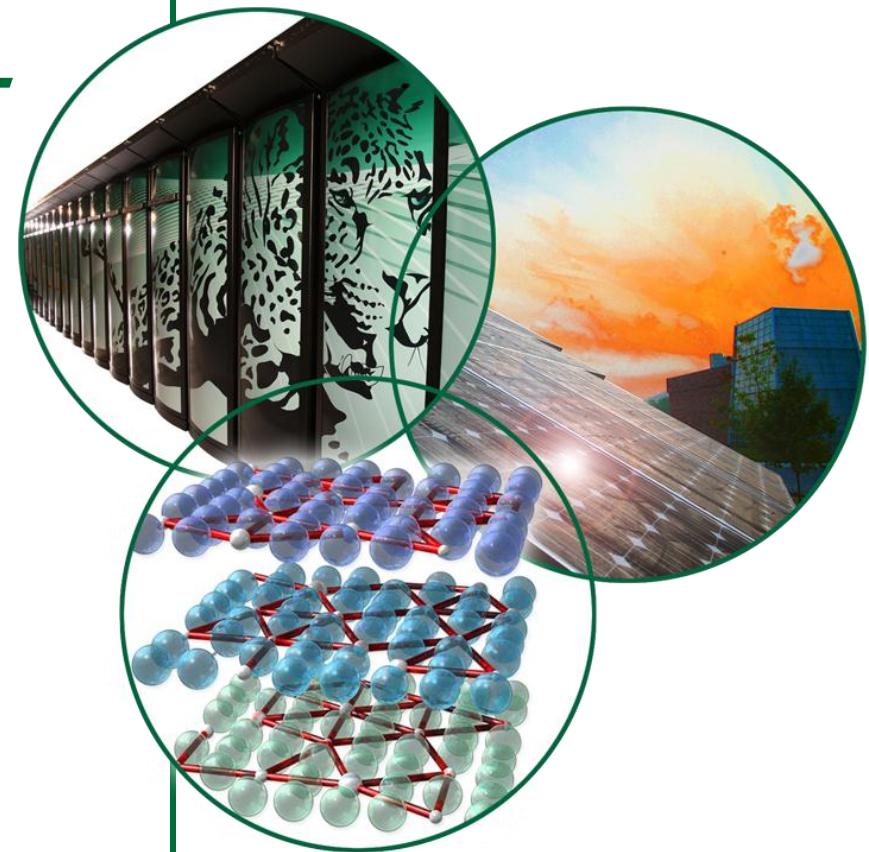


# **REVIEW OF RESULTS FOR THE OECD/NEA PHASE VII BENCHMARK: *STUDY OF SPENT FUEL COMPOSITIONS FOR LONG- TERM DISPOSAL***

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***International High-Level Radioactive Waste  
Management Conference***

**April 10 – 14, 2011, Albuquerque, NM**



# Outline

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- Overview of the benchmark specifications
- Participating organizations, computer codes, and nuclear data
- Results
  - Decay calculations for selected isotopes relevant to burnup-credit criticality safety analyses and for radiological dose assessments
  - Criticality calculations for actinide-only compositions and for actinide and fission product (FP) nuclide compositions
- Conclusions

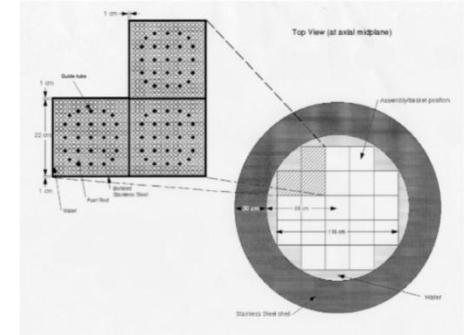
# Overview of the Benchmark Specifications (1/3)

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- Purpose
  - *Study the ability of relevant computer codes and associated nuclear data to predict spent fuel isotopic compositions and corresponding effective neutron multiplication factor ( $k_{\text{eff}}$ ) values in a cask configuration over the time duration relevant to spent nuclear fuel (SNF) long-term storage and disposal*
- Objective
  - *Improve understanding and confidence in our ability to predict  $k_{\text{eff}}$  and source terms for timeframes relevant to extended long-term storage and disposal of SNF*

# Overview of the Benchmark Specifications (2/3)

- Specification (issued Nov 2008)
  - <http://www.oecd-nea.org/science/wpnscs/buc/specifications/>
  - PWR  $\text{UO}_2$  discharged fuel compositions for decay calculations
    - 4.5-wt%  $^{235}\text{U}$  initial enrichment and 50 GWd/MTU burnup
    - Nuclides relevant to burnup credit and radiological dose as well as their precursors (113 total nuclides)
  - Representative cask model for  $k_{\text{eff}}$  calculations
    - Borrowed from previous benchmark specifications
- Requested results
  - Predicted isotopic concentrations for 30 time steps (0 –  $1 \times 10^6$  years)
  - Predicted  $k_{\text{eff}}$  values for each time step
    - Actinide-only (11 total isotopes) fuel compositions
    - Actinide and fission product (30 total isotopes) fuel compositions



# Overview of the Benchmark Specifications (3/3)

Nuclides selected for benchmark calculations based on relevance to radiological dose and burnup-credit criticality safety analyses

## Nuclides relevant to radiological dose assessments (44 total)

$^{14}\text{C}$ ,  $^{36}\text{Cl}$ ,  $^{41}\text{Ca}$ ,  $^{59}\text{Ni}$ ,  $^{79}\text{Se}$ ,  $^{93}\text{Zr}$ ,  $^{90}\text{Sr}$ ,  $^{93\text{m}}\text{Nb}$ ,  $^{94}\text{Nb}$ ,  $^{93}\text{Mo}$ ,  $^{99}\text{Tc}$ ,  $^{107}\text{Pd}$ ,  $^{126}\text{Sn}$ ,  $^{126}\text{Sb}$ ,  $^{126\text{m}}\text{Sb}$ ,  $^{129}\text{I}$ ,  $^{135}\text{Cs}$ ,  $^{137}\text{Cs}$ ,  $^{151}\text{Sm}$ ,  $^{210}\text{Pb}$ ,  $^{226}\text{Ra}$ ,  $^{228}\text{Ra}$ ,  $^{227}\text{Ac}$ ,  $^{229}\text{Th}$ ,  $^{230}\text{Th}$ ,  $^{232}\text{Th}$ ,  $^{231}\text{Pa}$ ,  $^{232}\text{U}$ ,  $^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{235}\text{U}$ ,  $^{236}\text{U}$ ,  $^{238}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{238}\text{Pu}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{241}\text{Pu}$ ,  $^{242}\text{Pu}$ ,  $^{241}\text{Am}$ ,  $^{242\text{m}}\text{Am}$ ,  $^{243}\text{Am}$ ,  $^{245}\text{Cm}$ ,  $^{246}\text{Cm}$

