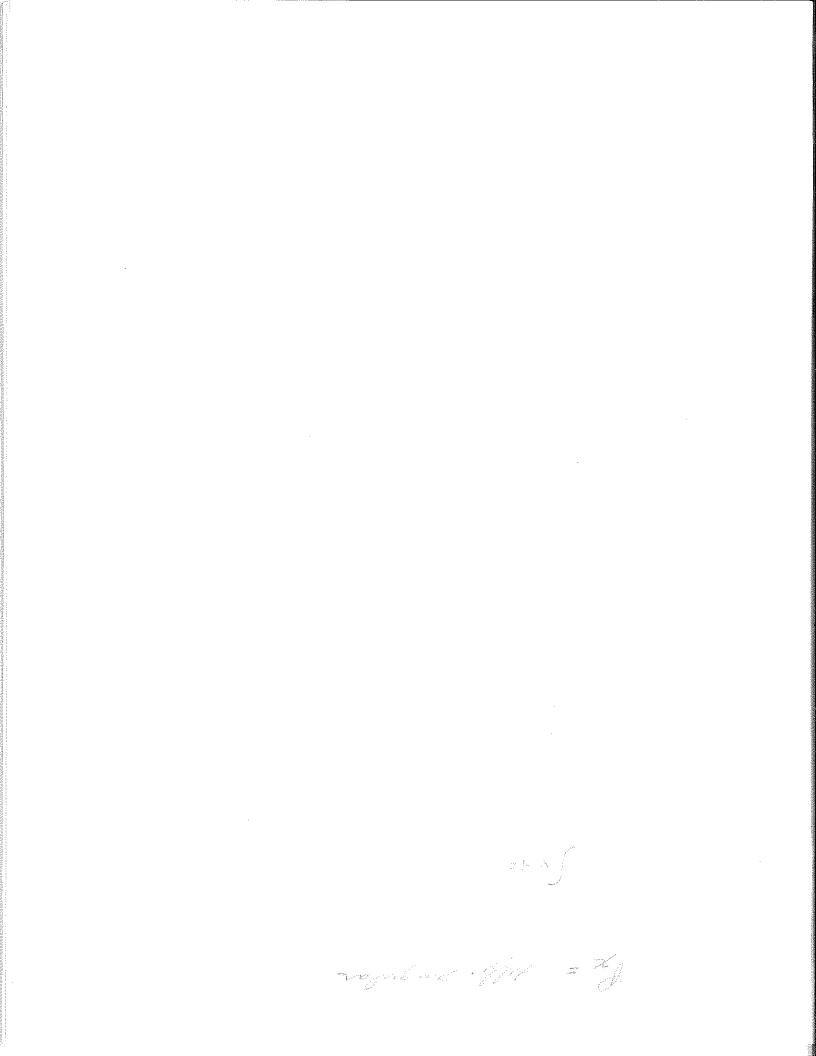
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## ESTIMATES OF MAXIMUM SUBCRITICAL DIMENSIONS OF SINGLE FISSILE METAL UNITS

W. H. Roach and D. R. Smith

### ABSTRACT

The maximum subcritical dimensions of water-reflected metal spheres, cylinders, and slabs of <sup>235</sup>U, <sup>233</sup>U, and <sup>239</sup>Pu, which will be of value in the specification of process, storage, and transport conditions for fissile materials, were determined using the DTF transport code with the Hansen-Roach 16-group cross sections. The effective neutron multiplication factor of single units which had been shown experimentally to be critical was first computed to evaluate the bias inherent in the calculations. These dimensions, which contain no safety factors other than those demanded by the uncertainty in the calculations, are internally consistent and derive from a common method of calculation and input data. Some individual values may be relaxed when based on well established experimental results.



Tabulations of criticality parameters which have been published (see, for example, Ref. 1) provide only a critical value for a particular parameter of interest. The Nuclear Safety Guide<sup>2</sup> contains a large number of useful safe parameters for a variety of plant processes and equipment, but, for some applications, is overly restrictive in recommended safety factors.

It is the purpose of the present note to attempt to establish subcritical bounds for several of the commonly utilized parameters. This information will be of particular value to those engaged in material processing when used in conjunction with realistic safety factors. Isotopically pure, unmoderated, water-reflected single units of <sup>233</sup>U, <sup>235</sup>U, and <sup>239</sup>Pu metal in simple geometry are considered primarily because the existing experimental data for such simple assemblies provide a base from which calculational extrapolations can be made.

The maximum subcritical dimensions of water-reflected metal spheres, cylinders, and slabs were determined after first calculating the critical values for these systems. All calculations utilized the Los Alamos DTF code, which is an application of the Carlson  $S_n$  method with the transport approximation. Both  $S_8$  and  $S_{16}$  angular approximations were used, and results were extrapolated to  $S_\infty$  to minimize geometrically dependent calculational errors. The variation of the effective neutron multiplication factor  $(k_{eff})$  with metal radius was also obtained. All assemblies were calculated using Hansen-Roach 16-group cross sections and a 20-cm-thick water reflector. Radii of spheres and of cylinders of infinite length and the thickness of slabs infinite in two dimensions were determined for  $^{233}$ U,  $^{235}$ U, and  $^{239}$ Pu based on densities of 18.66 g/cm³, 18.82 g/cm³, and 19.70 g/cm³, respectively. Results are presented in Table 1.

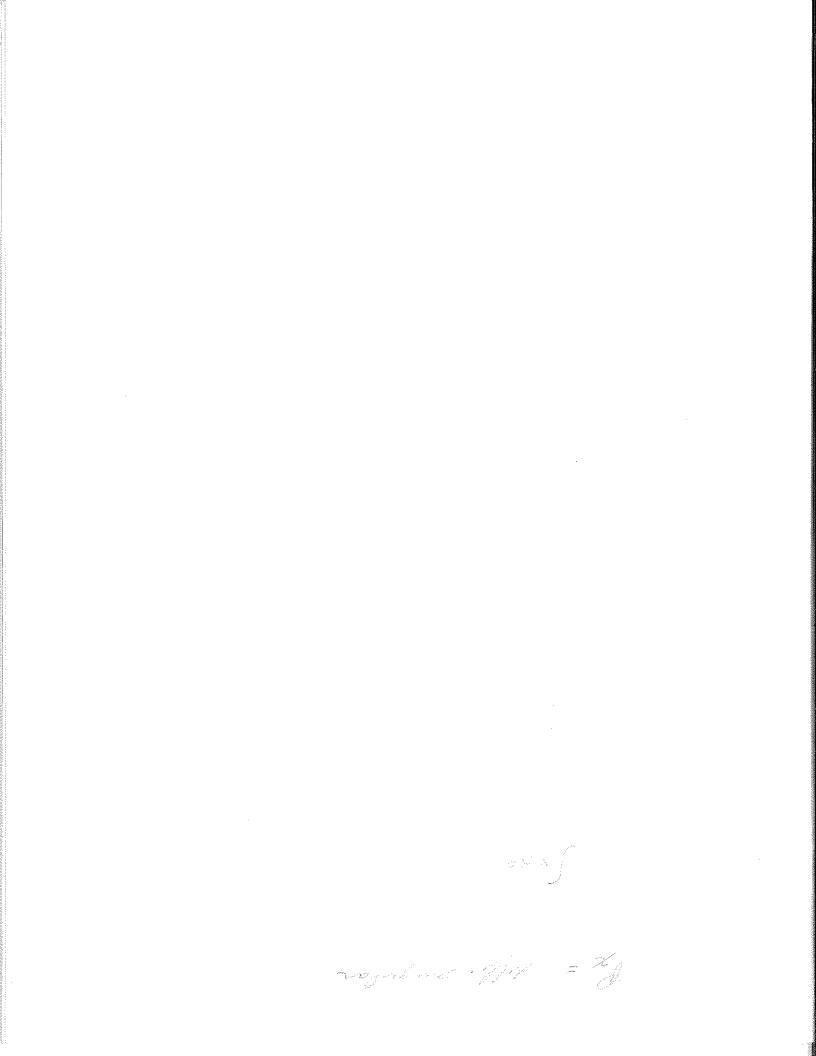
<sup>1.</sup> H. C. Paxton, J. T. Thomas, D. Callihan, and E. B. Johnson, "Critical Dimensions of Systems Containing U<sup>235</sup>, Pu<sup>239</sup>, and U<sup>233</sup>," USAEC Report TID-7028 (1964).

<sup>2.</sup> Subcommittee 8 of the American Standards Association Sectional Committee N6 and Project 8 of the American Nuclear Society Standards Committee, Nuclear Safety Guide, USAEC Report TID-7016, Rev. 1 (1961).

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3. B. G. Carlson et al., "DTF Users Manual," UNC Phys/Math-3321, Vol. I (1963), Vol. II (1964).

<sup>4.</sup> G. E. Hansen and W. H. Roach, "Six and Sixteen Group Cross Sections for Fast and Intermediate Critical Assemblies," LAMS-2543, Los Alamos Scientific Laboratory (1961).