## Nuclides relevant to actinide-only burnup-credit criticality safety analyses (11 total)

$^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{235}\text{U}$ ,  $^{236}\text{U}$ ,  $^{238}\text{U}$ ,  $^{238}\text{Pu}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{241}\text{Pu}$ ,  $^{242}\text{Pu}$ ,  $^{241}\text{Am}$

## Nuclides relevant to actinide and fission product burnup-credit criticality safety analyses (30 total)

$^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{235}\text{U}$ ,  $^{236}\text{U}$ ,  $^{238}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{238}\text{Pu}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{241}\text{Pu}$ ,  $^{242}\text{Pu}$ ,  $^{241}\text{Am}$ ,  $^{242\text{m}}\text{Am}$ ,  $^{243}\text{Am}$ ,  $^{95}\text{Mo}$ ,  $^{99}\text{Tc}$ ,  $^{101}\text{Ru}$ ,  $^{103}\text{Rh}$ ,  $^{109}\text{Ag}$ ,  $^{133}\text{Cs}$ ,  $^{143}\text{Nd}$ ,  $^{145}\text{Nd}$ ,  $^{147}\text{Sm}$ ,  $^{149}\text{Sm}$ ,  $^{150}\text{Sm}$ ,  $^{151}\text{Sm}$ ,  $^{152}\text{Sm}$ ,  $^{151}\text{Eu}$ ,  $^{153}\text{Eu}$ ,  $^{155}\text{Gd}$

Note: 16 nuclides are relevant to both burnup credit criticality and radiological dose analyses.

# Participating Organizations and Computer Codes/Data [1/2]

Country	Organization	Decay Code	Decay Data Library	Criticality Code	Cross-Section Data Library
Slovakia	Nuclear Power Plant Research Institute Trnava Inc, (VUJE)	SCALE 5.1/ ORIGEN-S	ENDF/B-VI	SCALE 5.1/ KENO VI	ENDF/B-V, 44 EGs
USA	Oak Ridge National Laboratory	SCALE 6.1/ ORIGEN-S (beta)	ENDF/B-VII	SCALE 6.0/ KENO V.a	ENDF/B-VII.0, CE
Japan	Japan Atomic Energy Agency	ORIGEN2.2- UPJ	ORLIBJ33	MCNP-4C2	JENDL3.3, CE
Sweden	E Mennerdahl Systems	SCALE 6.0/ ORIGEN-S	ENDF/B-VI	SCALE 6/ KENO V.a	ENDF/B-VII.0, CE
Spain	DENIM/CSN/ SEA Ingenieria	ACAB-2008	JEFF-3.1	MCNPX-2.5	JEFF-3.1.1, CE
				MCNPX-2.4.0	ENDF/B-VI, CE
France	Institut de Radioprotection et de Sûreté Nucléaire (IRSN)	DARWIN 2.0	JEF-2	MORET 5	JEFF-3.1, CE
		PHOENIX 1.0.0a (beta)	ORG2.2 DECAY.LIB	N/A	N/A

EGs = energy groups

CE = continuous energy

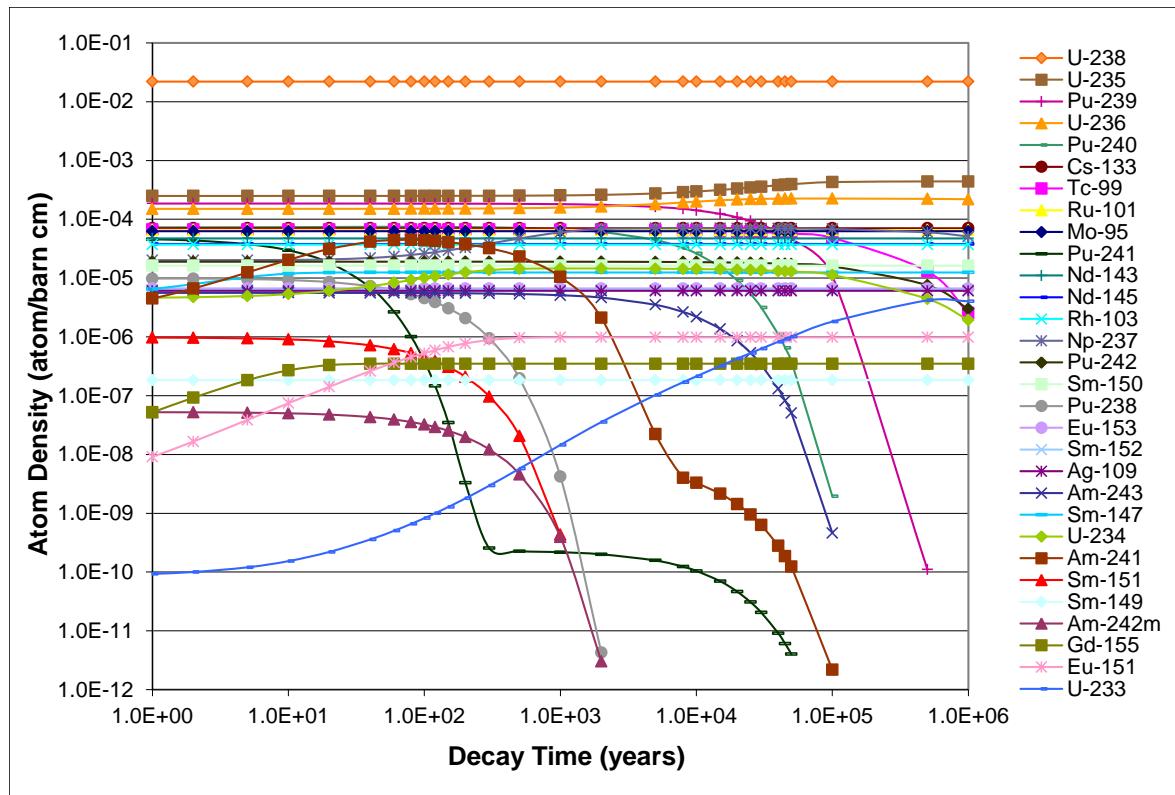
## Participating Organizations and Computer Codes/Data [2/2]

Country	Organization	Decay Code	Decay Data Library	Criticality Code	Cross-section Data Library
France	AREVA-TN	DARWIN 2.1	JEF-2.2	CRISTAL V1.0	JEF-2.2, 172 EGs
Germany	Gesellschaft für Anlagen-und Reaktorsicherheit mbH (GRS)	ORIGEN-X-2008	ENDF/B-VI	SCALE 6/ KENO V.a	ENDF/B-VII.0, 238 EGs
Czech Republic	Nuclear Research Institute at Rez	SCALE 6.0/ ORIGEN-S	ENDF/B-VI	SCALE 6.0/ KENO V.a	ENDF/B-VII.0, 238 EGs
				SCALE 6.0/ KENO V.a	ENDF/B-VII.0, CE
Finland	VTT Technical Research Centre of Finland	SCALE 6.0/ ORIGEN-S	ENDF/B-VI	MCNP5 1.40	ENDF/B-VI, CE
Hungary	KFKI Atomic Energy Research Institute	SCALE 6.0/ ORIGEN-S	ENDF/B-VI	MCNP5	ENDF/B-VI.2 and V, CE
		TIBSO	JEF-2.2	MCNP5	ENDF/B-VI.2 and V, CE
USA	Los Alamos National Laboratory	CINDER 90	ENDF/B-VI	N/A	

# ISOTOPIC RESULTS

# Time-Dependent Nuclide Concentrations [1/2]

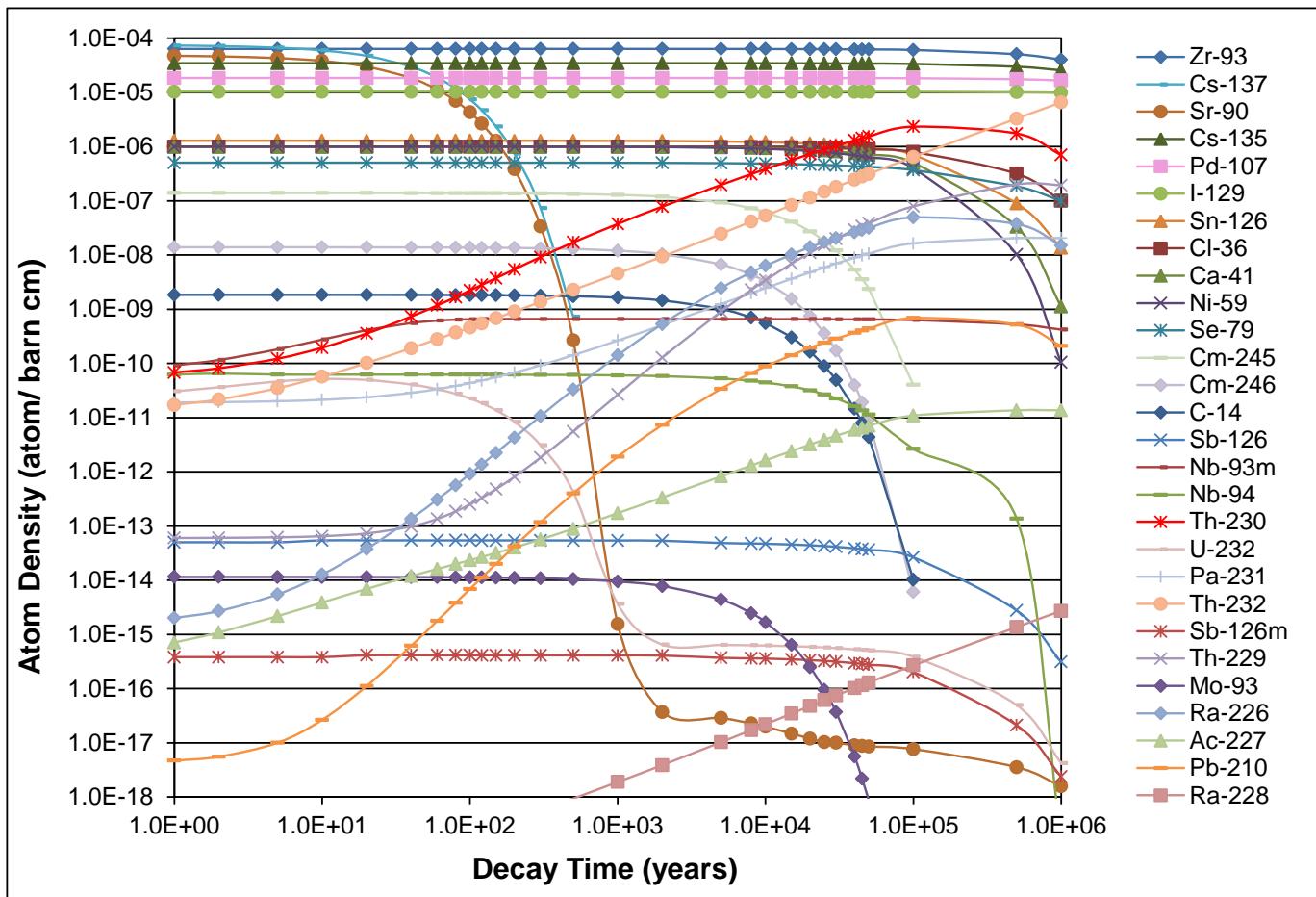
Showing actinides and fission product nuclides relevant to burnup credit



- Note: Nuclides  $^{99}\text{Tc}$ ,  $^{151}\text{Sm}$ ,  $^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{235}\text{U}$ ,  $^{236}\text{U}$ ,  $^{238}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{238}\text{Pu}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{241}\text{Pu}$ ,  $^{242}\text{Pu}$ ,  $^{241}\text{Am}$ ,  $^{242\text{m}}\text{Am}$ , and  $^{243}\text{Am}$  are also relevant to radiological dose assessments.