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Table	1.	Calculated	Critical	Dimensions
(	of Wa	ater-Reflect	ted Metal	Units

Critical Parameter (cm)	s <sub>8</sub>	s <sub>16</sub>	Estimated S <sub>∞</sub>	<u>∆k/∆r</u> r
233 U sphere radius	4.552	4.576	4.60	0.75
283 U cylinder radius	2.524	2.538	2.55	0.59
233 U slab thickness	0.6296	0.6288	0.628	0.21
<sup>235</sup> U sphere radius	6.464	6.496	6.52	0.71
<sup>235</sup> U cylinder radius	3.777	3.79 <sup>4</sup>	3.81	0.56
<sup>235</sup> U slab thickness <sup>239</sup> Pu sphere radius	1.494 4.024	1.494 4.047	1.49 4.06	0.22 0.77
239 Pu cylinder radius	2.265	2.280	2.29	0.67
<sup>239</sup> Pu slab thickness	0.723	0.724	0.725	0.29

The bias inherent in the calculations was evaluated by computing the values of  $k_{\mbox{\scriptsize eff}}$  of spheres shown experimentally to be critical. This bias is reflected in the degree of subcriticality of the values of the parameters listed in Table 2 in the following manner.

Table 2. Subcritical Parameters for Single Units of Water-Reflected Metal

Parameters	SSS	\$35 U	239 Pu
k <sub>eff</sub> (S <sub>w</sub> )	0.97	0.98	0.97
Mass (kg)	6.75	20.1	4.9
Sphere radius (cm)	4.4	6.3	3.9
Cylinder radius (cm)	2.3	3.7	2.2
Slab thickness (cm)	0.54	1.35	0.65

The water-reflected spherical critical mass of uranium enriched to 93.5% in  $^{235}\text{U}$  at a uranium density of  $18.8~\text{g/cm}^3$  has been reported as 22.8 kg of  $^{235}\text{U}$ . The value of  $k_{\text{eff}}$  from an  $S_8$  calculation of this unit

G. A. Graves and H. C. Paxton, "Critical Masses of Oralloy Assemblies," <u>Nucleonics</u> 15, No. 6, 90 (June 1957).

was 1.006. The  $^{235}$ U sphere radius from  $S_8$  calculations, in Table 1, is therefore low by a factor of 1.008, which is essentially the margin between  $S_8$  and  $S_\infty$ . There is, therefore, no significant bias in the  $S_\infty$  value of the sphere radius, and the  $S_\infty$  values for cylinders and slabs were assumed valid. The subcritical values quoted in Table 2 for  $^{235}$ U correspond to  $k_{eff}$  equal to 0.98 from  $S_\infty$  calculations and represent a margin below criticality of about 2% in  $k_{eff}$ .

There are no data available describing critical water-reflected metal spheres of plutonium or of <sup>233</sup>U. There are, however, measurements of critical dimensions of unreflected metal spheres and of unreflected solution spheres, so that one may evaluate the applicability of the <sup>233</sup>U and <sup>239</sup>Pu cross sections for both fast and moderated assemblies.

The reported<sup>6</sup> critical radius of an unreflected metal sphere, composed of 98.14%  $^{233}$ U, 1.24%  $^{234}$ U, 0.02%  $^{235}$ U, and 0.60%  $^{238}$ U at a density of 18.44 g/cm³, was 5.965 cm. The calculated value of  $k_{\rm eff}$  of this sphere, using the  $S_8$  approximation, was 1.006. A 16.0 cm radius unreflected sphere of  $^{233}$ UO $_2$ F $_2$  solution was critical at a concentration of 67.1 g of  $^{233}$ U per liter. The corresponding calculated  $k_{\rm eff}$  was 0.995. The value of  $k_{\rm eff}$  from an  $S_8$  calculation of a critical water-reflected metal sphere would be expected to lie between these two values, so any calculated value less than 0.995 is indicative of a subcritical unit. The 1.04% difference in critical radius calculated by  $S_8$  and by  $S_\infty$  corresponds to a difference in  $k_{\rm eff}$  of 0.75 x 1.04 = 0.78%, hence an  $S_\infty$  value of  $k_{\rm eff}$  below 0.987 would indicate subcriticality. A margin of 1.7% in  $k_{\rm eff}$  is considered adequate to provide confidence in the subcriticality of these units and therefore values quoted in Table 2 for  $^{233}$ U correspond to a calculated  $k_{\rm eff}$  ( $S_\infty$ ) of 0.97.

7. J. K. Fox, L. W. Gilley, and E. R. Rohrer, "Critical Mass Studies, Part VIII, Aqueous Solutions of U<sup>233</sup>," ORNL-2143, Oak Ridge National Laboratory (1959).