# Time-dependent Nuclide Concentrations [2/2]

Showing nuclides relevant to radiological dose assessments



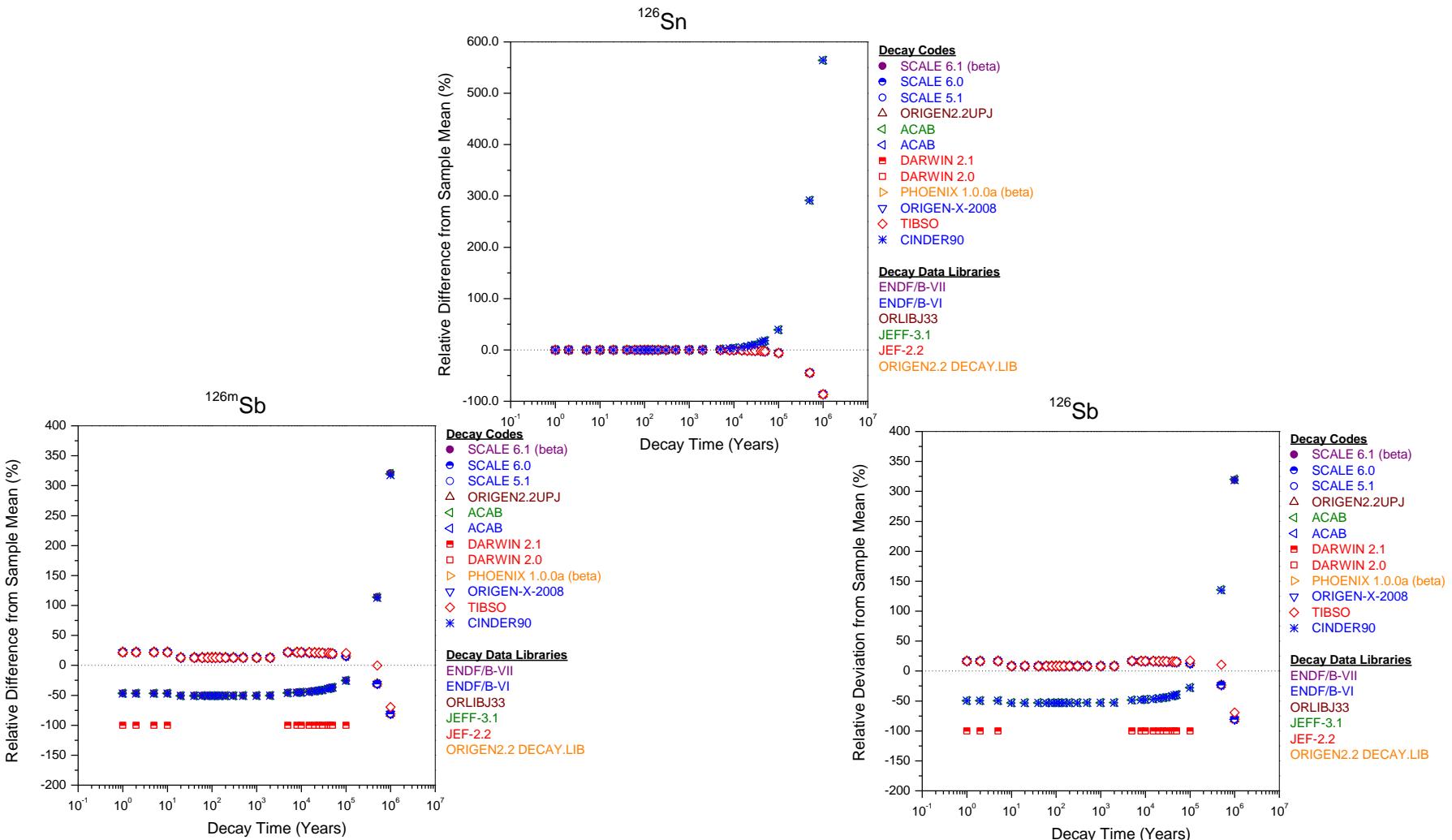
# Nuclides Important to Burnup Credit Criticality Safety Analyses

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- Negligible dispersions ( $\text{RSD} < 0.1\%$ ) of the calculated time-dependent concentrations for major actinide nuclides  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{238}\text{Pu}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ , and  $^{242}\text{Pu}$
- Insignificant dispersions of the calculated atom densities for stable fission product nuclides  $^{95}\text{Mo}$ ,  $^{103}\text{Rh}$ ,  $^{109}\text{Ag}$ ,  $^{133}\text{Cs}$ ,  $^{143}\text{Nd}$ ,  $^{147}\text{Sm}$ , and  $^{149}\text{Sm}$  whose concentrations slightly increase due to the decay of their short-lived precursors
- Dispersion of the decay calculation results ( $1\% < \text{RSD} < 5\%$ ) observed for  $^{99}\text{Tc}$ ,  $^{151}\text{Sm}$ ,  $^{155}\text{Gd}$ ,  $^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{241}\text{Pu}$ , and  $^{241}\text{Am}$

# Comparison of Decay Calculation Results [1/3]

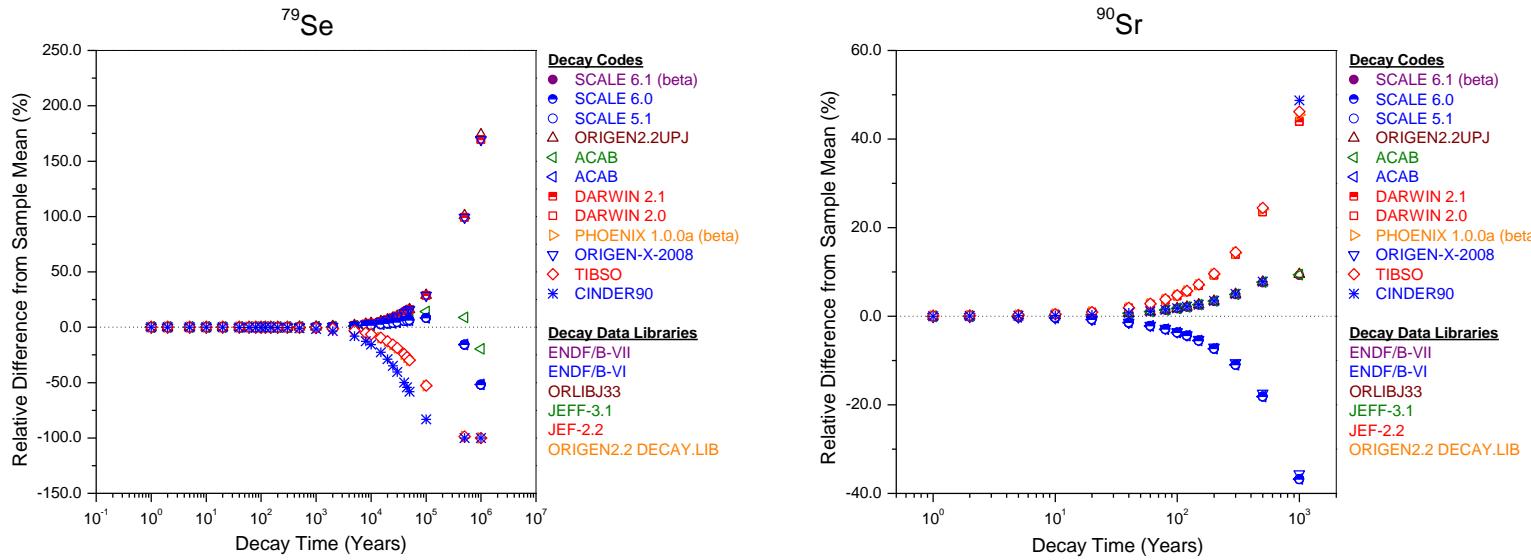
Showing the relative difference from sample mean for  $^{126}\text{Sn}$ ,  $^{126\text{m}}\text{Sb}$ , and  $^{126}\text{Sb}$



Library	ENDF/B-VII.0	ENDF/B-VI.8	JEFF-3.1	JEF-2.2	ORIGEN2.2-UPJ	ORIGEN 2.2
$^{126}\text{Sn}$ half-life (s)	7.25824E+12	3.15569E+12	7.25809E+12	3.15569E+12	3.15600E+12	3.15600E+12

# Comparison of Decay Calculation Results [2/3]

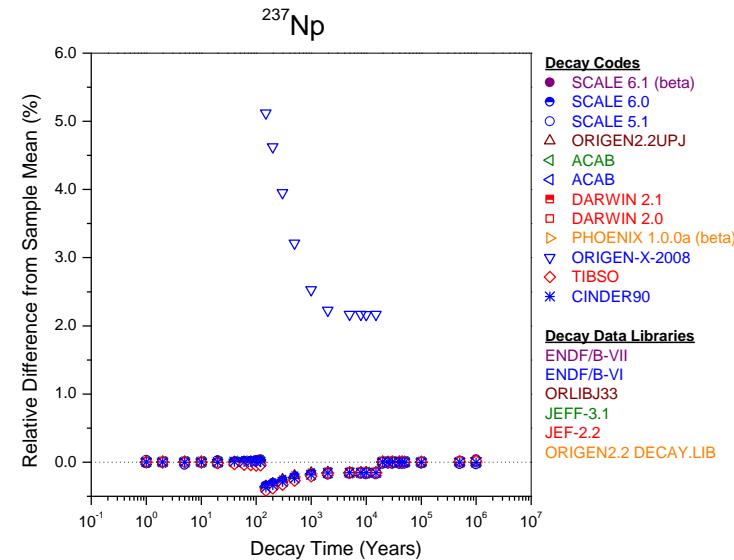
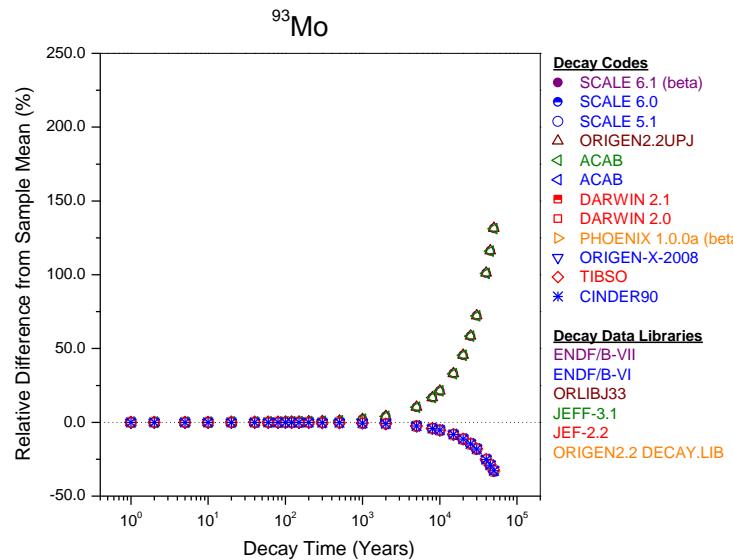
Showing the relative difference from sample mean for  $^{79}\text{Se}$  and  $^{90}\text{Sr}$



Library	ENDF/B-VII.0	ENDF/B-VI.8	JEFF-3.1	JEF-2.2	ORIGEN2.2-UPJ ORLIBJ33	ORIGEN 2.2 DECAY.LIB
$^{79}\text{Se}$ Half-life (s)	9.30949E+12	1.04138E+12	1.18970E+13	2.05120E+12	2.05124E+12	2.05000E+12
$^{90}\text{Sr}$ Half-life (s)	9.08543E+08	8.88327E+08	9.08524E+08	9.18938E+08	9.08226E+08	9.19000E+08

# Comparison of Decay Calculation Results [3/3]

Showing the relative difference from sample mean for  $^{93}\text{Mo}$  and  $^{237}\text{Np}$



Note: Small deviations might occur in the ORIGEN-X-2008 calculated concentrations for times beyond 150 years due to a splitting of the calculation and due to the choice of large time steps.