<sup>6.</sup> G. E. Hansen, "Status of Computational and Experimental Correlations for Los Alamos Fast Neutron Critical Assemblies," <a href="Proceedings of the International Atomic Energy Conference on Physics of Fast and Intermediate Reactors, Vienna, August 3-11, 1961">1961</a>, Vol. I, 445, International Atomic Energy Agency, Vienna (1962).

The critical unreflected plutonium sphere was reported to have a mass of 16.28 kg of  $^{239}\mathrm{Pu}$  at a density of 15.44 g/cm³; the calculated  $k_{eff}$  (S<sub>8</sub>) was 0.999. The calculated value of  $k_{eff}$  (S<sub>8</sub>) of an unreflected spherical critical plutonium solution was 1.015, so the critical water-reflected plutonium sphere should have  $k_{eff}$  greater than 0.999 in S<sub>8</sub>, or greater than 0.992 in S<sub>∞</sub>. The values quoted in Table 2 correspond to  $k_{eff}$  (S<sub>∞</sub>) equal to 0.97 and provide a margin of at least 2.2% in  $k_{eff}$ .

The authors wish to acknowledge the helpful comments and criticism of Dr. Gordon E. Hansen and the invaluable computational assistance of Mrs. Laura Stone of the Los Alamos Theoretical Division.

<sup>8.</sup> G. A. Jarvis, G. A. Linenberger, J. D. Orndoff, and H. C. Paxton, Nucl. Sci. Eng. 8, 525 (1960).

<sup>9.</sup> F. E. Kruesi, J. O. Erkman, and D. D. Lanning, "Critical Mass Studies of Plutonium Solutions," HW-24514 (Del.), Hanford Atomic Products Operation (1962).

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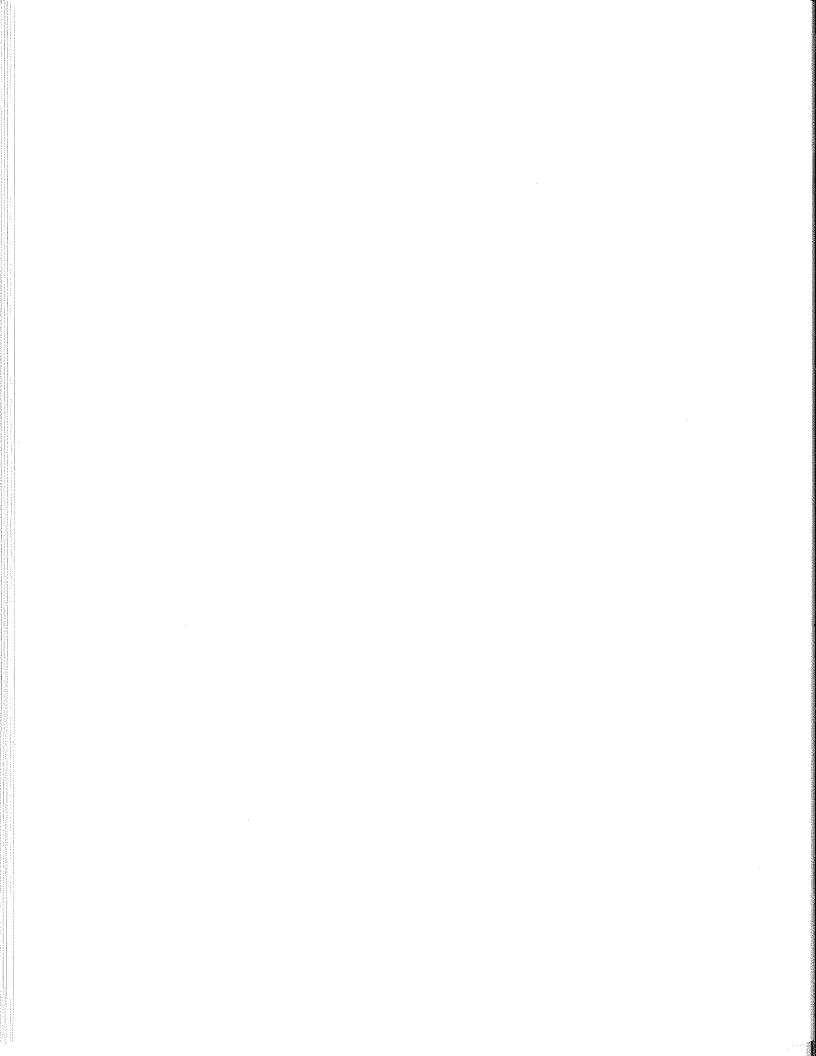
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