Library	ENDF/B-VII.0	ENDF/B-VI.8	JEFF-3.1	JEF-2.2	ORIGEN2.2-UPJ	ORIGEN 2.2
$^{93}\text{Mo}$ half-life (s)	1.26230E+11	1.10449E+11	1.26228E+11	1.10449E+11	1.26230E+11	1.10400E+11
$^{237}\text{Np}$ half-life (s)	6.76594E+13	6.75318E+13	6.75318E+13	6.75318E+13	6.75318E+13	6.75300E+13

# Factors Affecting the Accuracy of Decay Calculation Results

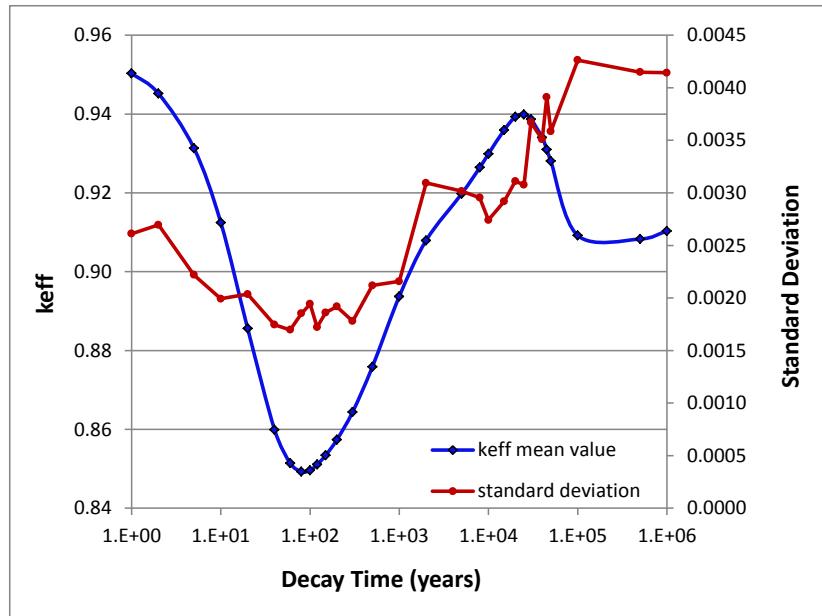
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- Different half-life values among the ENDF/B-VII.0, JEFF-3.1, ENDF/B-VI.8, and JEF-2 evaluations:
  - $^{14}\text{C}$ ,  $^{41}\text{Ca}$ ,  $^{59}\text{Ni}$ ,  $^{79}\text{Se}$ ,  $^{90}\text{Sr}$ ,  $^{94}\text{Nb}$ ,  $^{93}\text{Mo}$ ,  $^{99}\text{Tc}$ ,  $^{126}\text{Sn}$ ,  $^{151}\text{Sm}$ ,  $^{155}\text{Eu}$ ,  $^{229}\text{Th}$ ,  $^{232}\text{U}$ ,  $^{236}\text{Np}$ ,  $^{236}\text{Pu}$ , and  $^{246}\text{Cm}$
- Outdated half-life values in ORIGEN2.2 DECAY.LIB (based on ENDF/B-IV):
  - $^{41}\text{Ca}$ ,  $^{59}\text{Ni}$ ,  $^{93\text{m}}\text{Nb}$ ,  $^{228}\text{Ra}$ ,  $^{238}\text{Pu}$ ,  $^{239}\text{Pu}$ ,  $^{240}\text{Pu}$ ,  $^{242}\text{Pu}$ , and  $^{242\text{m}}\text{Am}$
- Different branching ratio values for  $^{93}\text{Zr}$  beta decay (0.95, 0.975, 1)
- Approximations related to the number of time steps allowed by a decay code, which affected contributions from short-lived precursor nuclides
- Neglected contributions from relevant precursor decay chains
  - $^{210}\text{Pb}$  and  $^{228}\text{Ra}$  time-dependent atom densities most impacted
- Numerical approximations made by the participants

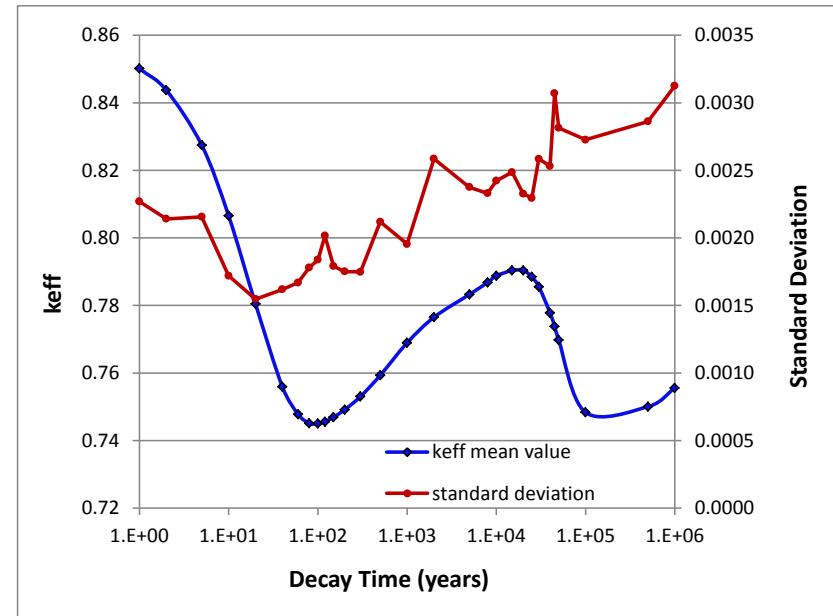
# CRITICALITY CALCULATION RESULTS

# $k_{\text{eff}}$ Values – Mean and Standard Deviation as a Function of Decay Time

	$\overline{k}_{\text{eff}}$	Standard Deviation
Fresh fuel	1.1485	0.0026
Discharged actinide-only compositions	0.9548	0.0027
Discharged actinide + FP compositions	0.8604	0.0021



Actinide-only nuclides



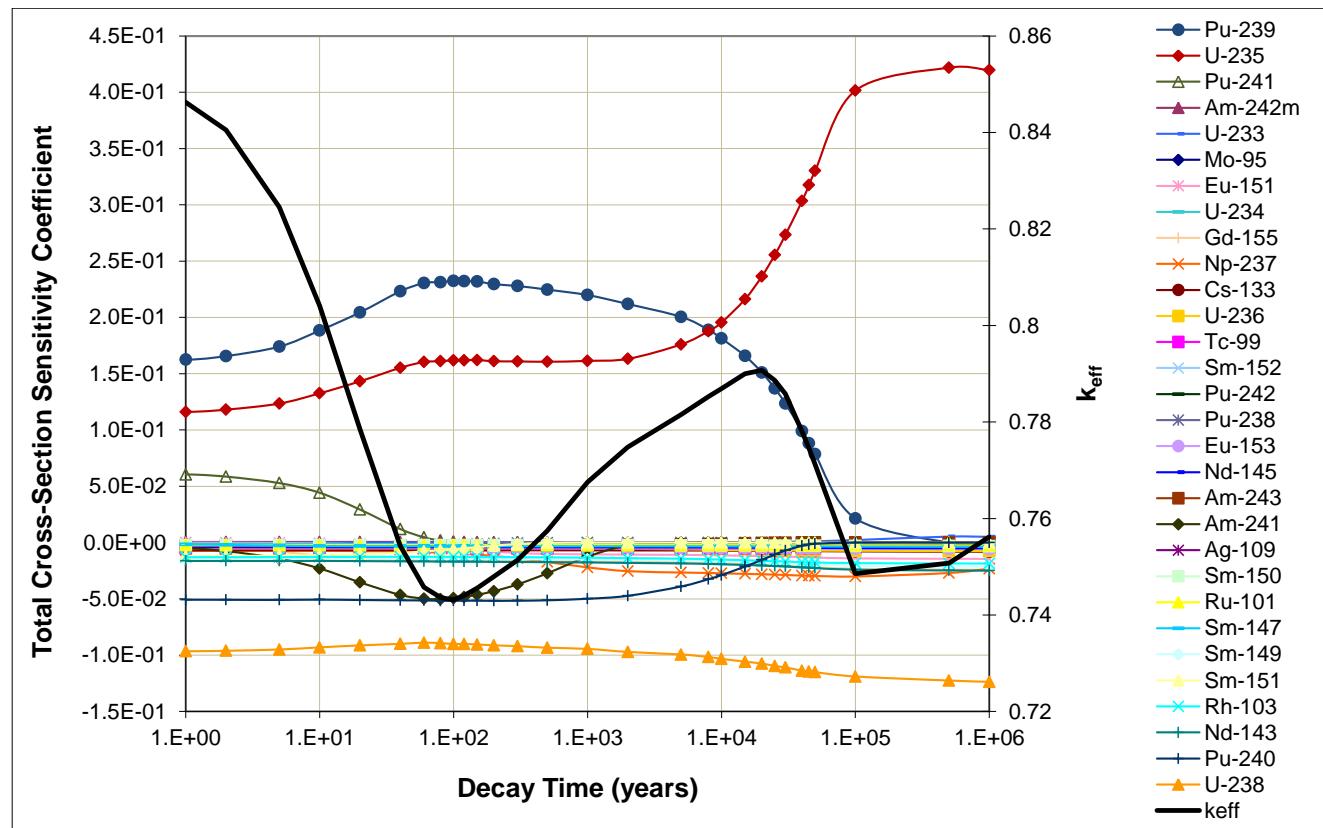
Actinides and FP nuclides

# Analysis of Criticality Calculation Results

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- Factors that may cause the variability of the criticality calculation results
  - Differences among nuclear cross-section data
  - Dispersion of decay calculation results for nuclides important to burnup credit ( $^{99}\text{Tc}$ ,  $^{151}\text{Sm}$ ,  $^{155}\text{Gd}$ ,  $^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{241}\text{Pu}$ , and  $^{241}\text{Am}$ )
  - Modeling and numerical approximations made by participants
- Cross-section sensitivity and uncertainty analysis performed using the TSUNAMI tools in SCALE to understand what may have caused the small dispersion of the criticality calculation results
  - Determined  $k_{\text{eff}}$  sensitivity to the total cross section of individual nuclides
    - Sensitivity coefficient: 
$$S_{k,\Sigma_x^n} = \frac{\delta k_{\text{eff}} / k_{\text{eff}}}{\delta \Sigma_x^n / \Sigma_x^n}$$
    - 238-group cross-section library based on ENDF/B-VII evaluations
  - Determined  $k_{\text{eff}}$  uncertainty (1 sigma confidence level) due to cross-section uncertainties
    - 44-group covariance data developed from ENDF/B-VII, ENDF/B-VI, and JENDL3.3 evaluations

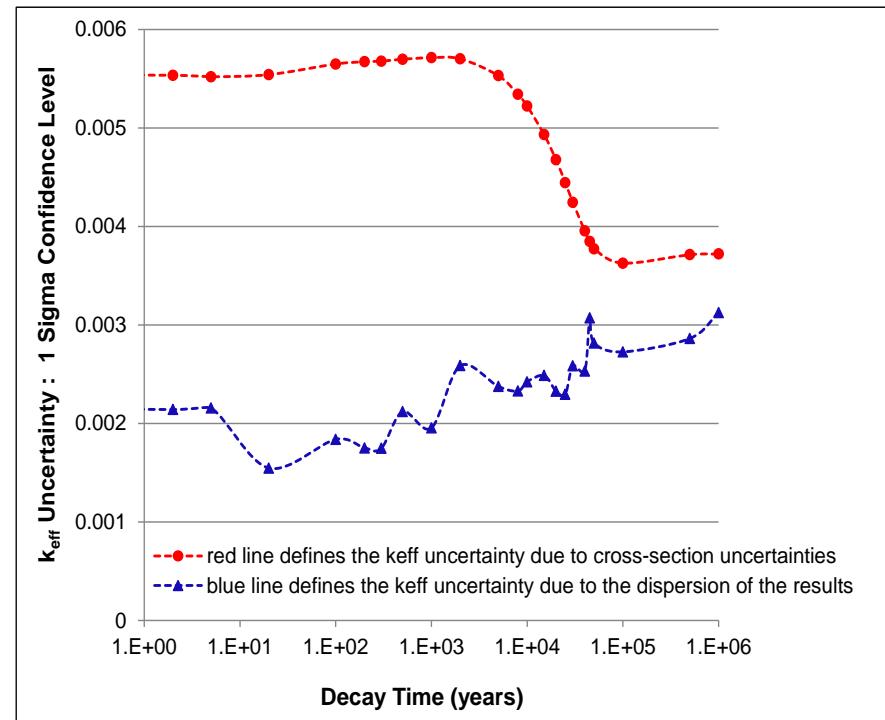
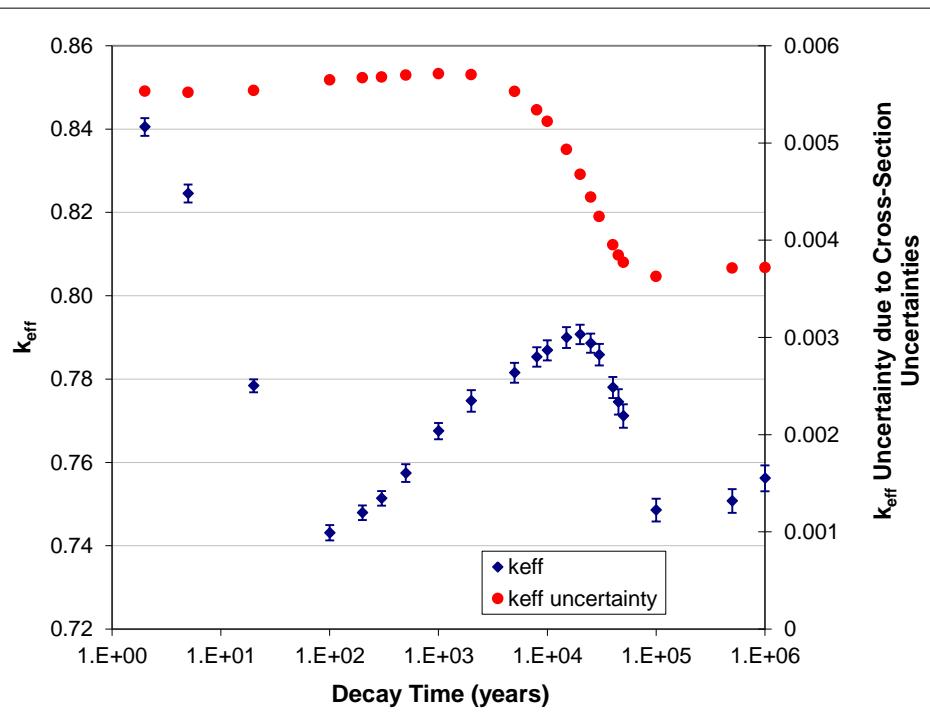
# $k_{\text{eff}}$ Sensitivity to ENDF/B-VII Total Cross-Section Data for Actinides and Fission Product Nuclides



- $k_{\text{eff}}$  has large sensitivities to perturbations in  $^{239}\text{Pu}$ ,  $^{235}\text{U}$ , and  $^{238}\text{U}$  cross-section data
- $k_{\text{eff}}$  has negligible sensitivities to perturbations in the cross-section data of the nuclides for which slightly different atom densities were calculated ( $^{99}\text{Tc}$ ,  $^{151}\text{Sm}$ ,  $^{155}\text{Gd}$ ,  $^{233}\text{U}$ ,  $^{234}\text{U}$ ,  $^{237}\text{Np}$ ,  $^{241}\text{Pu}$ , and  $^{241}\text{Am}$ )

# $k_{\text{eff}}$ Uncertainty Due to Cross-Section Uncertainties

## Showing the results for Actinide and Fission Product Fuel Compositions



Note: Error bars show the uncertainty in  $k_{\text{eff}}$  due to uncertainties associated with cross-section data.

- Variability of the benchmark  $k_{\text{eff}}$  results
  - Bounded by the uncertainty in  $k_{\text{eff}}$  due to cross-section covariance data
  - May be predominantly attributed to the criticality calculation methods and cross-section data

# Conclusions of the OECD/NEA Phase VII Benchmark Results

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- 15 organizations in 10 countries contributed
  - 15 decay calculations using 12 different decay codes/data libraries
  - 15 criticality calculations using 13 different criticality codes/nuclear cross-section data libraries
- Time-dependent concentrations for major burnup credit actinides and fission product nuclides were very similar
- Small dispersions (RSD < 5%) of the decay calculation results for some of the nuclides important to burnup credit
- Significant variability of the decay calculation results for  $^{79}\text{Se}$ ,  $^{90}\text{Sr}$ ,  $^{126}\text{Sn}$ ,  $^{126m}\text{Sb}$ , and  $^{126}\text{Sb}$  (nuclides important to radiation dose assessments)
- Small variability of the benchmark criticality results (RSD < 0.5%)
- Variability of the decay calculation results may be attributed to:
  - Different half-life and branching ratio values among the evaluated libraries
  - Approximations related to the number of time steps allowed by a decay code
  - Neglected contributions from relevant precursor decay chains (e.g.,  $^{210}\text{Pb}$  and  $^{228}\text{Ra}$ )
- Variability of the  $k_{\text{eff}}$  results may be predominantly attributed to differences among the evaluated criticality calculation methods and cross-section data

# Acknowledgements

- This manuscript has been authored by UT-Battelle, LLC, under contract DE-AC05-00OR22725 with the U.S. Department of Energy.
- The participants in the burnup credit criticality benchmark study are: V. Chrapčiak (VUJE, Slovak Republic); G. Radulescu (Oak Ridge National Laboratory, USA); K. Ohkubo, H. Okuno, and K. Suyama (Japan Atomic Energy Agency, Japan); D. Mennerdahl (E Mennerdahl Systems, Sweden); O. Cabellos, B. Cabellos, N. Garcia-Herranz, and J. Sanz (Universidad Politécnica de Madrid, Spain); J. M. Conde and C. Alejano (CSN, Spain); P. Ortego and C. Tore (SEA Ingenieria, SL., Spain); M. Tardy and A. Peillet (AREVA TN International, France); L. Jutier, W. Haeck, Y. Liegard, I. O. Echevarria, and J. Thevenin [Institut de Radioprotection et de Sûreté Nucléaire (IRSN), France] ; M. Wagner, R. Kilger, U. Hesse, and M. Behler [Gesellschaft für Anlagen- und Reaktorsicherheit (GRS) mbH, Germany]; F. Havluj (Nuclear Research Institute at Rez, Czech Republic); K. Rantamäki and M. Anttila (VTT Technical Research Centre of Finland, Finland); G. Hordosy, P. Vertes, and A. Brolly (KFKI Atomic Energy Research Institute, Hungary); S. P. Szabo (Anandor Ltd., Hungary); and H. Trellue (Los Alamos National Laboratory, USA).